

# Colloidal Processing of Alumina-Zirconia Composites

**Pradip**

**Tata Research Development & Design Centre, Pune, India**

**[pradip.p@tcs.com](mailto:pradip.p@tcs.com)**

## Acknowledgements

- Department of Science & Technology
- National Institute of Standards and Technology, USA
- R S Premachandran
- Vijay Ramakrishnan
- S. Sivakumar
- S. Manjunath
- S.G. Malghan
- Sandhya Thaokar
- S. Krishnamurty
- Beena Rai
- P. Sathish
- P.C. Kapur

# Nanoparticles – Synthesis and Processing

- **Technology Forecasting**
  - **Global market**
    - \$1 Trillion by 2015 (NSF, USA)
    - \$225 billion by 2005 (Nanobusiness Alliance)
- **Current World Market for Nanomaterials ~ \$900 million**
  - **Electronic, magnetic & optoelectronic** **74%**
  - **Biomedical, pharmaceutical & cosmetics** **16%**
  - **Energy, catalytic & structural** **10%**

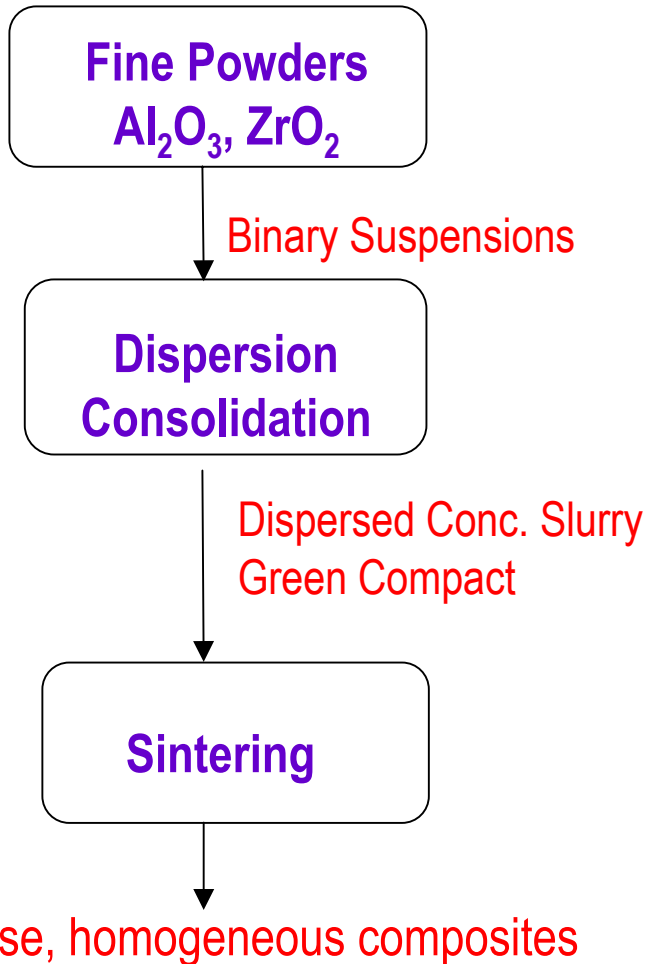
# Applications in the Near Future

- Fuel Cells
- Silicon Carbide/Nitride Nanocomposites
- Fe-Nd-B alloys
- Nanosensors
- Drug Delivery Systems
- Bio-implants

# Advanced Ceramics and Colloidal Processing

- Higher fracture toughness and strength due to transformation toughening – crystallite size is important
- Colloidal processing of submicron particles enables better homogenization, dispersion and control of microstructure in the green compact and the final product; Superior properties, Reduction in rejection rates; Lower sintering temperatures
- Slip/tape/gel casting/pressure filtration

# Colloidal Processing Program at TRDDC



*Size, Shape, Morphology*  
*Dopants, Purity*  
*Physico - Chemical Characterization*  
*Surface - Chemical Properties*

*Extent of Dispersion,*  
*Design of dispersants, Packing*  
*Sediment Volume, Settling Rate*  
*Agglomerate Size and Distribution*  
*Rheology - Viscosity and Yield Stress*

*Structure - Property Relationships*  
*Evolution of Grain / Pore Size Distribution*  
*Sintering Kinetics*  
*Porosity / Strength*

## Selected Topics for Presentation

- Rheology: mixed colloidal suspensions of alumina-zirconia
- Dispersion: colloidal alumina, zirconia, barium titanate suspensions
- Simulation and control of the evolution of microstructure during solid state sintering

# Physical and Surface Chemical Characteristics of Powder Samples

Powder	Source	BET surface area (m <sup>2</sup> /g)	Average particle size d <sub>50</sub> nm	PZC (pH)
Alumina (A-16)	Alcoa, USA	9.3	380	9.9
Zirconia (SY5.2)	Z Tech, Australia	14.9	210	6.65
Silicon nitride (SNE-10)	Ube, Japan	10.1	400	6.5

# Rheology of Colloidal Suspensions

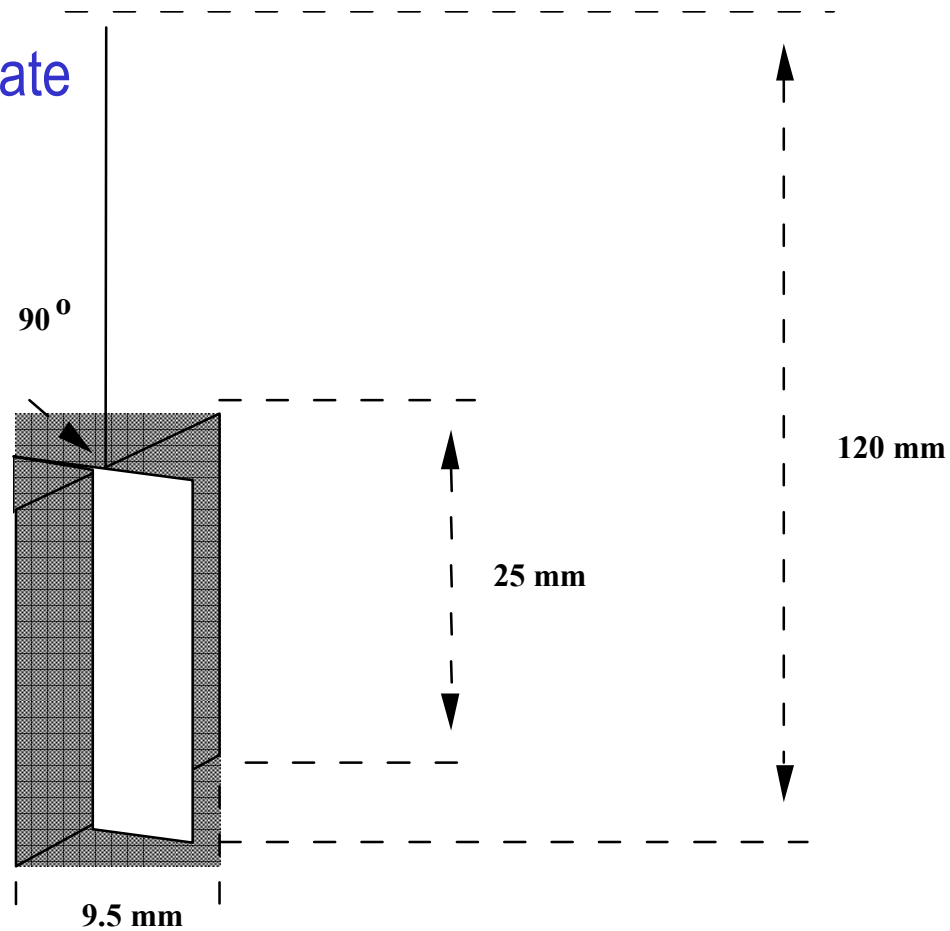
## Measurement of shear yield stress, $\tau$

- Indirect method
  - Estimation of  $\tau$  from power law models
- Direct method
  - Vane method\*

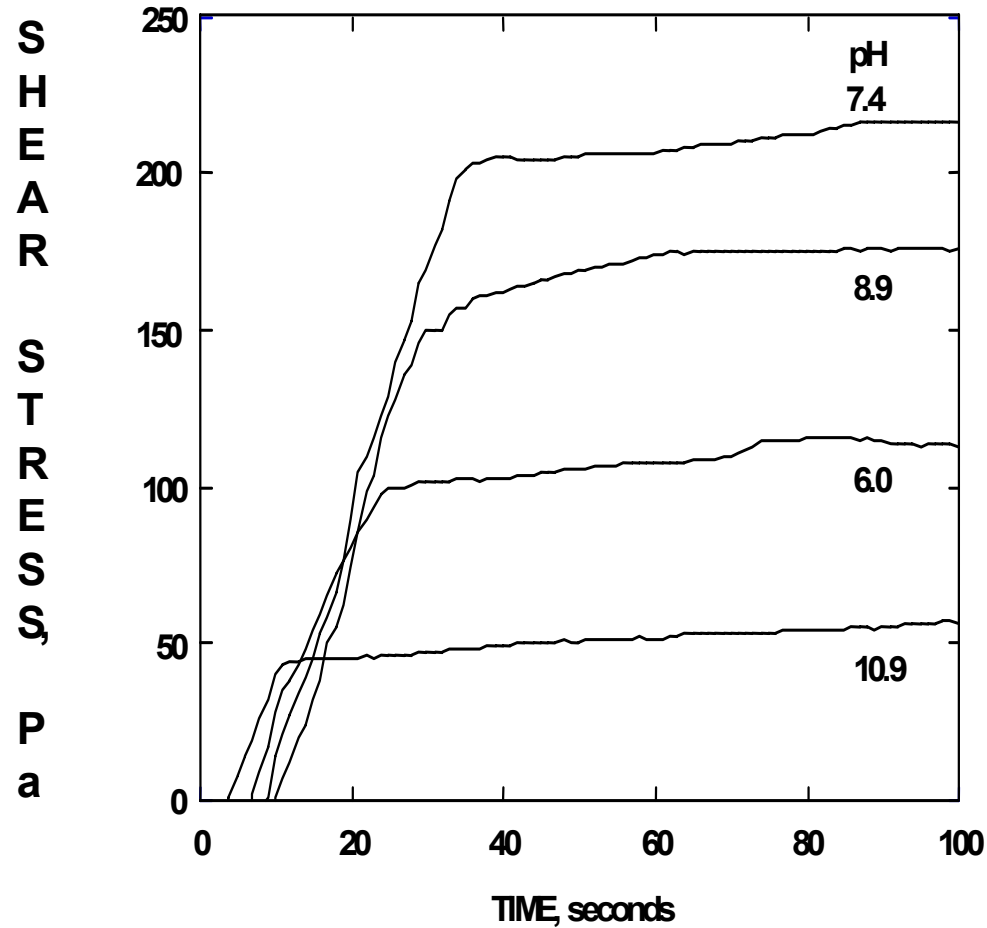
\*[Ref: Nguyen, Q.D., Boger, D.V., 1985, J. Rheol. (NY) 29[3], 335-347

# Direct Measurement - the Vane Spindle

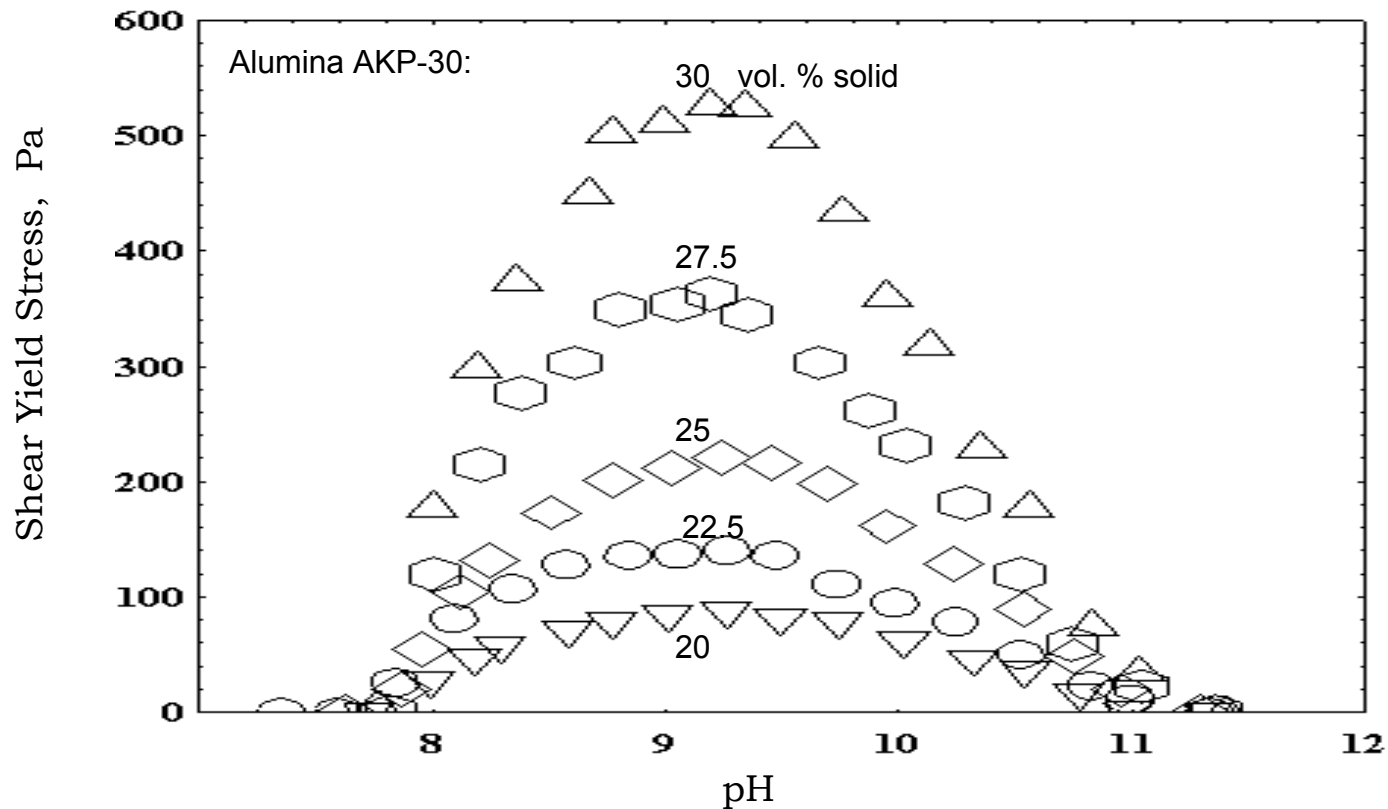
Rotated at  
 $0.1 \text{ s}^{-1}$  shear rate



# Typical Data from Vane Rheometer

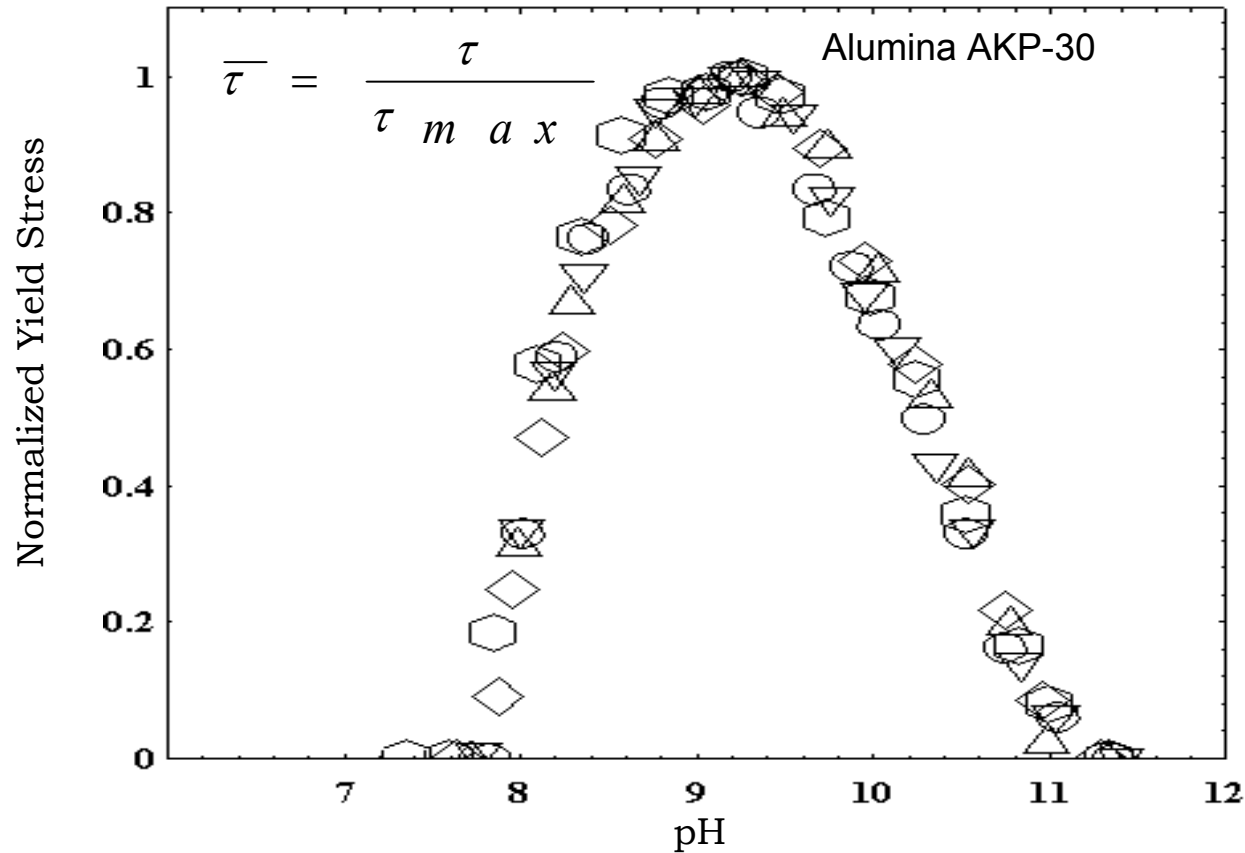


# Shear Yield Stress: Effect of Solid Loading & pH



[Ref: P.J. Scales et al, AIChE J. 44 (3) (1998) 538-544

# Yield Stress: Self-similar Normalized Curves



[Ref: P.J. Scales et al, AIChE J. 44 (3) (1998) 538-544]

# Shear Yield Stress - Model Equations

$$\bar{P} = \frac{P(\text{pH})}{P(\text{iep})} = 1 + \frac{F_{\text{dl}}}{F_{\text{vw}}}$$

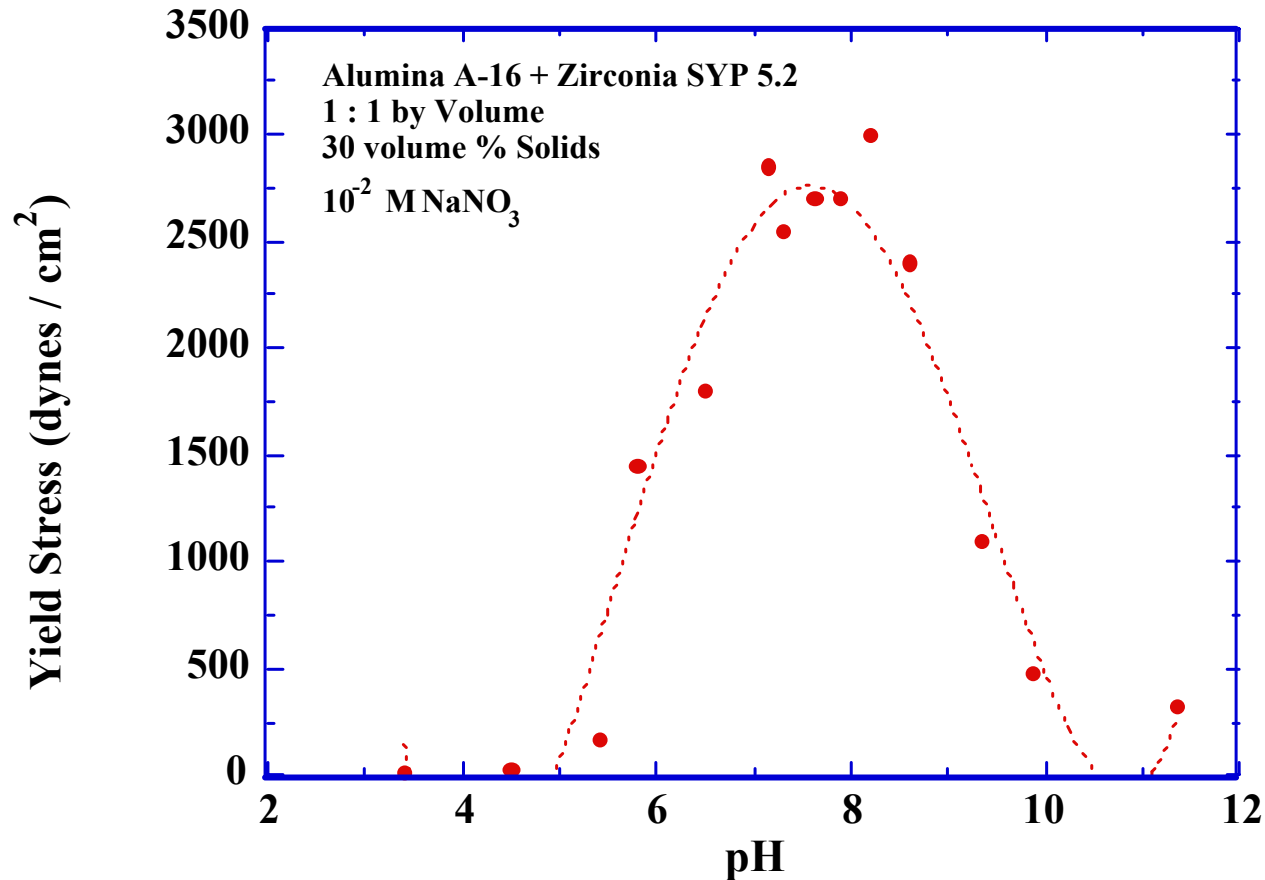
$$F_{\text{dl}} = \frac{a_1 a_2 \varepsilon \kappa (\psi_{01}^2 - 2\psi_{01} \psi_{02} e^{(h_0 \kappa)} + \psi_{02}^2)}{2(a_1 + a_2) (e^{(2h_0 \kappa)} - 1)}$$

$$F_{\text{vw}} = \frac{A a_1 a_2}{6(a_1 + a_2) h_0^2}$$

$$P_{\text{(overall)}} = \phi_{\text{al}}^2 P_{\text{al}} + \phi_{\text{zr}}^2 P_{\text{zr}} + 2\phi_{\text{al}} \phi_{\text{zr}} P_{\text{al-zr}}$$

(Ref: Ramkrishnan, V. et al J. Am. Ceram. Soc. 79 (1996) 2567)

# Yield Stress of Alumina-Zirconia Suspensions



Ref: Ramkrishnan, V. et al J. Am. Ceram. Soc. 79 (1996) 2567

# Shear Yield Stress in Suspensions of Size Distributed Multi-Component Powders

- Model Based on DLVO Theory incorporating
  - Particle Size Distribution
  - Solids Loading
  - pH Effect
  - Electrolyte Concentration
  - Mixtures of Powders
- Validated with experimental data on Zirconia, Alumina and Alumina-Zirconia synthetic mixtures

# Model Equations

## Shear Yield Stress

$$\tau = \frac{0.011}{\pi} \phi K(\phi) \left[ \frac{A}{h^2(\phi)} - \frac{24\pi\epsilon\kappa\zeta^2}{(1+e^{h(\phi)\kappa})} \right] \times \sum_j \frac{S_j}{X_j} \sum_i S_i \left[ \frac{X_i}{X_j + X_i - \sqrt{X_j^2 + 2X_i X_j}} \right]$$

## Maximum Shear Yield Stress

( z=0 )

$$\tau_{\max} = \frac{0.011}{\pi} \frac{\phi K(\phi) A}{h^2(\phi)} \times \sum_j \frac{S_j}{X_j} \sum_i S_i \left[ \frac{X_i}{X_j + X_i - \sqrt{X_j^2 + 2X_i X_j}} \right]$$

## Normalized Shear Yield Stress ( $\tau/\tau_{\max}$ )

$$\bar{\tau} = 1 - \frac{24\pi\epsilon\kappa\zeta^2 h^2(\phi)}{A(1+e^{\kappa h(\phi)})}; 0 \leq \bar{\tau} \leq 1$$

(Ref: Manjunath S. et al, Chem. Eng. Sci. 53 (1998) 3073)

# Yield Stress of Mixed Suspensions

$$A_{Al-Zr} = \sqrt{A_{Al}A_{Zr}}$$

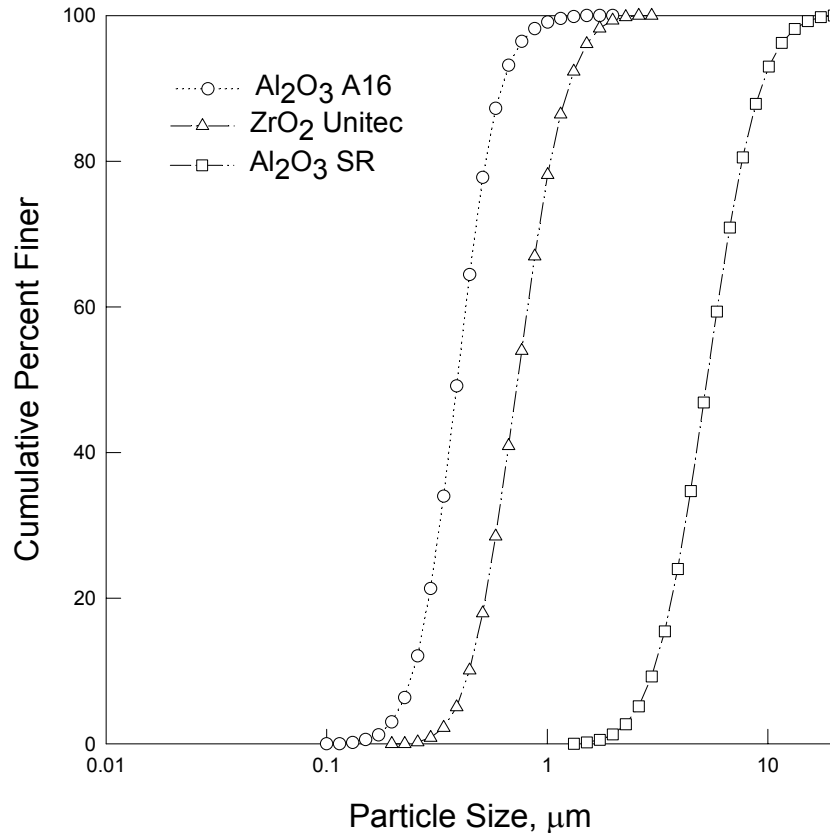
$$h_{Al-Zr} = \frac{h_{Al} + h_{Zr}}{2}$$

$$f_{Al-Zr} = v_{Al}f_{Al} + v_{Zr}f_{Zr}$$

$$P_{mix} = \frac{0.011\phi K(\phi)}{\pi} \left[ v_{Al}^2 \frac{A_{Al}}{h_{Al}^2} \Xi(f_{Al}) + v_{Zr}^2 \frac{A_{Zr}}{h_{Zr}^2} \Xi(f_{Zr}) + 2v_{Al}v_{Zr} \frac{A_{Al-Zr}}{h_{Al-Zr}^2} \Xi(f_{Al-Zr}) \right]$$

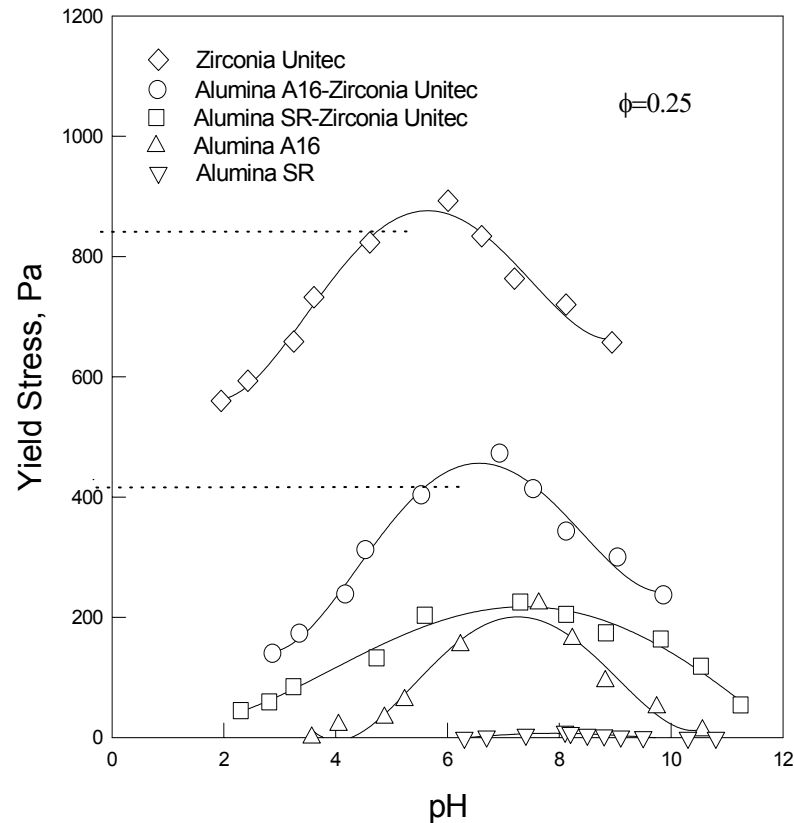
Ref: Manjunath S. et al, Chem. Eng. Sci. 53 (1998) 3073 and

# Particle Size Distribution of Powders



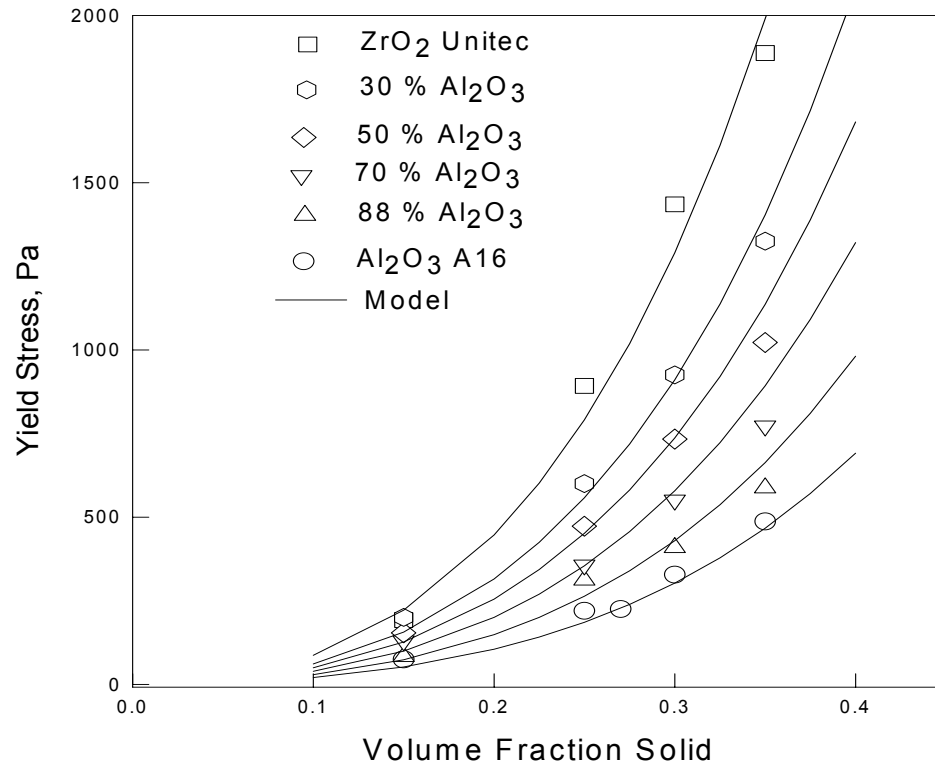
Ref: Manjunath S. et al, Chem. Eng. Sci. 53 (1998) 3073

# Shear Yield Stress of Mixed Suspensions



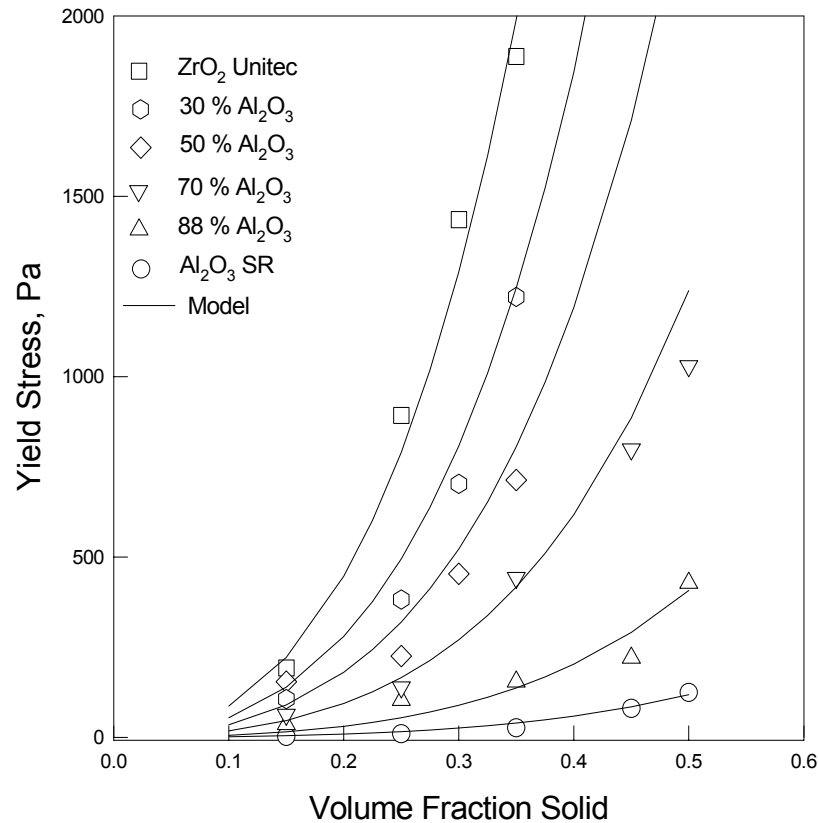
Ref: Manjunath S. et al, Chem. Eng. Sci. 53 (1998) 3073

# Yield Stress of Alumina-Zirconia Suspensions



Ref: Manjunath S. et al, Chem. Eng. Sci. 53 (1998) 3073

# Yield Stress of Alumina-Zirconia Suspensions

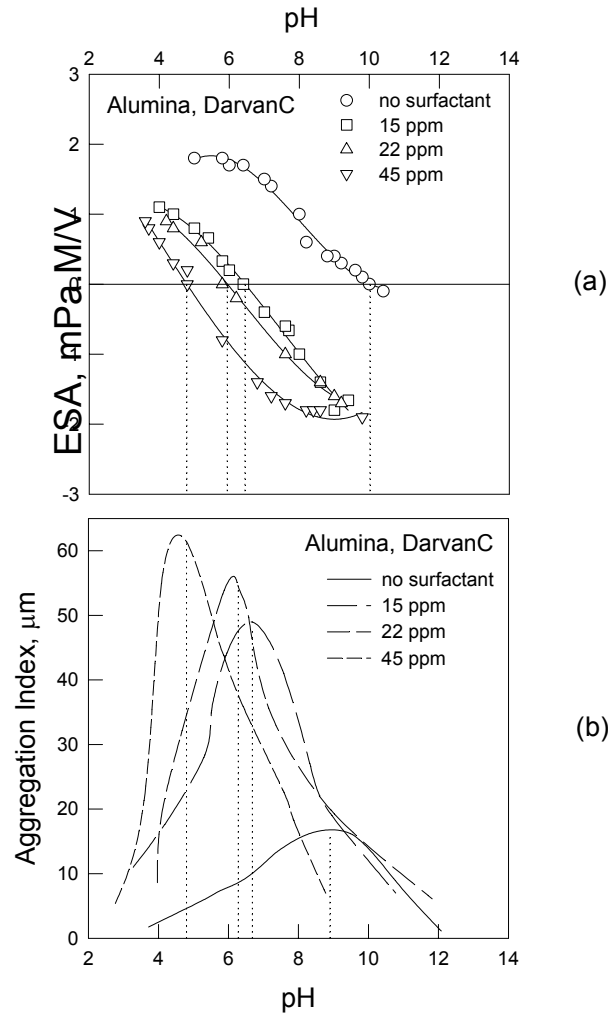


Ref: Manjunath S. et al, Chem. Eng. Sci. 53 (1998) 3073

# Aggregation-Dispersion of Colloidal Suspensions in presence of Additives

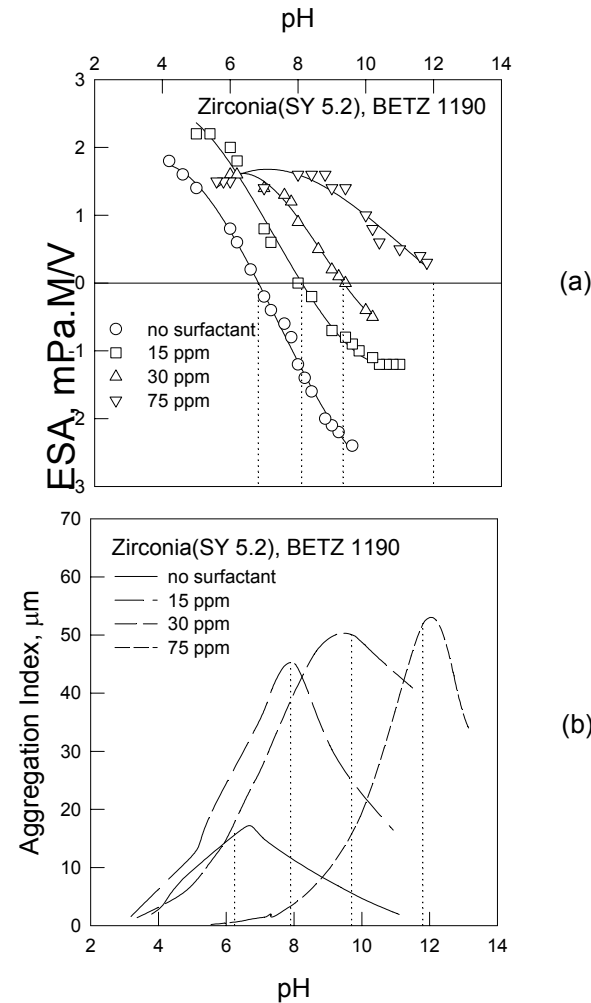
- Electrostatic, Steric and Electrosteric
- Shift in IEP
- Maximum aggregation at IEP
- Shift in IEP related to extent of adsorption (a measure of the affinity of the additive for the substrate)
- Aggregation possible even in presence of dispersant (at IEP)

# Aggregation Index of Alumina Suspensions with Darvan C



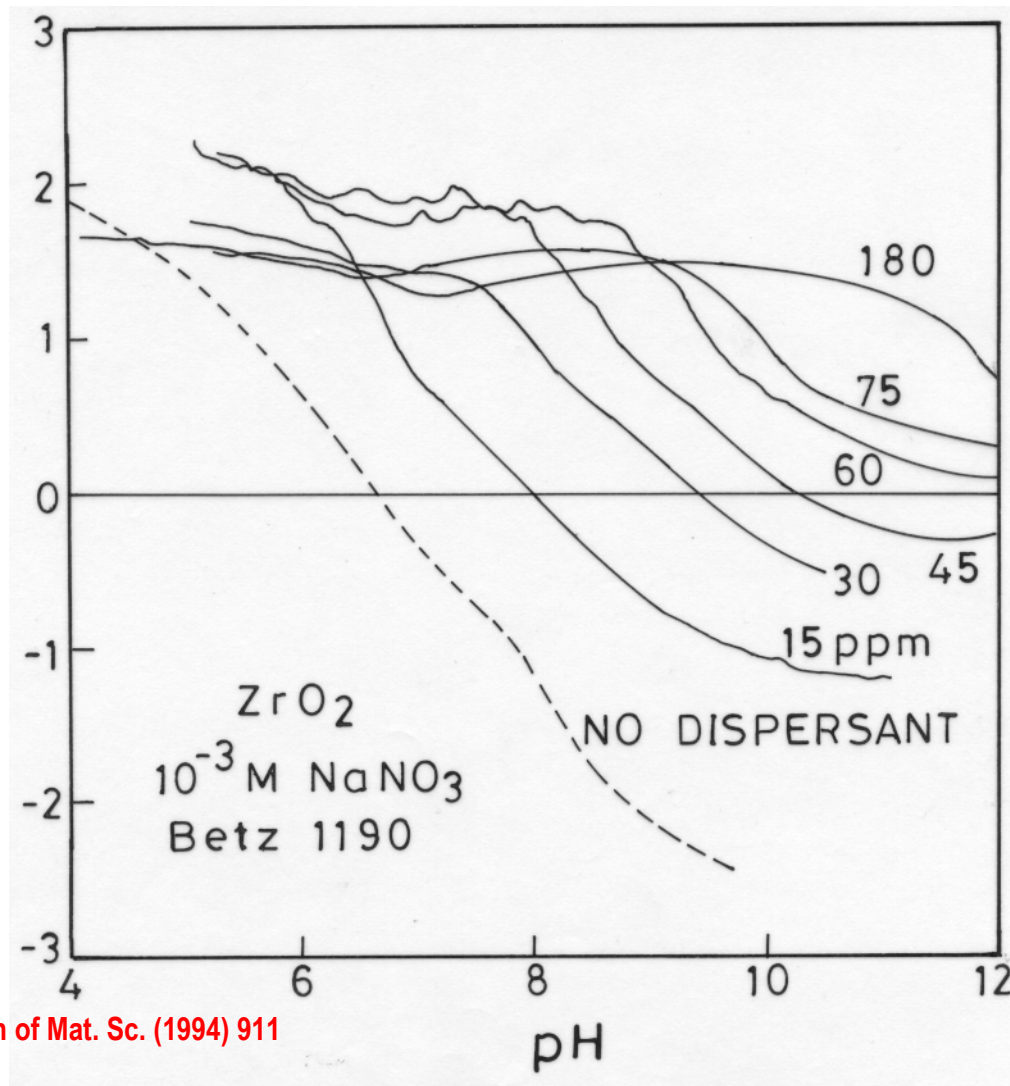
M. Subbanna et al., Langmuir, 14 (1998), 7364

# Aggregation Index of Zirconia Suspensions with BETZ 1190



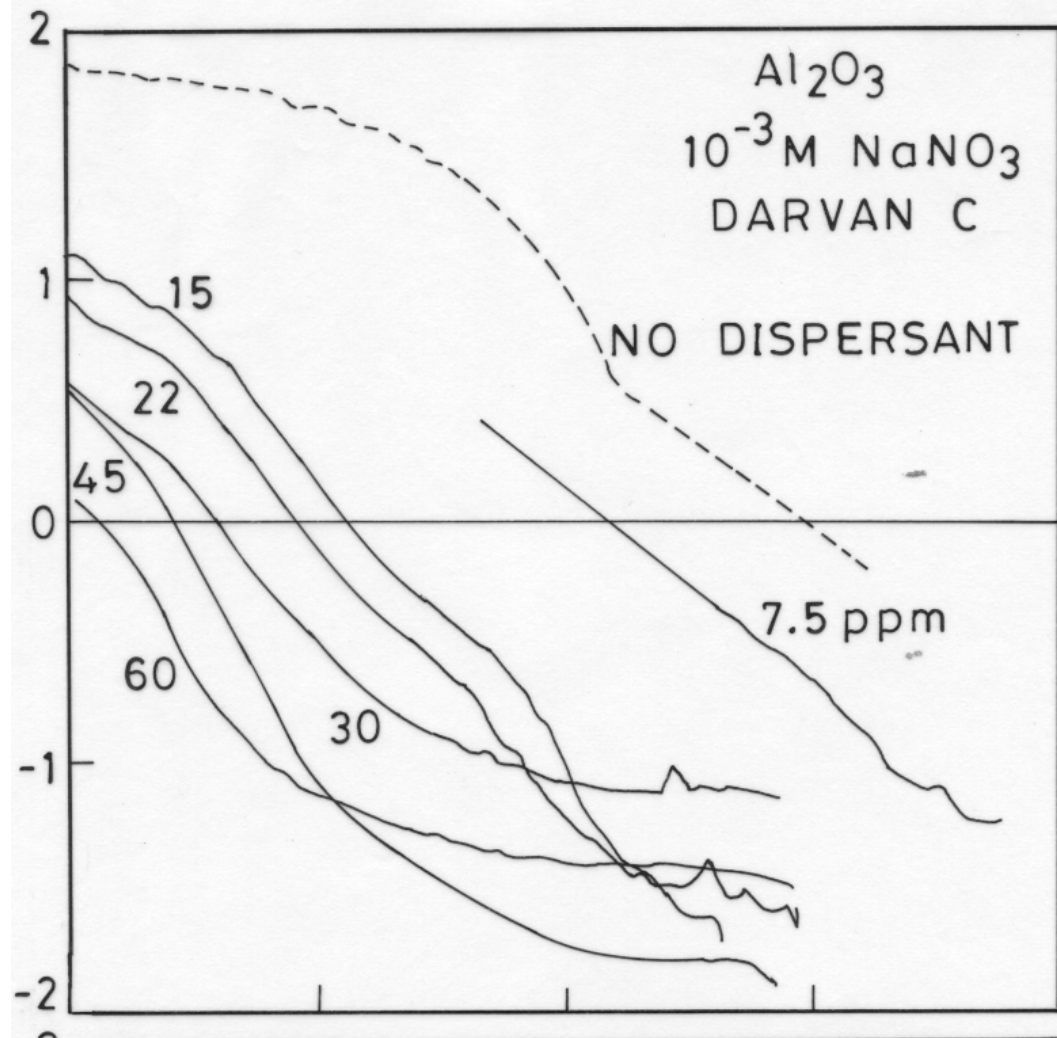
M. Subbanna et al., Langmuir, 14 (1998), 7364

# Zirconia – Betz 1190

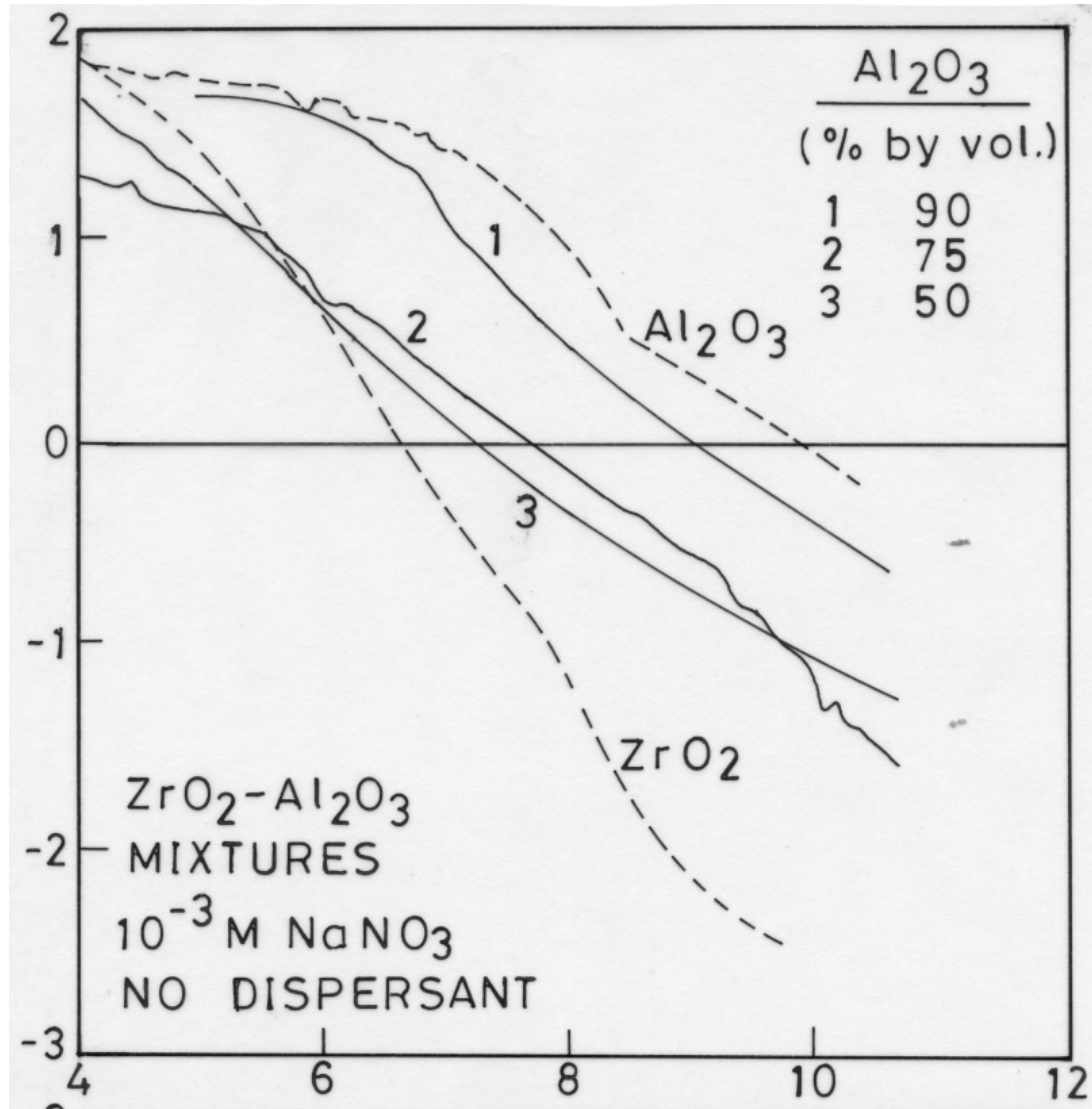


Pradip et al. Bulletin of Mat. Sc. (1994) 911

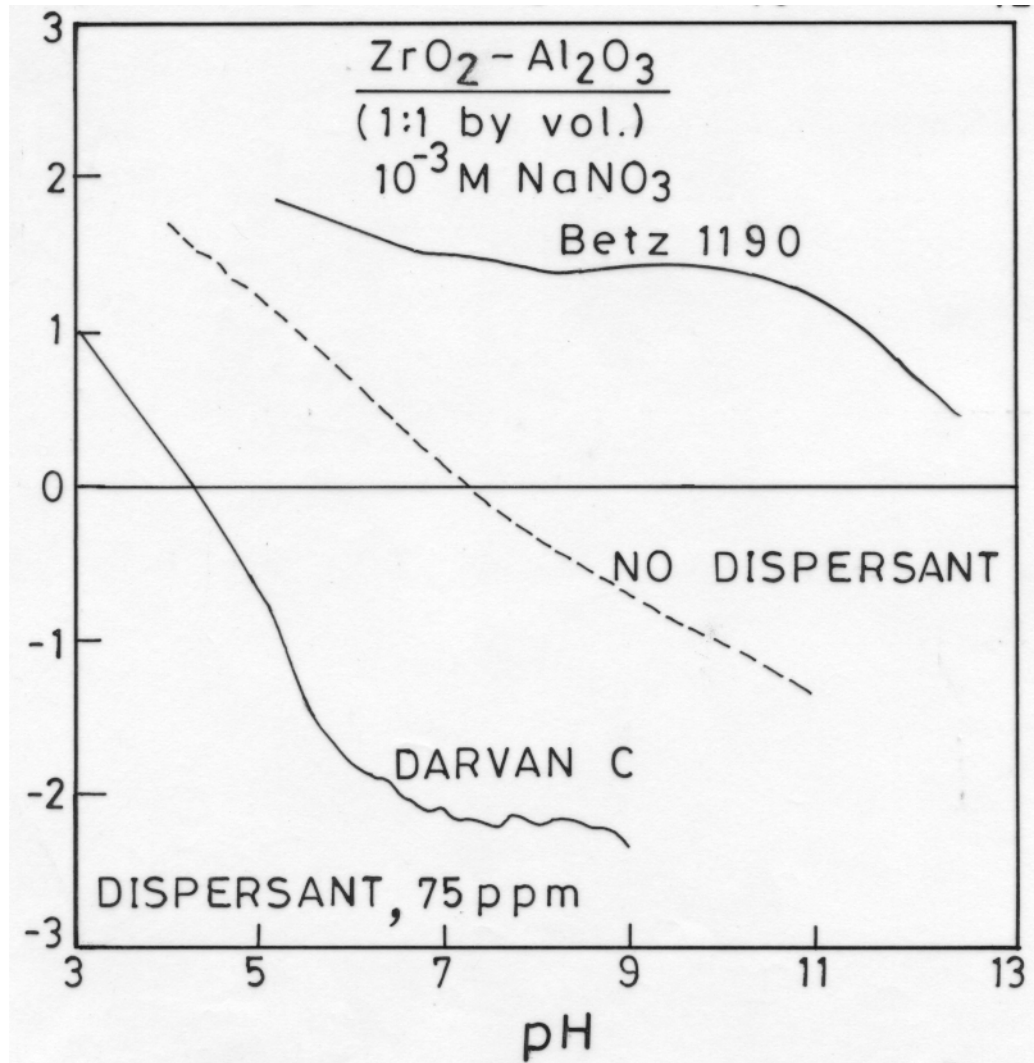
# Alumina – Darvan C



# Zirconia – Alumina Synthetic Mixtures



# Zirconia – Alumina Mixtures & Dispersants



## Co-relation of the Extent of Dispersion as Measured through d50, the Mean Size

System	pH <sub>i</sub>	(pH <sub>i</sub> -pH <sub>IEP</sub> )	Dispersion	
			d <sub>50</sub> nm	Remarks
Alumina (A-16) No dispersant (pH <sub>IEP</sub> 9.9)	4	5.9	0.38	W
	10	1.1	3.59	N
With 75 ppm Darvan-C (pH <sub>IEP</sub> 4.5)	4	0.5	4.18	N
	10	5.5	0.38	W
With 150 ppm Betz 1190 (pH <sub>IEP</sub> > 10)	4	>6	0.39	W
	8.1	>2	0.38	W

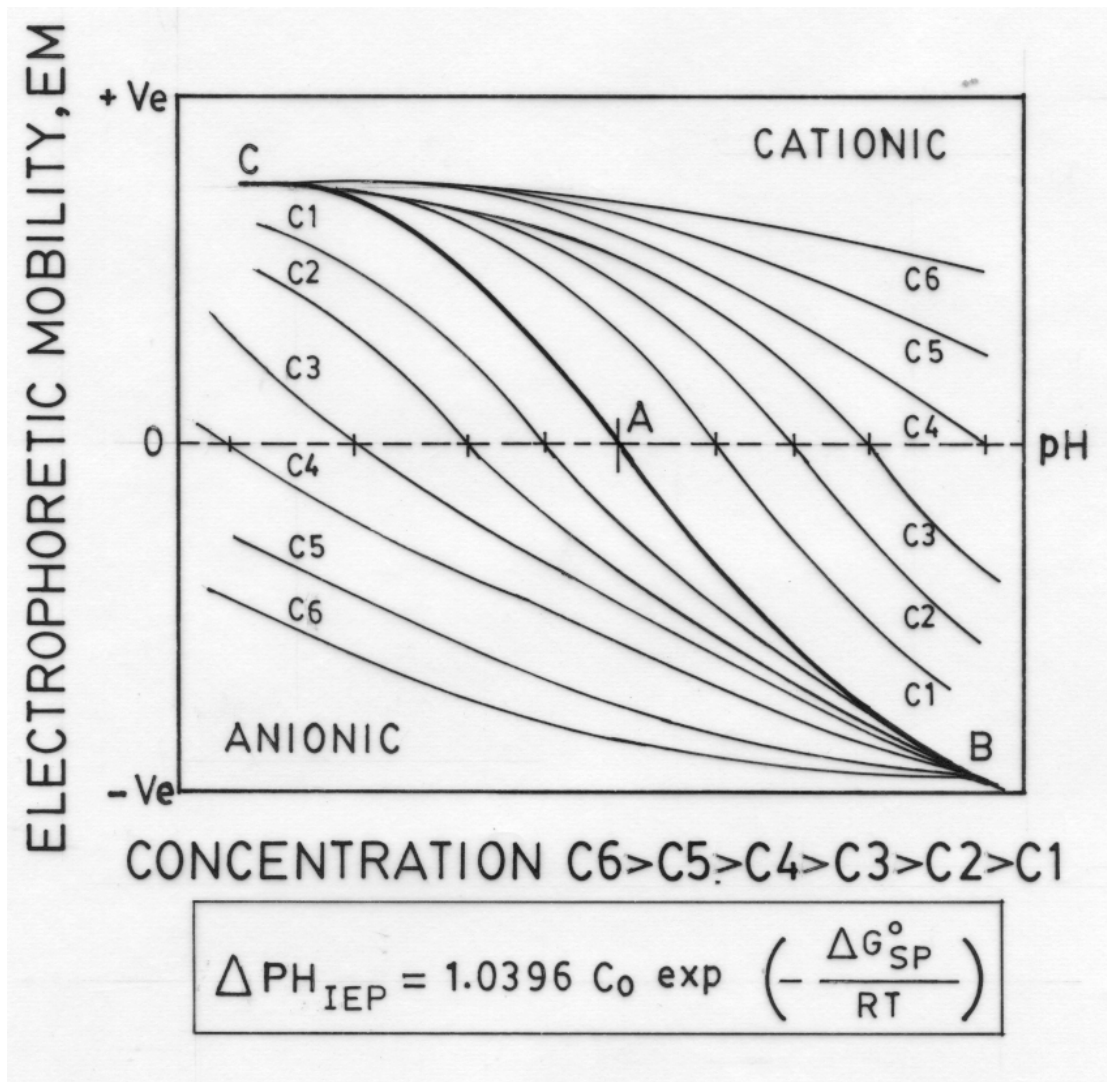
(Contd.)

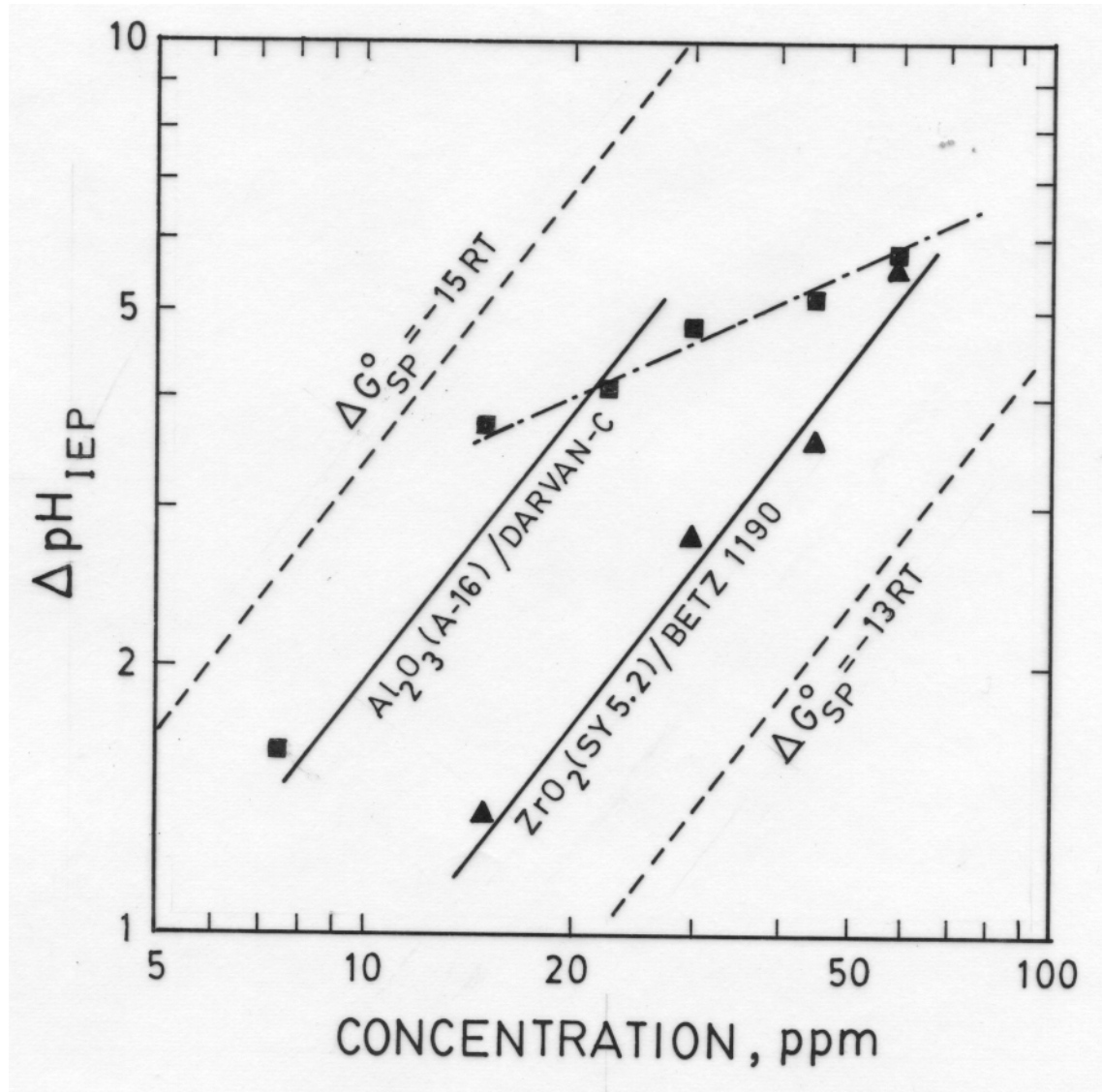
System	pH <sub>i</sub>	(pH <sub>i</sub> -pH <sub>IEP</sub> )	Dispersion		
			d <sub>50</sub> nm	Remarks	
Zirconia (SY 5.2)	No dispersant (pH <sub>IEP</sub> 6.65)	4	2.7	0.21	W
		4	~0	9.8	N
	With 75 ppm Darvan-C (pH <sub>IEP</sub> 4)	7.4	3.4	0.21	W
		9.1	5.1	0.21	W
	With 150 ppm Betz 1190 (pH <sub>IEP</sub> > 12)	6.3	>5.7	0.21	W

(Contd.)

System	pH <sub>i</sub>	(pH <sub>i</sub> -pH <sub>IEP</sub> )	Dispersion	
			d <sub>50</sub> nm	Remarks
Silicon nitride (SNE-10)				
With 25 ppm Darvan-C (pH <sub>IEP</sub> 4.1)	9	4.9	0.4	W
With 25 ppm Betz 1190 (pH <sub>IEP</sub> > 12)	7.4	3.4	0.21	W
	9.1	5.1	0.21	W

# Shift in IEP in Presence of Dispersants





# Rational Design of Additives/Dispersants

- Paradigm Shift
  - Tailor-made additives and reagents
  - Rational design/selection based on
    - Identification of molecular recognition mechanisms
    - Molecular modeling of surface-reagent interactions
      - Interaction Energy Computations
        - » Force field/quantum mechanical
      - Molecular Dynamics Simulation
        - » Conformation/orientation and nature of adsorbed layers (self assembly)

# Molecular Modeling Methods

## Quantum Mechanics

- Ab initio (HF, MP2)
- DFT
- Semi-empirical  
EHMO, CNDO,  
MINDO, MNDO,  
ZINDO

## Force Field

- MM2
- AMBER
- OPLS
- UFF
- Drieding
- COMPASS

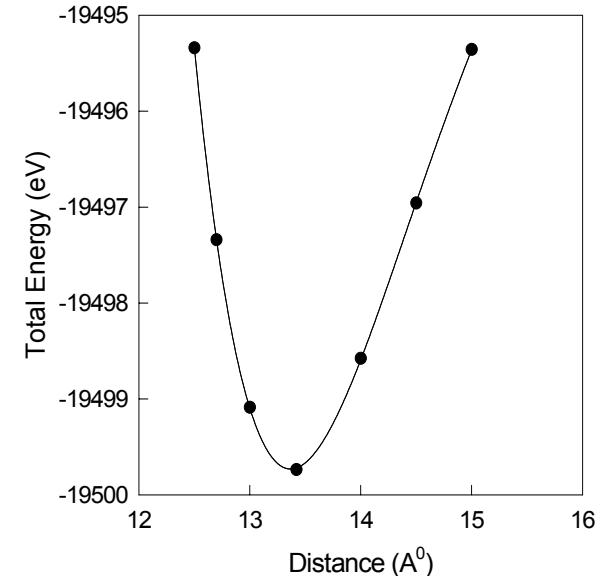
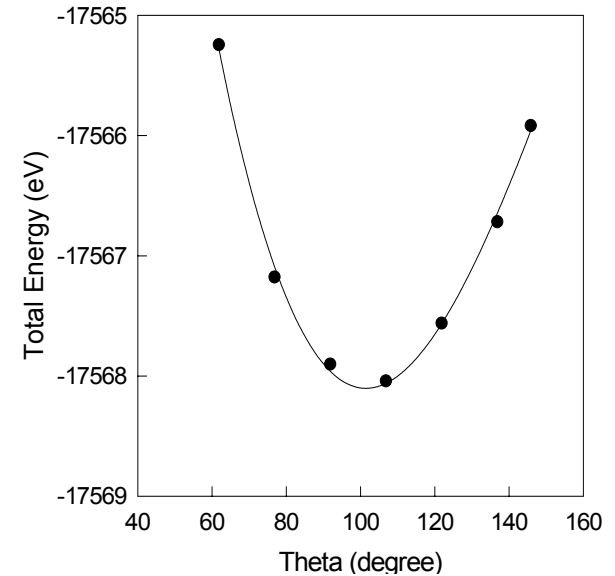
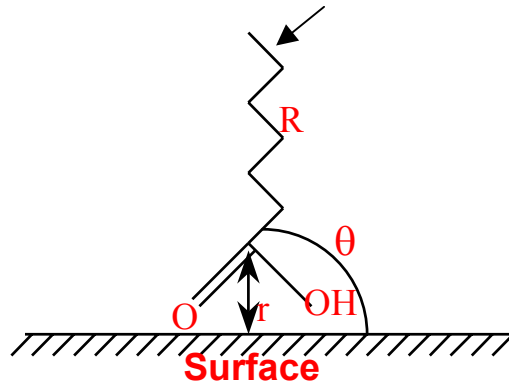
## Molecular Dynamics

- NVE
- NVT

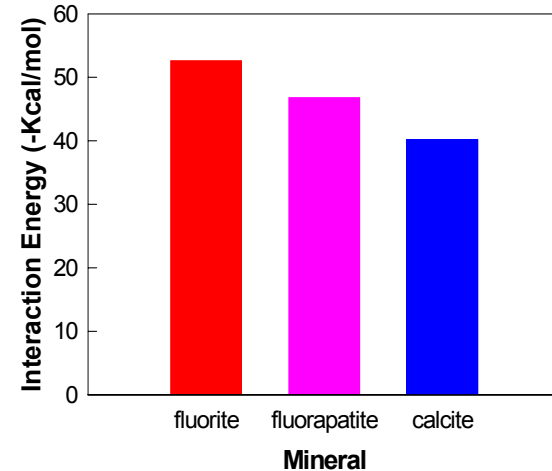
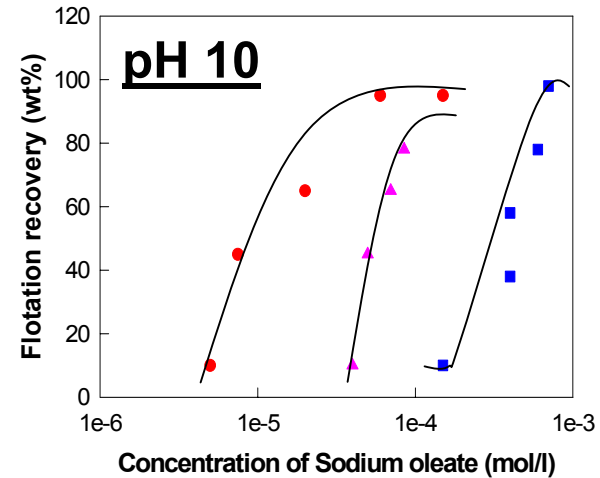
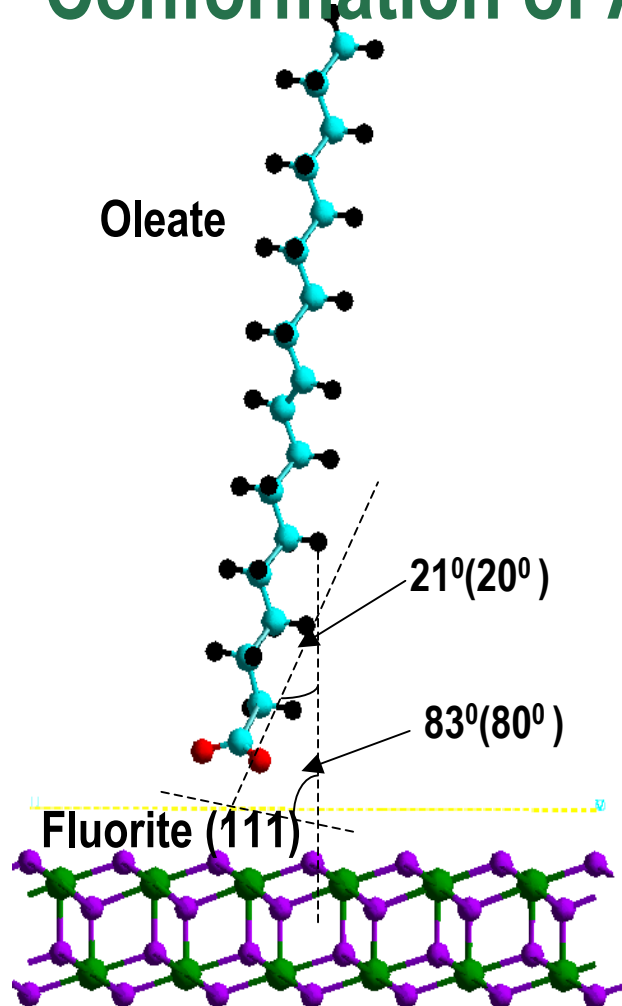
# Quantum Mechanical and Force Field Computations

- Neutral cluster models for the surface with desired Miller planes
- The geometry of surface-surfactant complex optimized
- Corresponding Interaction Energy

$$\Delta E = TE_{\text{complex}} - (TE_{\text{surface}} + TE_{\text{surfactant}})$$



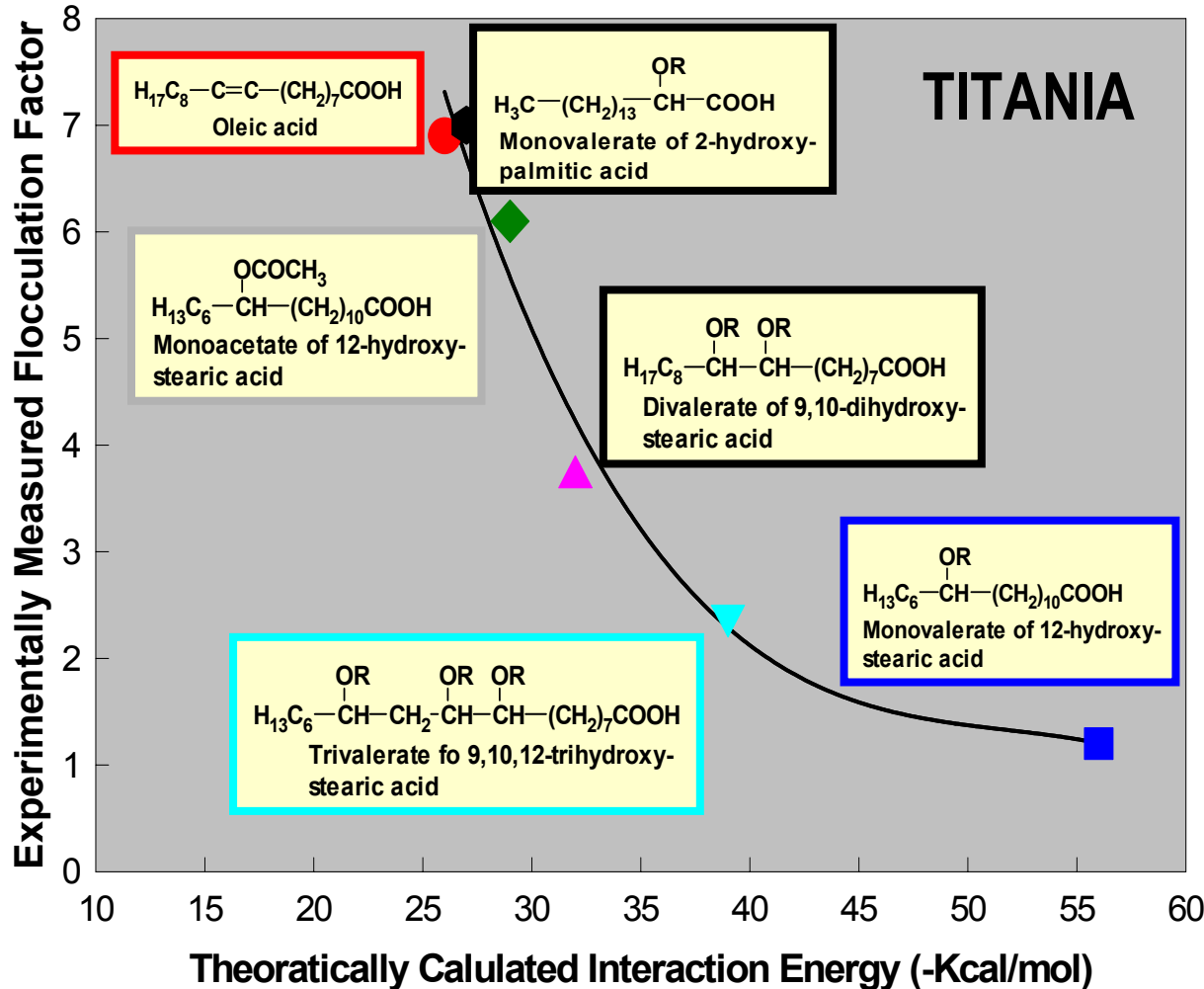
# Conformation of Adsorbed Molecules



(Values in bracket are the experimentally measured values (by in-situ infrared external reflection spectroscopy technique) taken from Mielczarski et. al., Langmuir, 14, 1739, 1998)

( Ref: Pradip and Beena Rai, Colloid and Surfaces A: 205(1-2), 139)

# Dispersion of Titania Powders

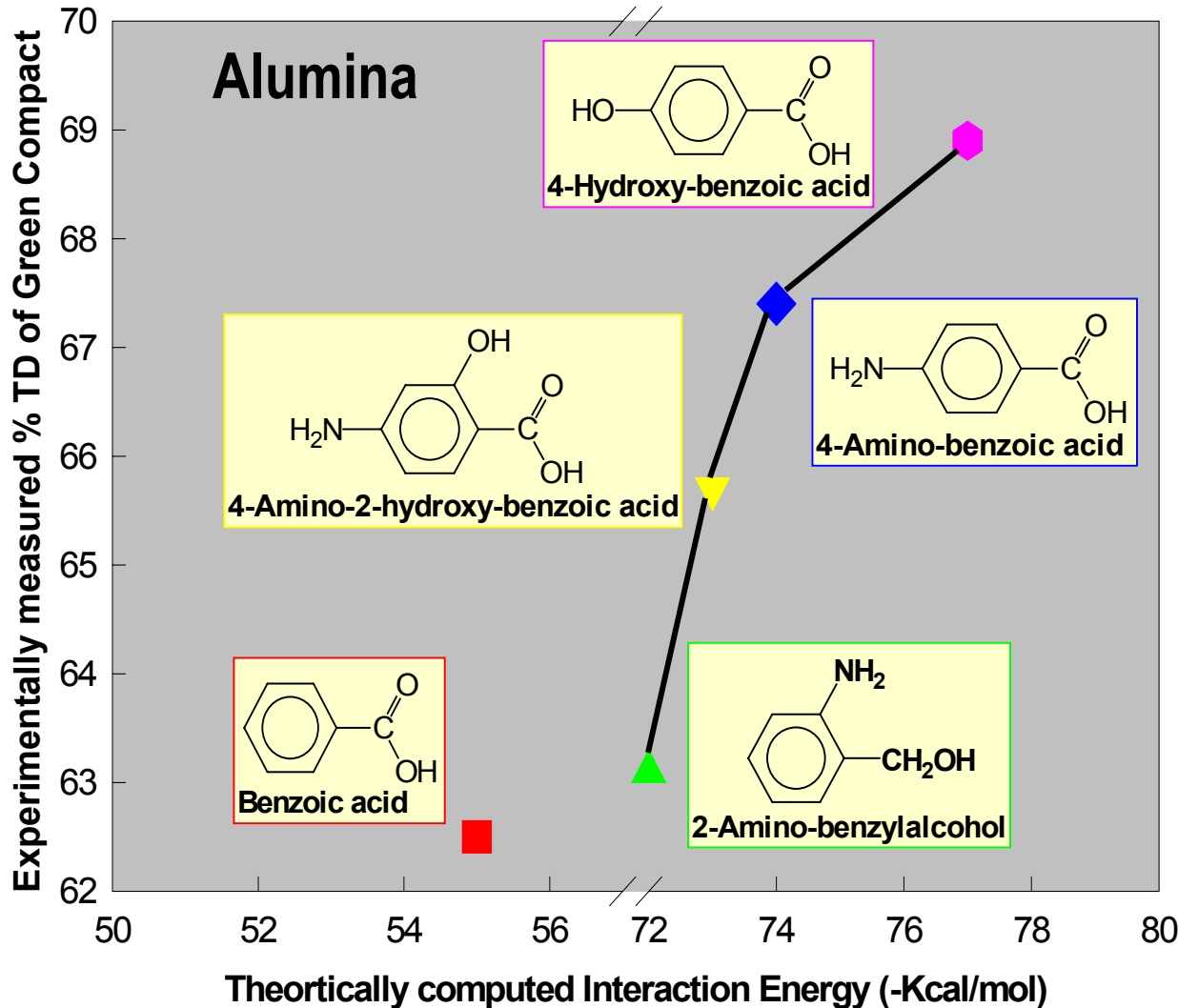


**Flocculation Factor is the slope of the plot of: log (viscosity) against the reciprocal square root of shear rate**

(Experimental data taken from Doroszkowski A. and Lambourne R., Faraday Discuss. Chem. Soc., 65, 252, 1978 )

( Ref: Pradip and Beena Rai, Colloid and Surfaces A: 205(1-2), 139)

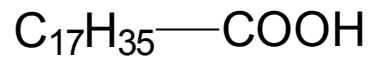
# Dispersion of Alumina Suspensions



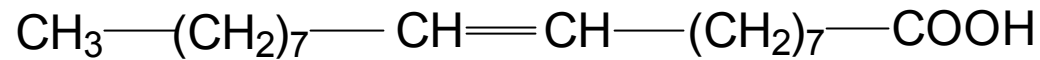
(Experimental data taken from:  
Sumita et. al., J. Am. Ceram.  
Soc., 74(9), 2189, 1991)

(Ref: Pradip and Beena Rai, Colloid and Surfaces A: 205(1-2), 139)

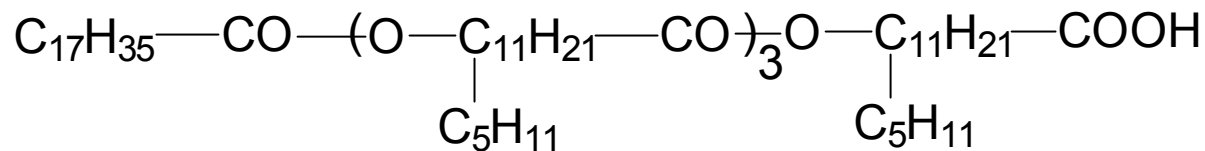
# Dispersants for Zirconia



STEARIC ACID

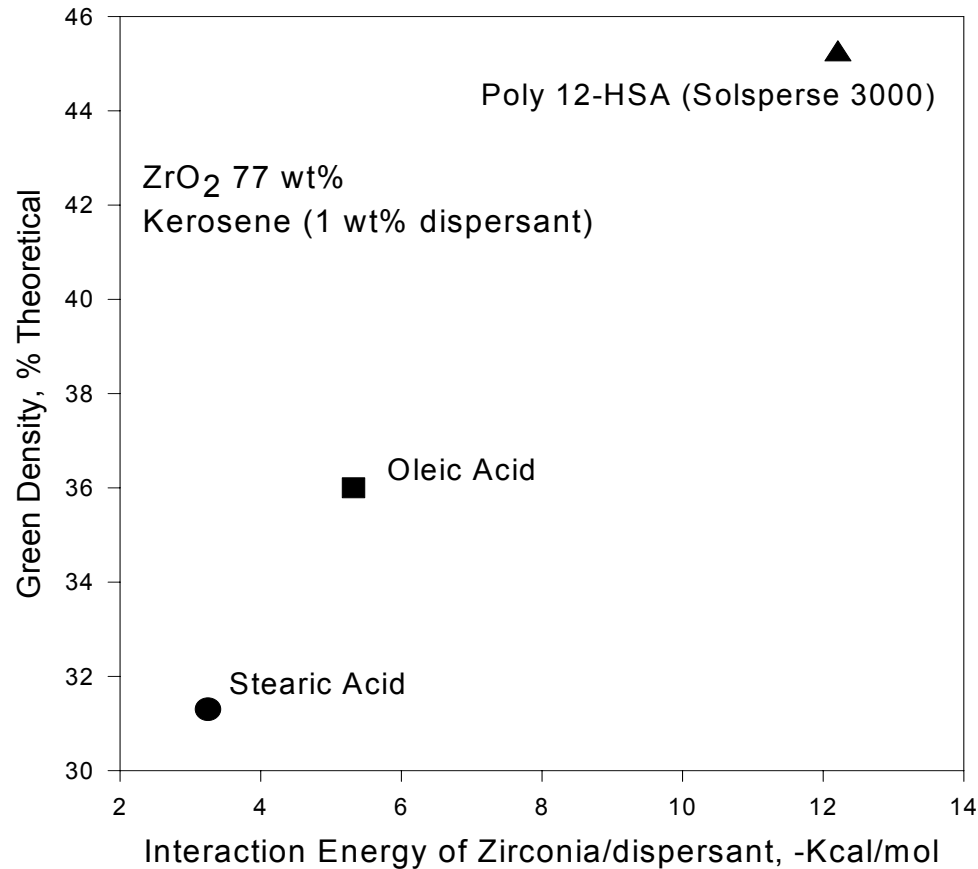


OLEIC ACID

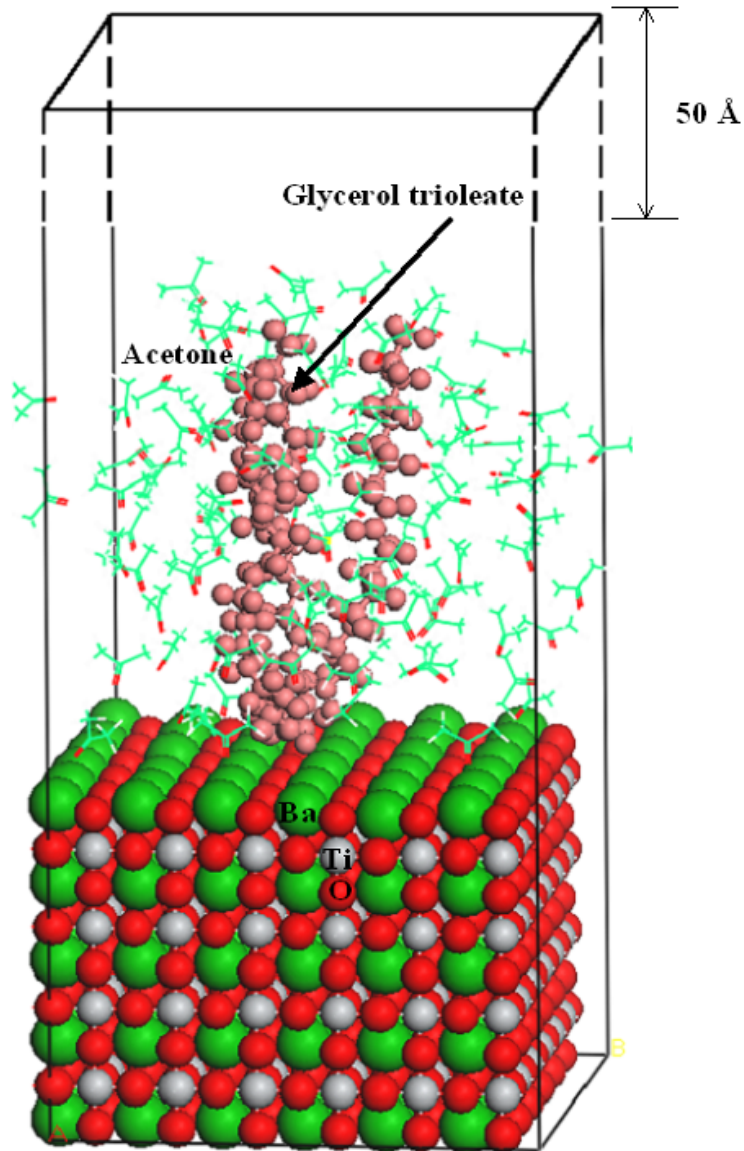


SOLSPERSE 3000

# Zirconia-Dispersant Interaction Energies: Correlation with Experimental Results



Ref: [Moloney et al, J. Amer. Ceram. Soc. 78 (12) (1995) 3225]



**BaTiO<sub>3</sub>(001) /Glycerol trioleate /Acetone**

**Substrate - Dispersant Complex**

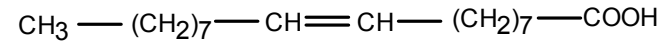
**MD Simulation  
300 °K and 300 ps**

Pradip et al., *Ferroelectrics*, 306, 2004, 195-208

# Dispersants

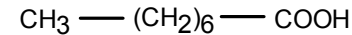
**Oleic Acid**

**OLA**

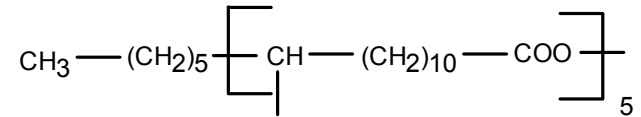


**Octanoic Acid**

**OCA**

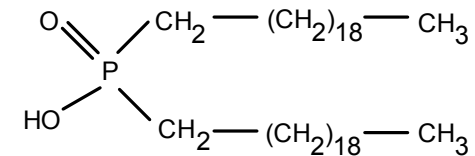


**Polyhydroxy Stearic Acid PHS**



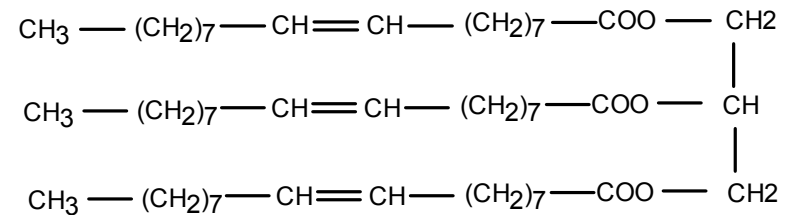
**Emphos PS-21A**

**EPS**



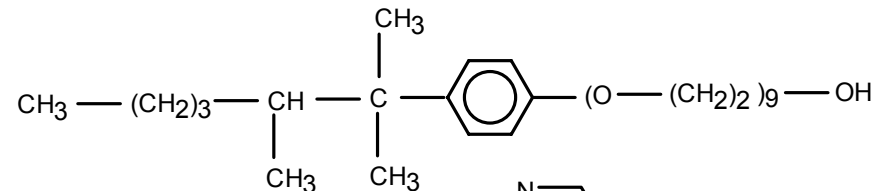
**Menhaden Fish Oil**

**MFO**



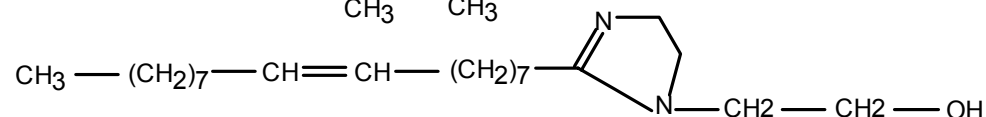
**Zonyl-A**

**ZNL**

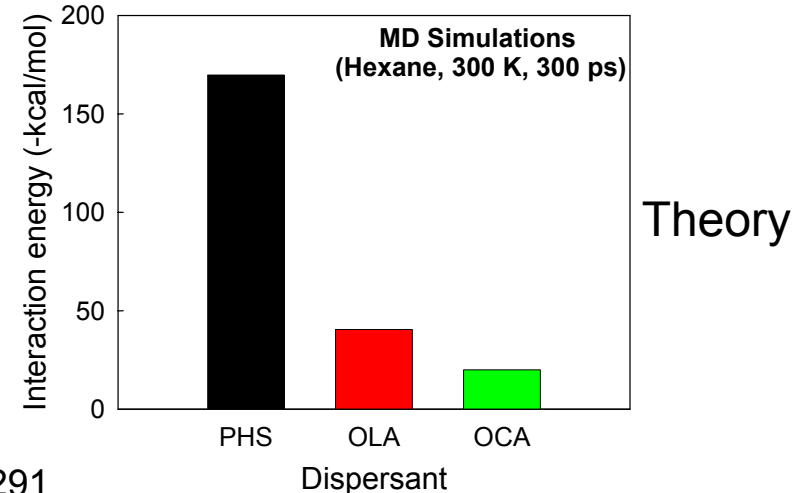
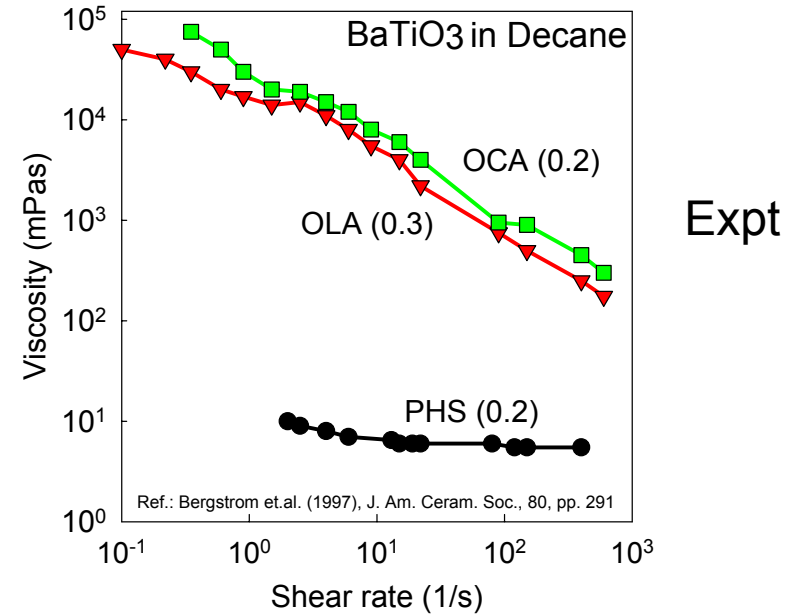
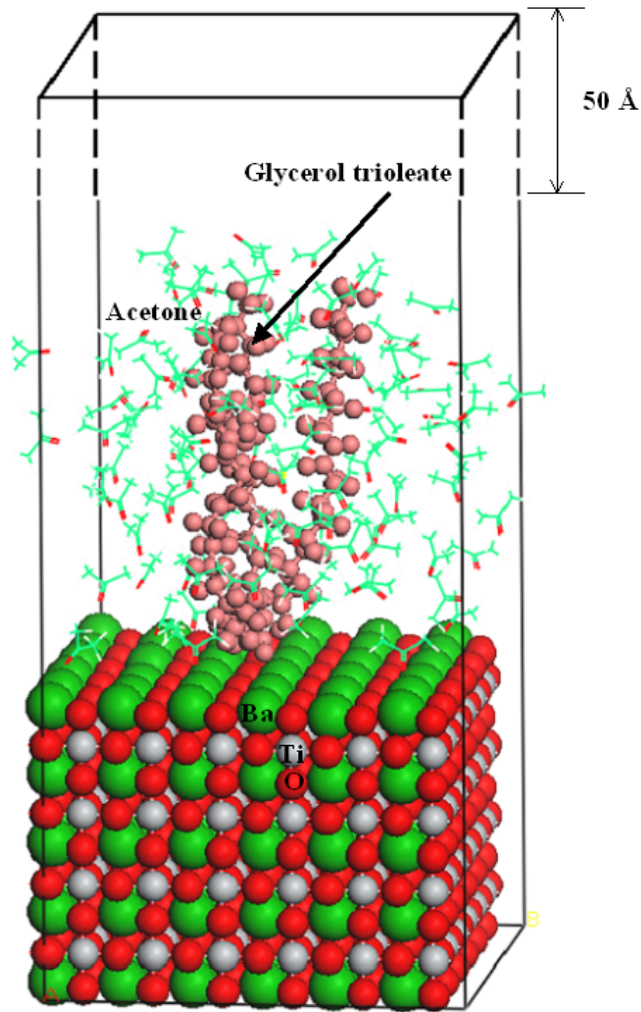


**Alkazine - O**

**AIME**



# Molecular Dynamics Simulation



Data from: Bergstrom et.al. (1997) J. Am. Ceram. Soc., 80, pp. 291

# Population Balance Modeling of Sintering

## Prediction of Microstructure Evolution during Sintering

- Extensive research /published literature on idealized systems available on the mechanisms of sintering but difficult to translate into commercial solutions
- Need exists for a quantitative approach to optimize sintering cycles, for example
- What kind of green body microstructure is desirable for desired properties in the final product?

- Is it possible to embed our fundamental mechanistic understanding in a mathematical representation (model) of commercial sintering process (size distribution) so as to be able to optimize practical systems
- Population balance paradigm offers such a possibility

# Sintering Stages

## ***Initial Stage***

Rapid interparticle neck growth by diffusion, vapor transport, plastic or viscous flow

## ***Intermediate Stage***

Pores reach equilibrium shape as dictated by interfacial free energy. A network of grain and pores defines the microstructure whose evolution is driven by trajectories of pore and grain size distributions. This stage normally covers the major part of sintering process

## ***Final Stage***

Pores may get pinched off and exist in isolation at grain corners or within the grains. Abnormal grain growth can occur

# Population Balance Paradigm

Accumulation Term

Changes due to convection in physical space

$$\underbrace{\frac{\partial H}{\partial t}} + \underbrace{\frac{\partial}{\partial x} (v_x H) + \frac{\partial}{\partial y} (v_y H) + \frac{\partial}{\partial z} (v_z H) + \sum_{j=1}^J \frac{\partial}{\partial w_j} v_j H}_{\text{Continuous changes in property space}} + \underbrace{\overline{D} - \overline{B}}_{\text{Jump changes due to discrete events}} = 0$$

Continuous changes in property space

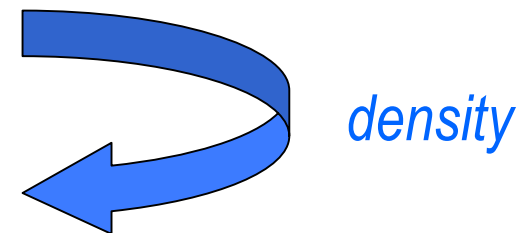
Jump changes due to discrete events

# An Operational Approach to Intermediate Stage of Solid State Sintering

In coupled population balance equations for evolution of pore and grain size spectra, incorporate semi-empirical velocity or convective terms for:

Pore Shrinkage

Grain Shrinkage and Growth



# Pore Shrinkage and Evolution of Pore Size Spectra I

- Continuity equation

$$\frac{\partial n(r,t)}{\partial t} + \frac{\partial}{\partial r} \left[ n(r,t) \frac{dr}{dt} \right] = 0$$

- Shrinkage “velocity”

$$\frac{dr}{dt} = -\frac{k}{r^m}$$

$$k = \exp\left(k_0 - \frac{Q}{RT}\right)$$

- ✓  $n(r,t)$  is number of pores of radius  $r$  at sintering time  $t$ .
- ✓  $m$  is a floating exponent that need not represent any one particular surface or bulk diffusion mechanism of shrinkage.
- ✓  $k$  is a specific rate constant that follows an Arrhenius type relationship.
- ✓ Pore coalescence can be incorporated in the continuity equation.

# Pore Shrinkage and Evolution of Pore Size Spectra II

- Solution

$$n(r, t) = \frac{n_0 \left( [ r^{m+1} + (m+1)kt ]^{1/(m+1)} \right)}{\left( 1 + (m+1)ktr \right)^{m/(m+1)}}$$

- Total pore volume

$$V(t) = C \int_0^{\infty} n(r, t) r^3 dr$$

- Normalized cumulative pore volume distribution

$$F_V(r, t) = \frac{C}{V(0)} \int_r^{\infty} n(r', t) r'^3 dr'$$

# Grain Growth and Evolution of Grain Size Spectra I

- Continuity equation

$$\frac{\partial H(r,t)}{\partial t} + \frac{\partial}{\partial r} \left( H(r,t) \frac{dr}{dt} \right) = 0$$

- Growth “velocity”

$$\frac{dr}{dt} = \frac{C_G}{[1 - \rho(t)]^\alpha r^n} \left( \frac{1}{r_c} - \frac{1}{r} \right)$$

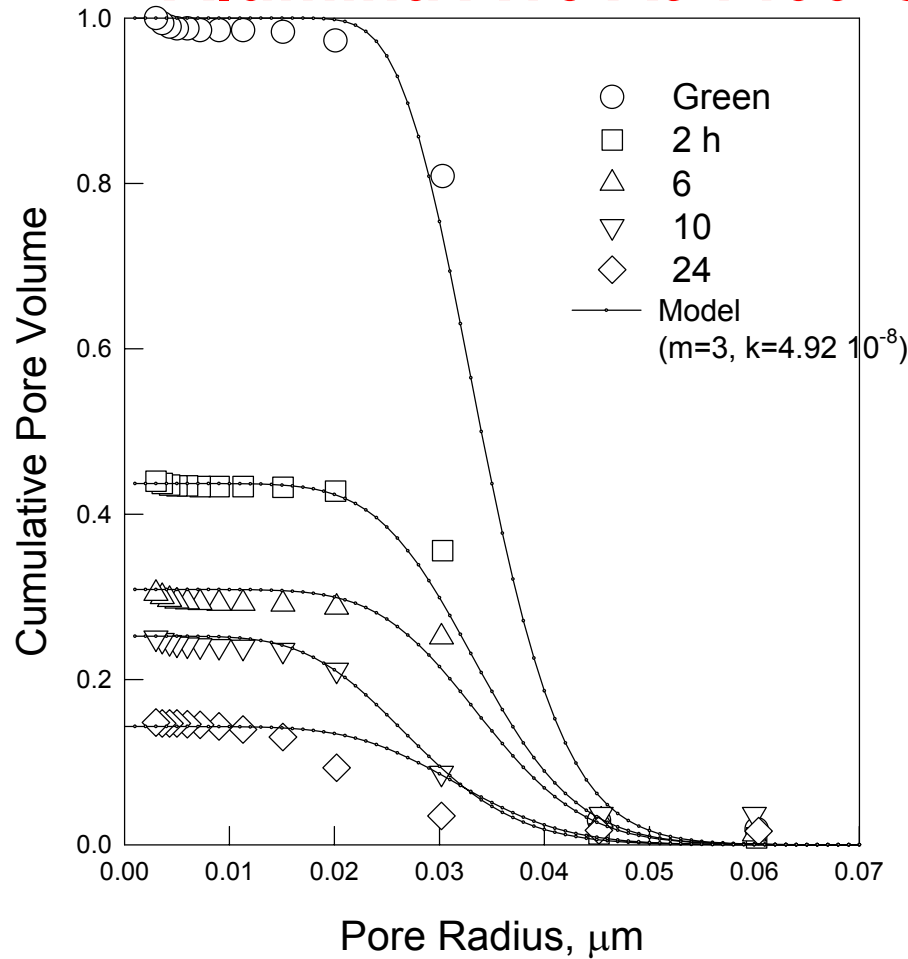
$$C_G = \exp \left( C_{G0} - \frac{Q_G}{RT} \right)$$

- ✓  $H(r,t)$  is number of grains of radius  $r$
- ✓  $r_c$  is critical radius
- ✓  $n$  is a floating exponent that depends on transport mechanism(s)
- ✓  $C_G$  is a specific rate constant that conforms with an Arrhenius type relationship
- ✓  $\alpha$  is a coupling parameter. Any alternate plausible coupling relationship can be employed

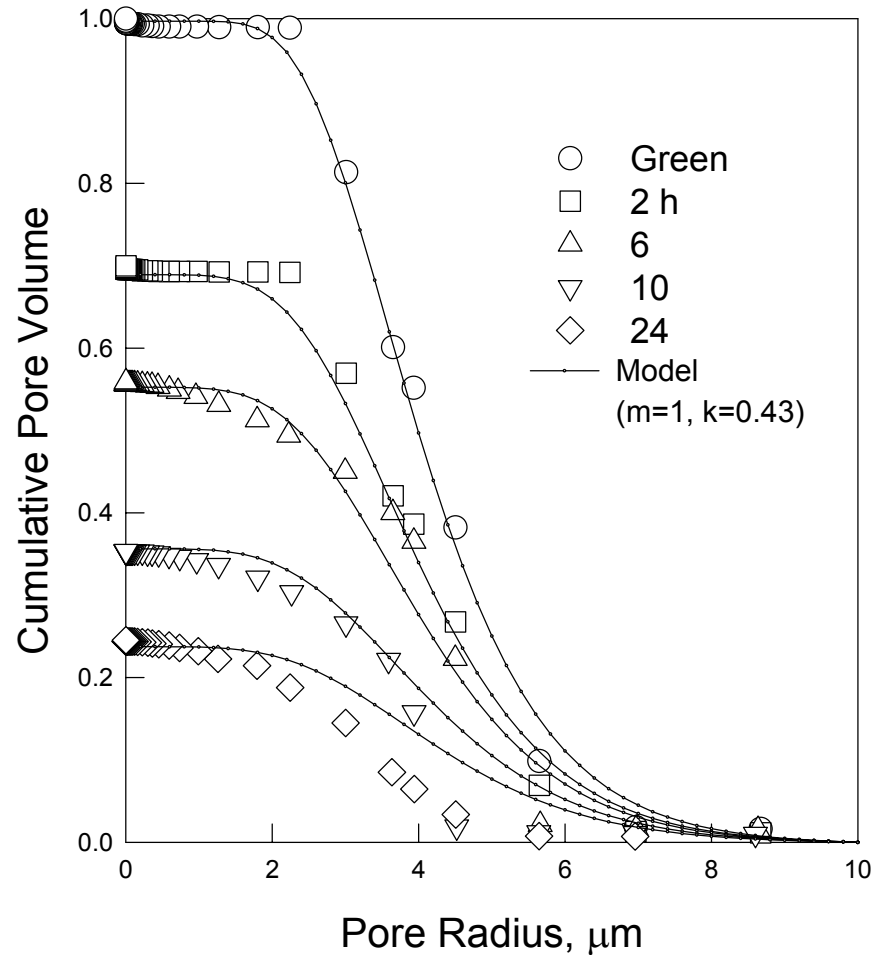
## Model Validation

- **Alumina, zirconia powders sintered at different temperatures for varying times**
- **Pore size distributions, porosity, grain size distribution as a function of time and temperature determined for parameter estimation**
- **Model is adequate to describe the pore shrinkage and grain growth (essence of sintering kinetics) and hence can be used to simulate sintering for different conditions.**

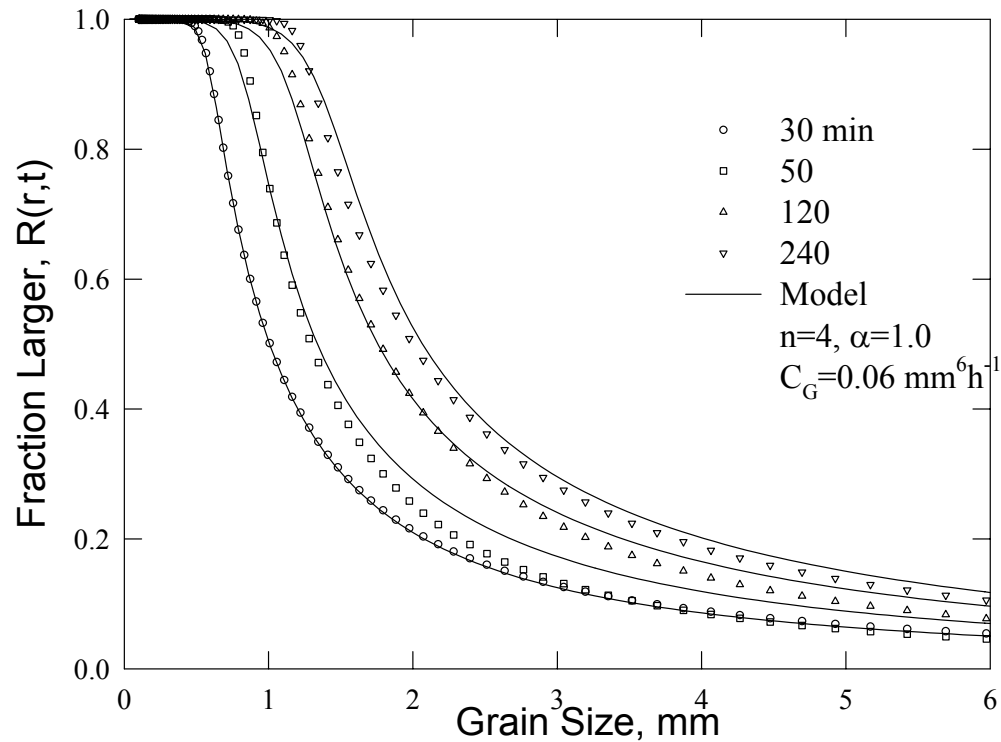
# Test of Pore Shrinkage Model I: Alumina A16 At 1400°C



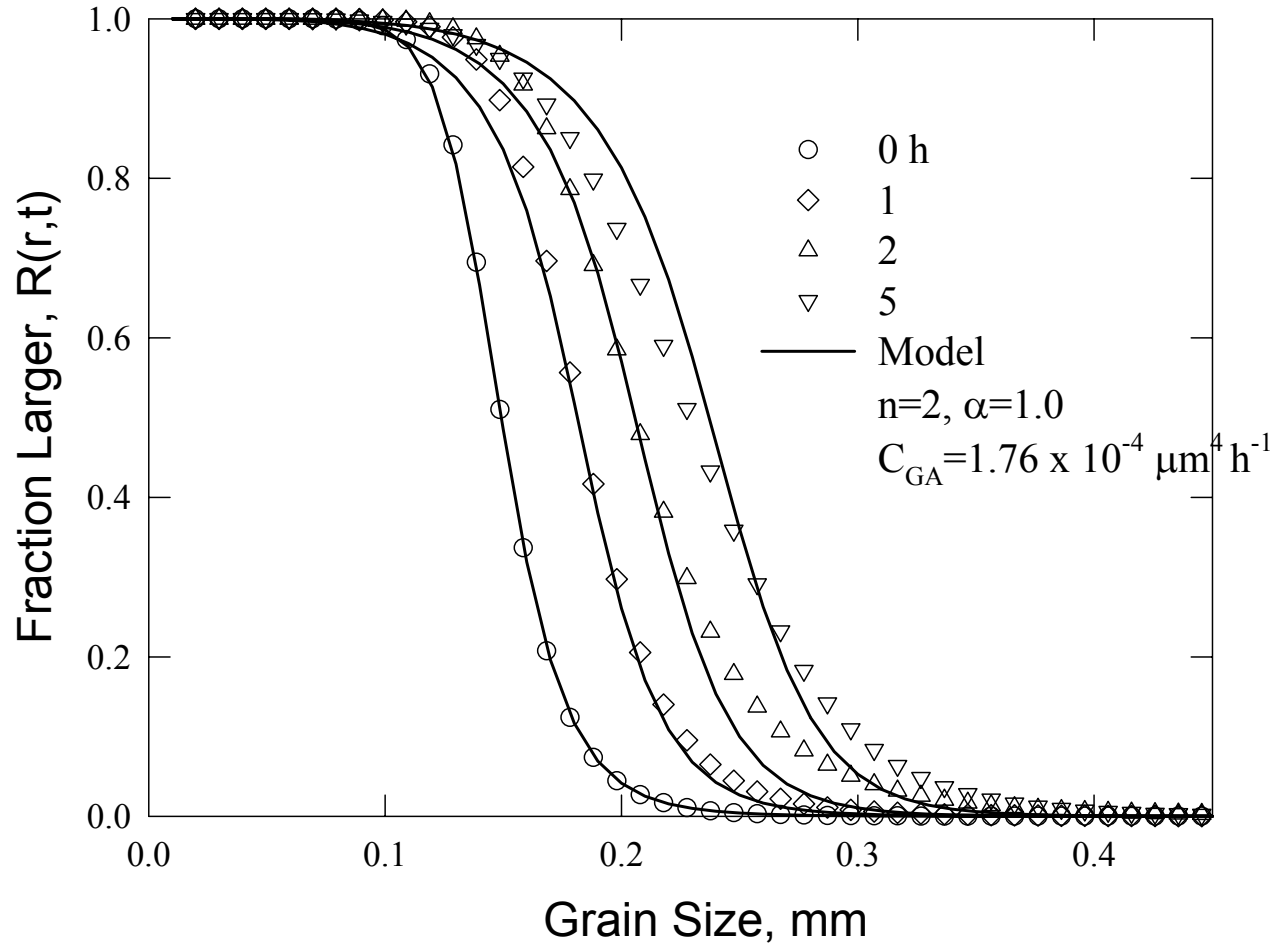
# Test of Pore Shrinkage Model II: Zirconia Syp 5.2 At 1400°C



# Test of Grain Growth Model I: Alumina Hpa10w, At 1500°C (Ting Data)

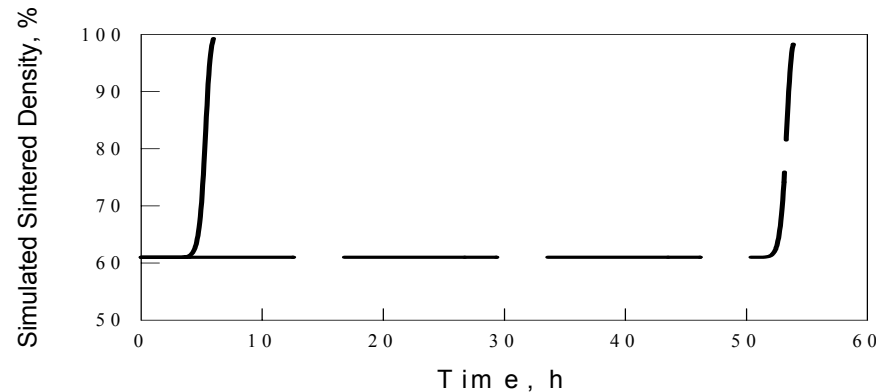
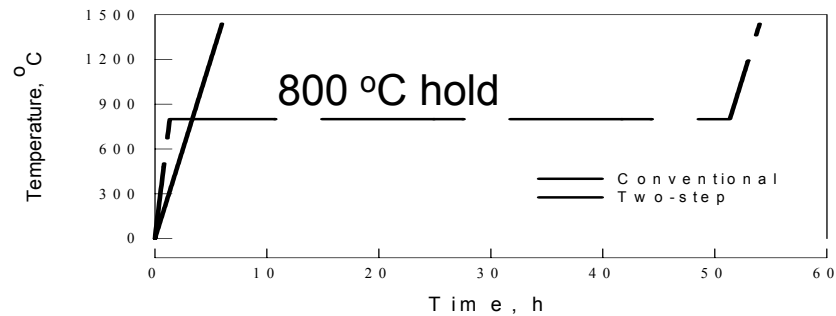


# Test of Grain Growth Model II: Zirconia Syp 5.2, At 1500°C



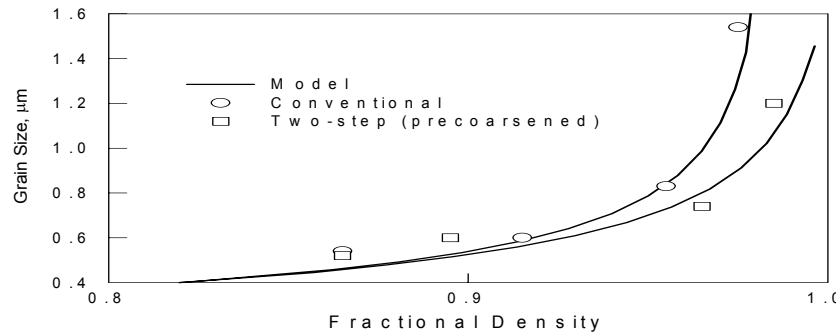
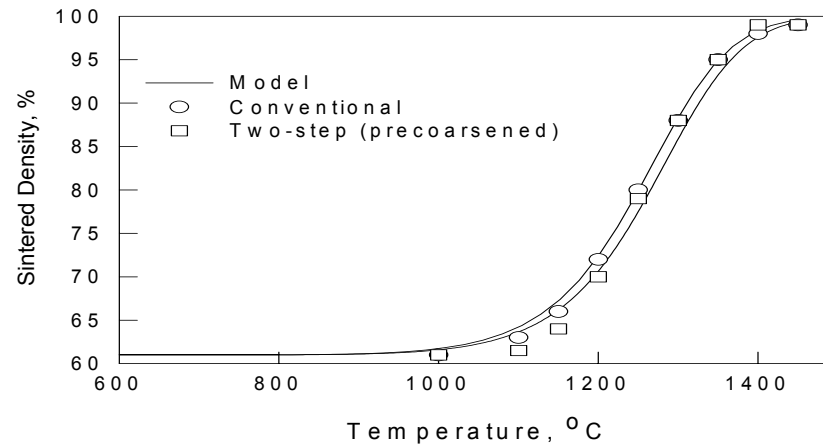
# Application: Sintering By Precoarsening Hold

## I. Alumina At 1450°C (Lin Data)



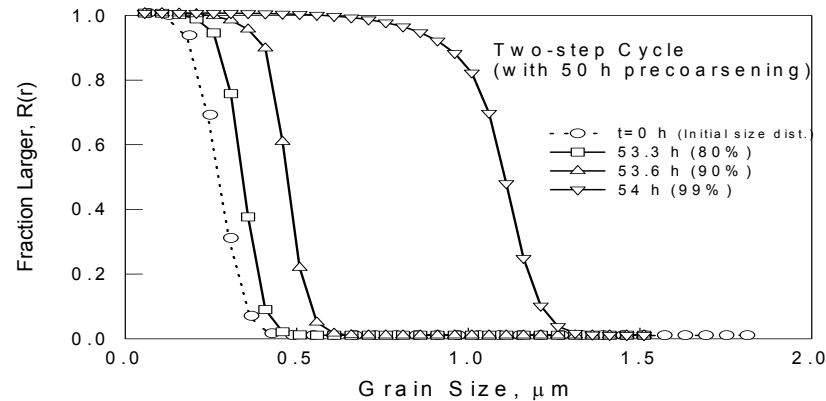
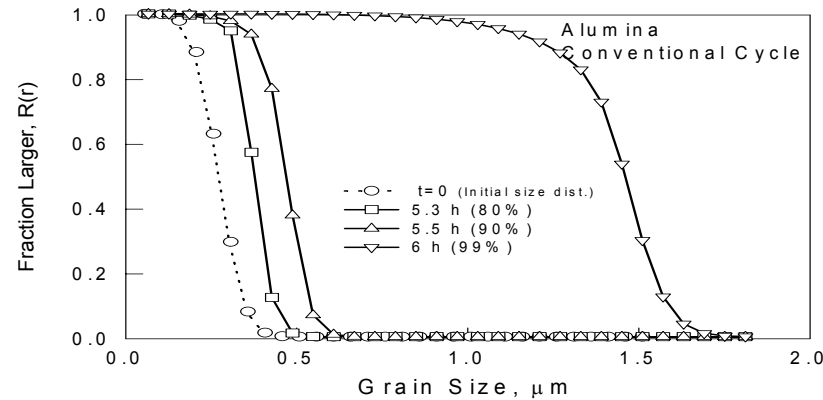
# Sintering by Precoarsening Hold

## II. Simulated and Measured Density & Grain Size

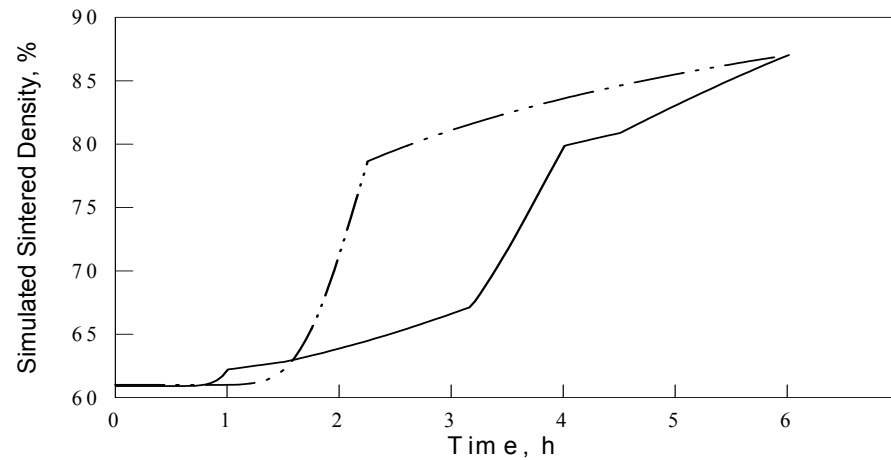
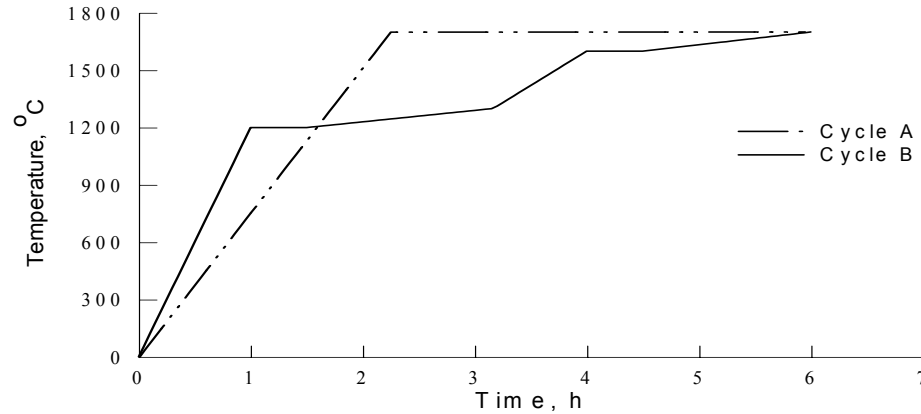


# Sintering by Precoarsening Hold

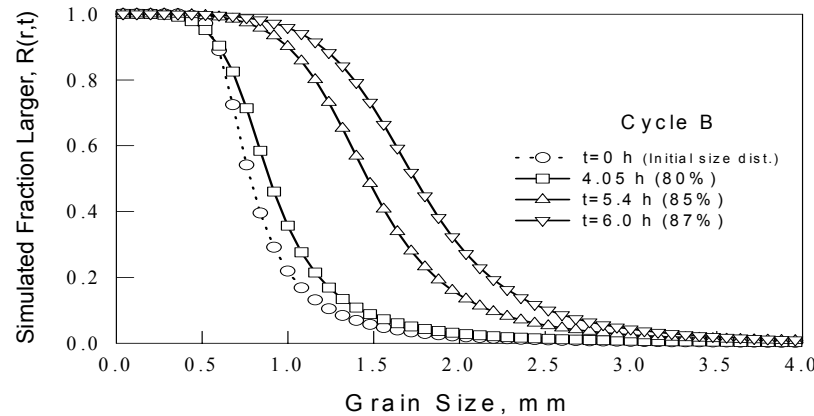
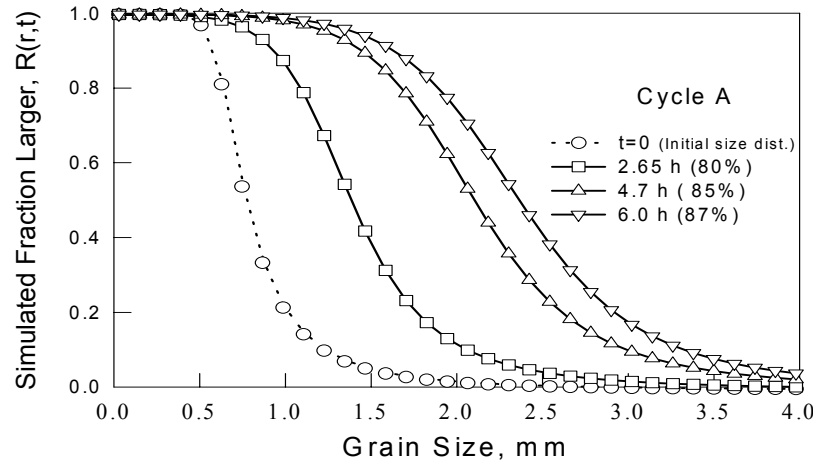
## III. Simulated Alumina Grain Size Distributions



# Simulation of Heating Cycles I



# Simulation of Heating Cycles II



# Key Publications

- **M. Subbanna, P.C. Kapur and Pradip, Role of Powder Size, Packing, Solid Loading and Dispersion in Colloidal Processing of Ceramics, Ceramics International, 28(4), (2002) pp 401-405**
- **Pradip and Beena Rai, Design of Tailor-made Surfactants for Industrial Applications using a Molecular Modeling Approach, Colloids and Surfaces, 205(1-2), (2002) pp 139-148**
- **Manjunath Subbanna, P.C. Kapur and Pradip, Computer-Aided Control of the Evolution of Microstructure during Sintering, Materials Chemistry and Physics, 67(1-3), (2001) pp 17 – 24**
- **Subbanna, M., Kapur, P.C., Pradip and Malghan, S.G, Population Balance Model for Solid State Sintering. Part I. Pore Shrinkage and Densification, Ceramics International, 27 (1), (2001) pp 57 - 62.**

- **Sivakumar, S., Subbanna, M., Sahay, S.S., Ramakrishnan, V., Kapur, P.C., Pradip and Malghan, S.G, Population Balance Model for Solid State Sintering. Part II. Grain Growth, Ceramics International, 27 (1), (2001) pp 63 - 71.**
- **M. Subbanna, Pradip and S.G. Malghan, Shear Yield Stress of Flocculated Alumina-Zirconia Mixed Suspensions : Effect of Solid Loading, Composition and Particle Size Distribution, Chem. Engineering. Sci, 53(17), (1998) pp 3073-79**
- **Manjunath Subbanna, Sandhya Kokil, P.C. Kapur, Pradip and S.G. Malghan, An Aggregation Index for Monitoring the State of the Suspensions, Langmuir, 14, (1998) pp 7364-70**
- **V. Ramakrishnan, Pradip and S.G. Malghan, The Stability of Alumina-Zirconia Suspensions, Colloids and Surfaces, 133, (1998), pp 135-142**

- **S. Sivakumar, Pradip, P.C. Kapur and S.G. Malghan, Size-interval by Size-interval Marching Algorithm for Simulation of Intermediate Stage of Sintering, *Colloids and Surfaces*, 133, (1998), pp 173-182**
- **V. Ramakrishnan, Pradip, S.G. Malghan, Yield Stress of Alumina Zirconia Suspensions, *J. American Ceramic Society* , 79(10), (1996), 2567-76**
- **Pradip, R. S. Premachandran and S. G. Malghan, Electrokinetic Behaviour and Dispersion Characteristics of Ceramic Powders with Cationic and Anionic Polyelectrolytes, *Bull. of Materials Science*, 17(6), (1994), pp 911-920**
- **Pradip, Design of Crystal-Structure Specific Surfactants Based on Molecular Recognition at Mineral Surfaces, *Current Science*, 63(4), (1992), pp 180-186.**

# Summary

- **Dispersion and rheology (shear yield stress) of mixed suspensions modeled incorporating inter-particle surface forces**
- **A molecular modeling based approach to rational design of dispersants for colloidal suspensions**
- **Shift of IEP of colloidal suspensions in presence of dispersants (e.g. poly electrolytes) and its effect on dispersion (Electro-steric dispersion)**
- **Population balance model for solid state sintering adequately describes the evolution of microstructure as a function of time-temperature cycles (densification and grain growth is explicitly reflected)- A powerful tool for quantitative and rigorous optimization and control in the industry**