

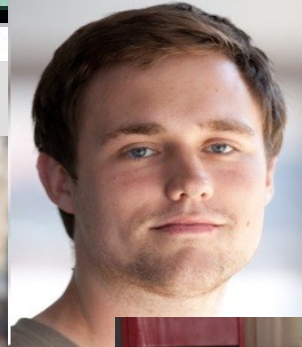
# *Parameterized modeling and model order reduction for large electrical systems*

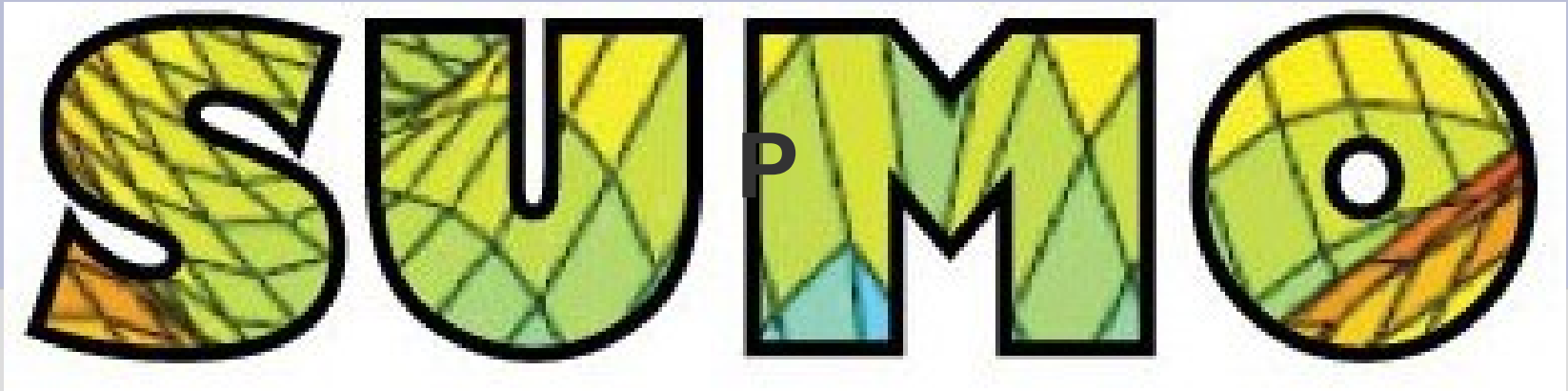
*Dr Elizabeth Rita Samuel*





# SUMMO





**Parametric modeling**  
**Parametric model order reduction**  
**Supervised machine learning**  
**Bioinformatics**  
**High performance computing**

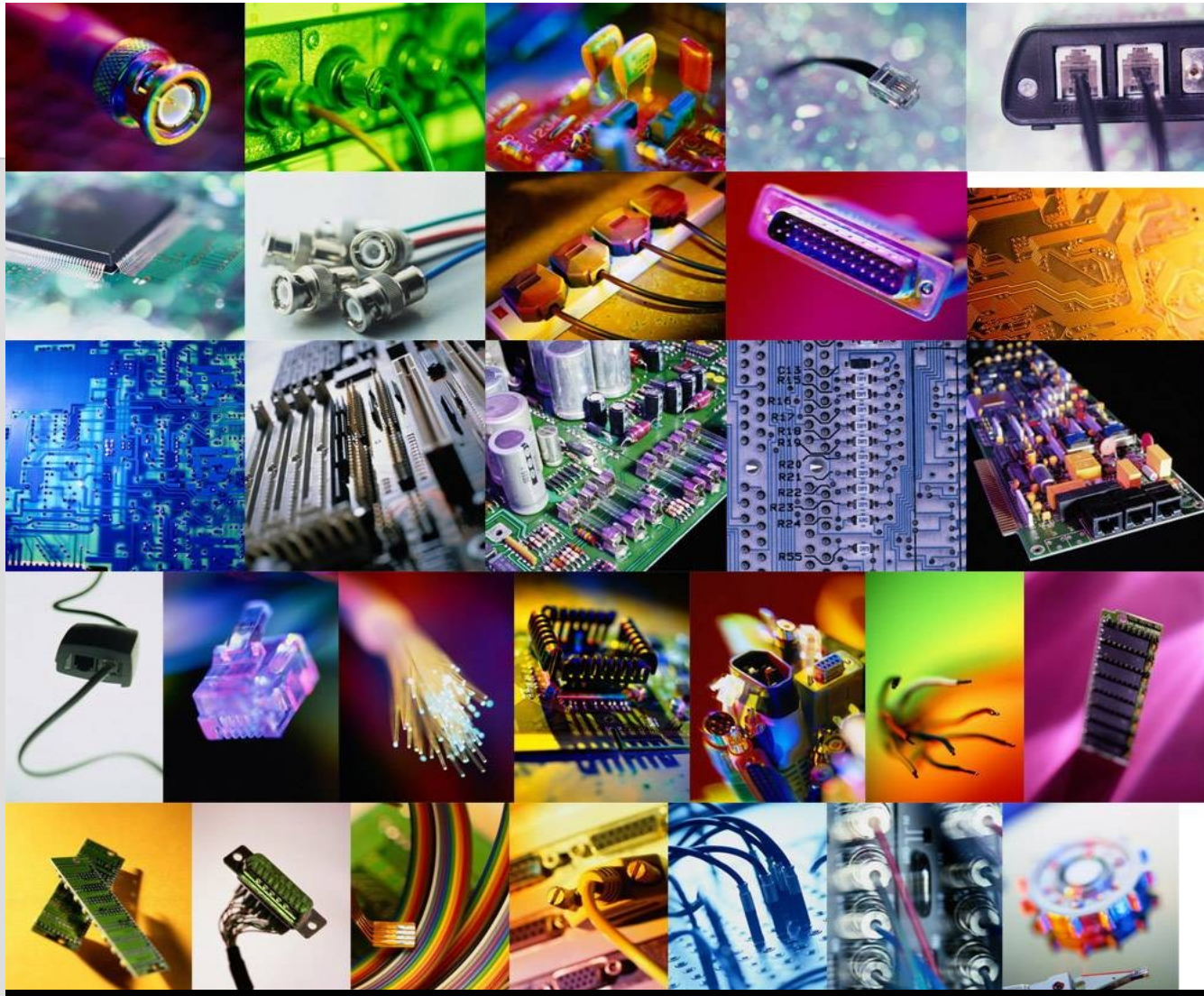
# *Parameterized modeling and model order reduction for large electrical systems*

*Dr Elizabeth Rita Samuel*







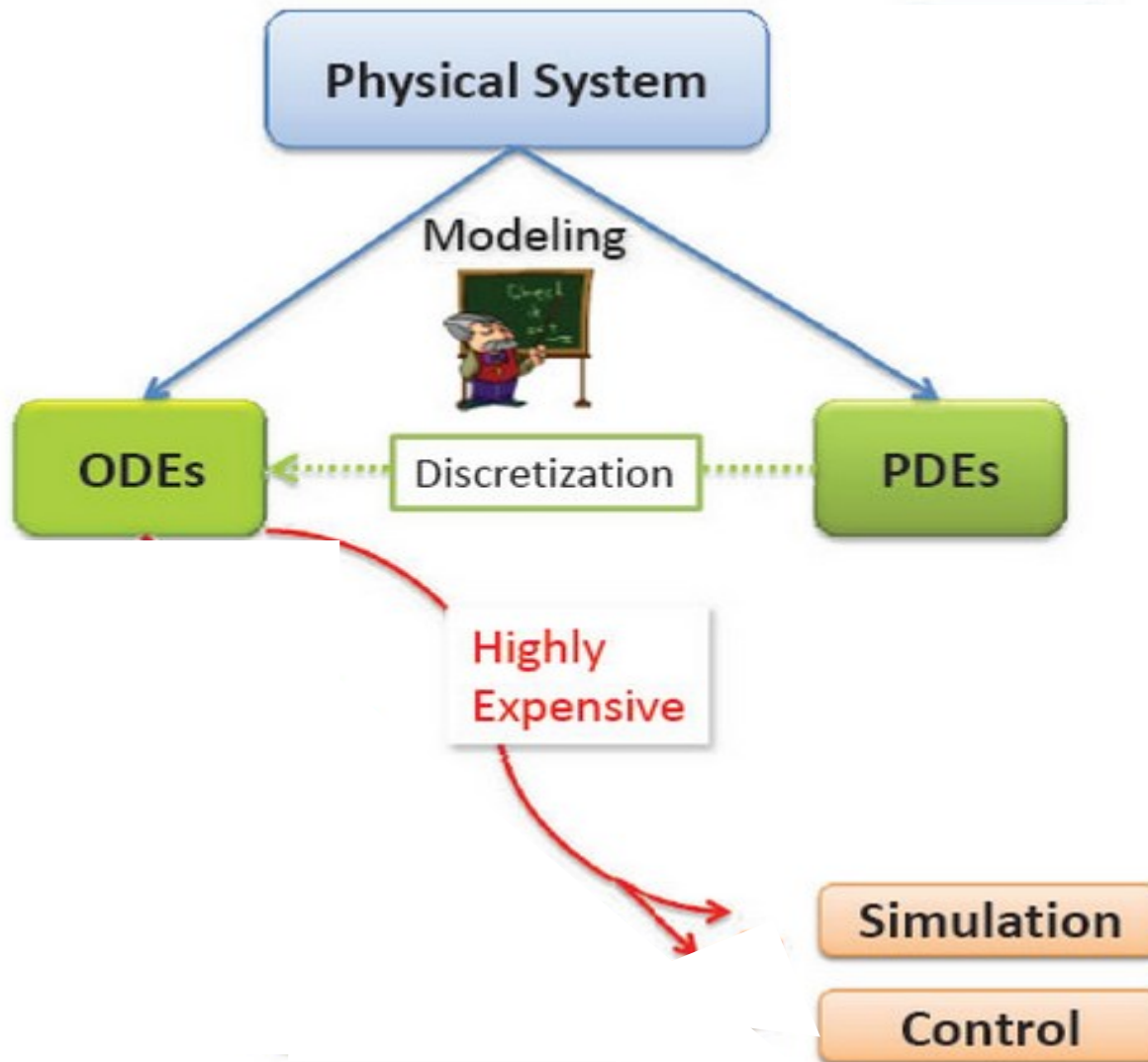




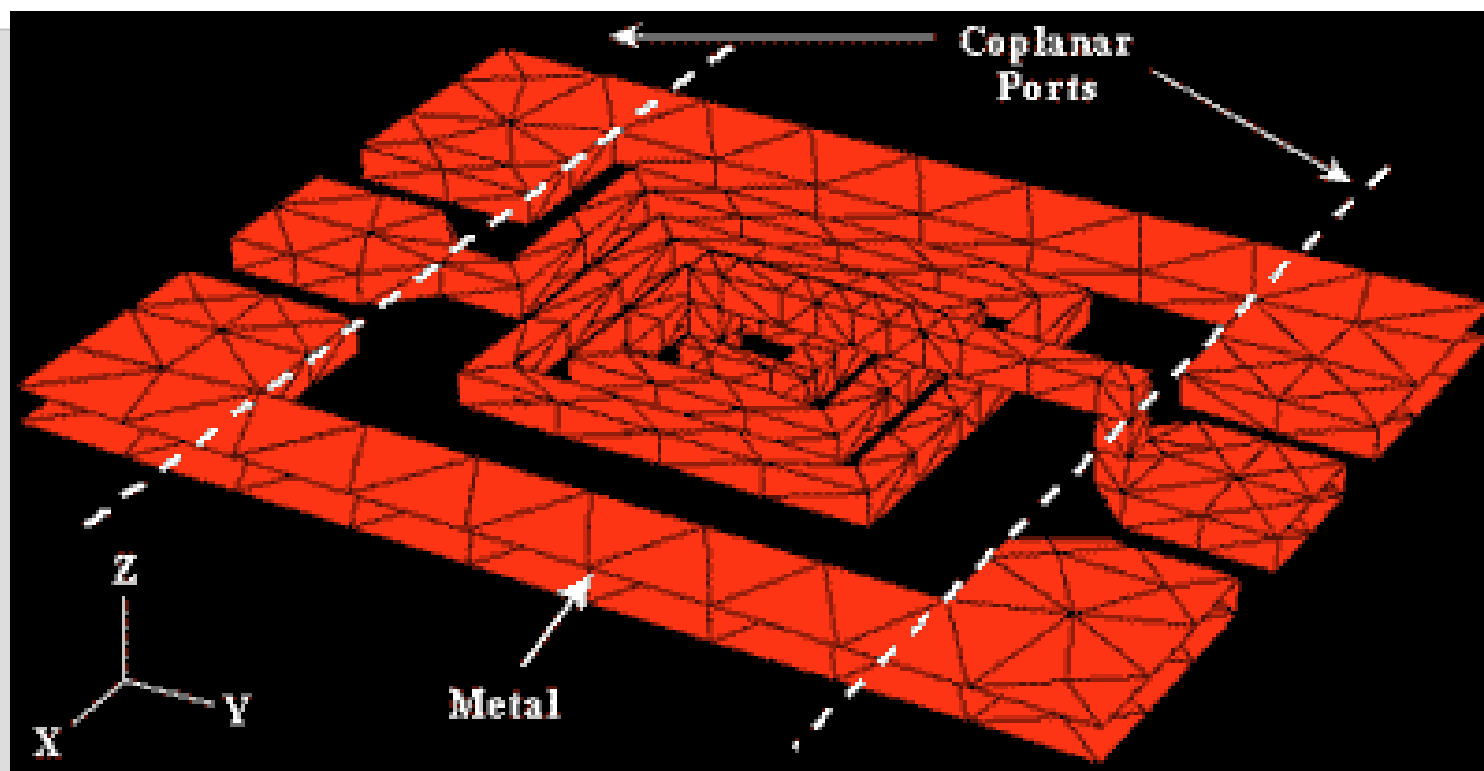
# OVERVIEW

- ★ **Model Order Reduction**
- ★ Multipoint expansion
- ★ Parameterized modeling

# MODEL ORDER REDUCTION

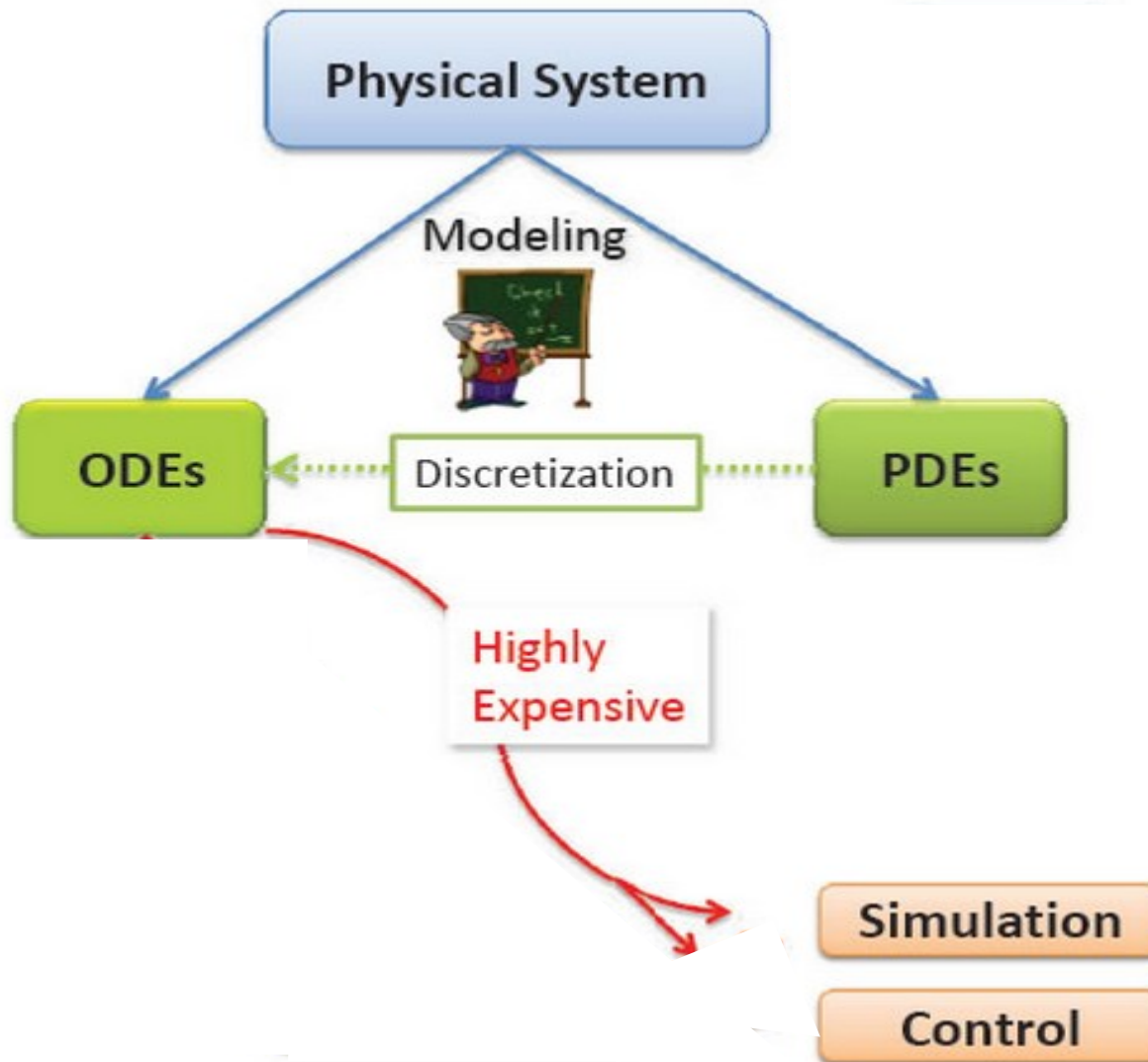


# DISCRETIZATION

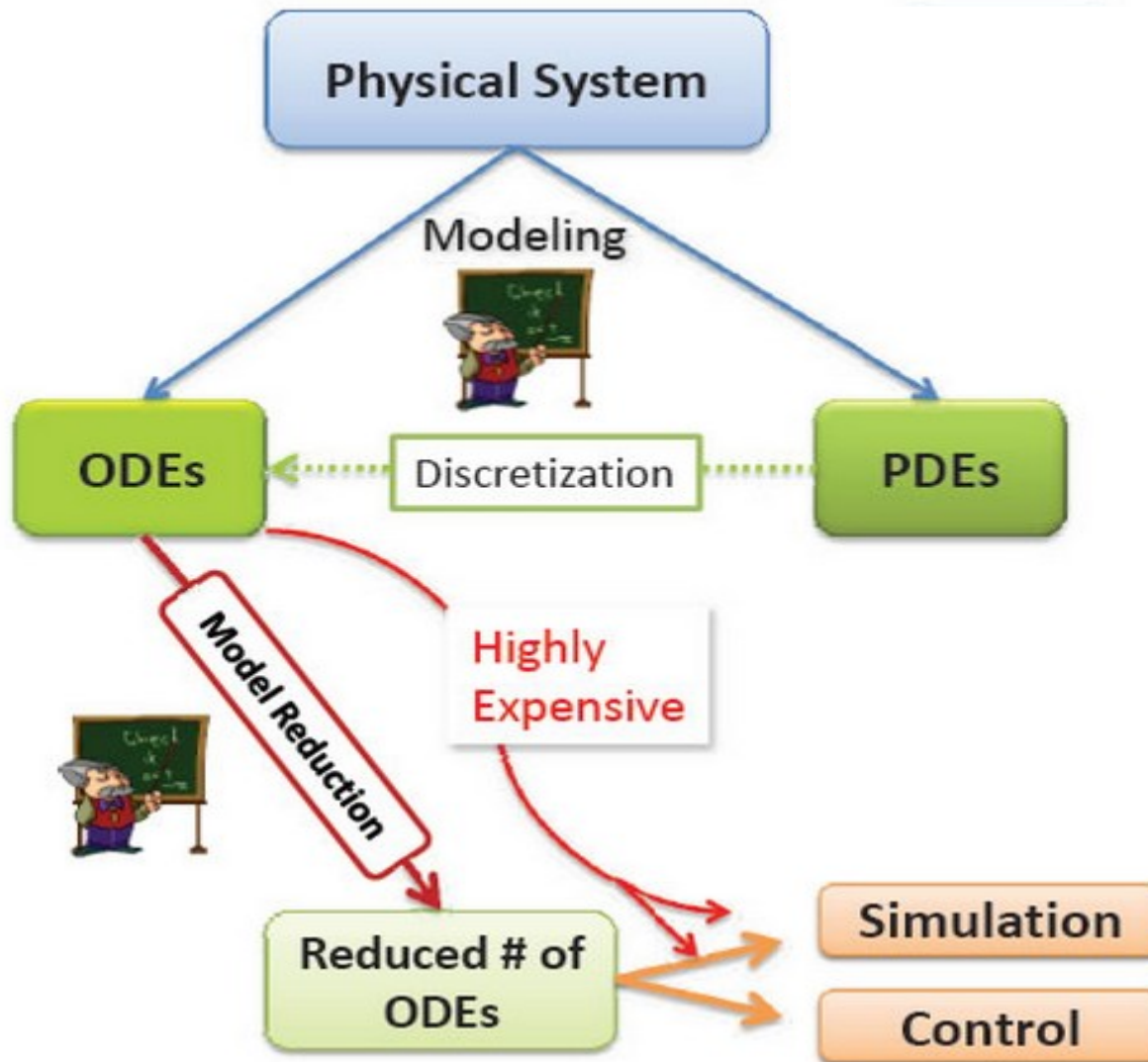




# MODEL ORDER REDUCTION



# MODEL ORDER REDUCTION



## *STATE SPACE*

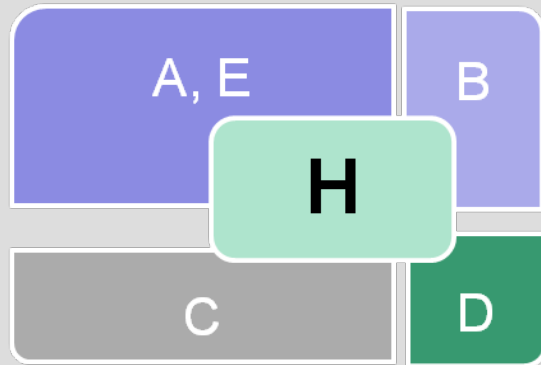
$$\dot{E}x = Ax + Bu$$



# MODEL ORDER REDUCTION

$$E \dot{x} = Ax + Bu$$

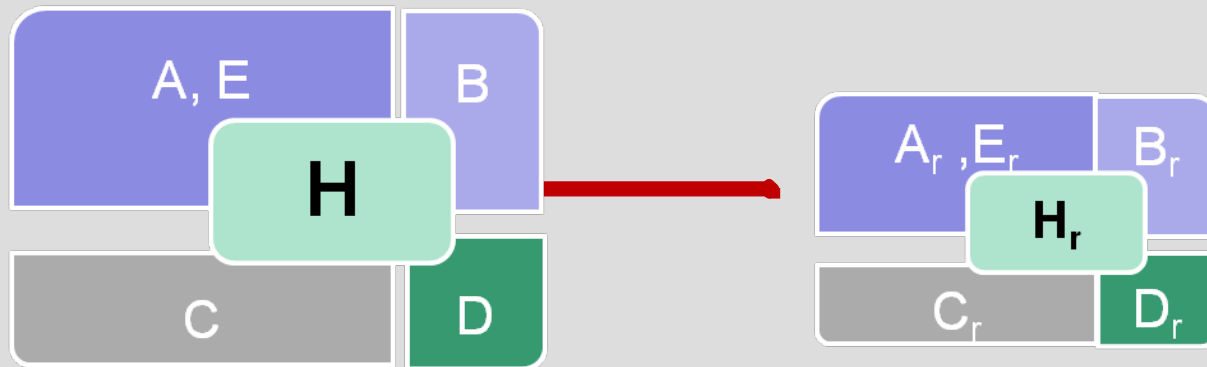
$$y = Cx$$



# MODEL ORDER REDUCTION

$$E \dot{x} = Ax + Bu$$

$$y = Cx$$



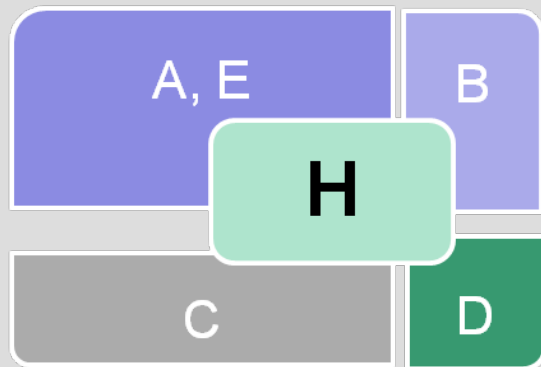
# MODEL ORDER REDUCTION



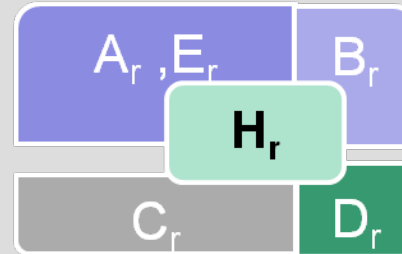
$$E \dot{x} = Ax + Bu$$

$$V^T E V \dot{z} = V^T A V z + V^T B u$$

$$y = Cx$$



$$y = CVz$$





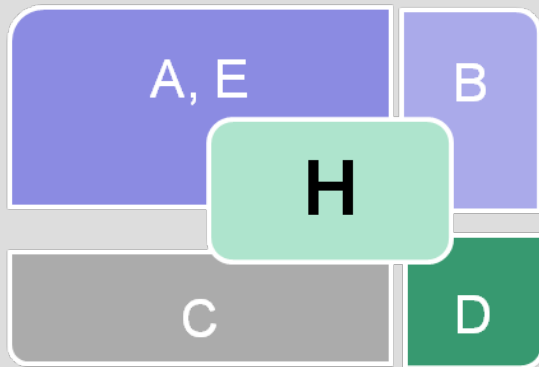
# MODEL ORDER REDUCTION

$$E \dot{x} = Ax + Bu$$

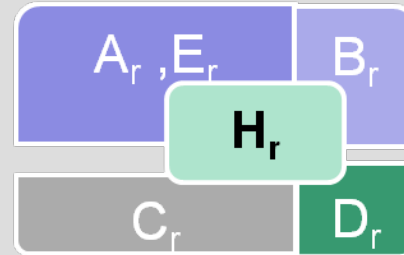
MOR

$$V^T E V \dot{z} = V^T A V z + V^T B u$$

$$y = Cx$$



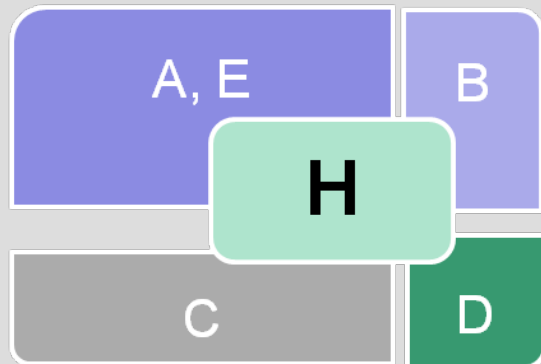
$$y = C V z$$



# MODEL ORDER REDUCTION

$$E \dot{x} = Ax + Bu$$

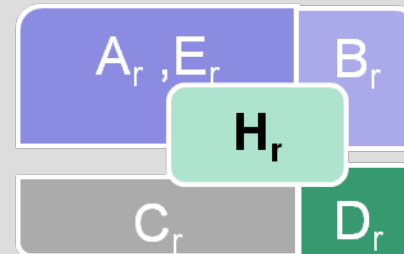
$$y = Cx$$



MOR

$$\cancel{V}^T E \cancel{V} \dot{z} = \cancel{V}^T A \cancel{V} z + \cancel{V}^T B u$$

$$y = C \cancel{V} z$$

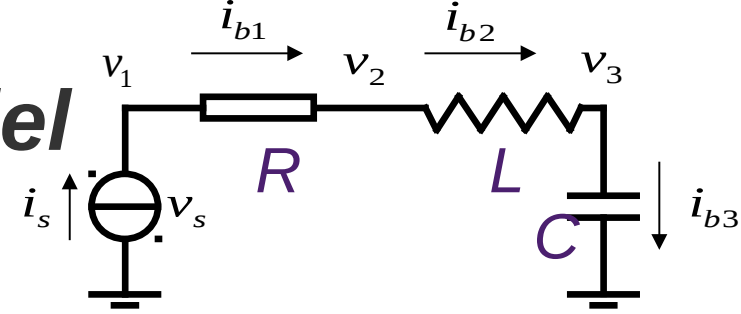


*Approximation error small*

*Preservation of system properties*

*Computationally stable and efficient.*

# RLC circuit model



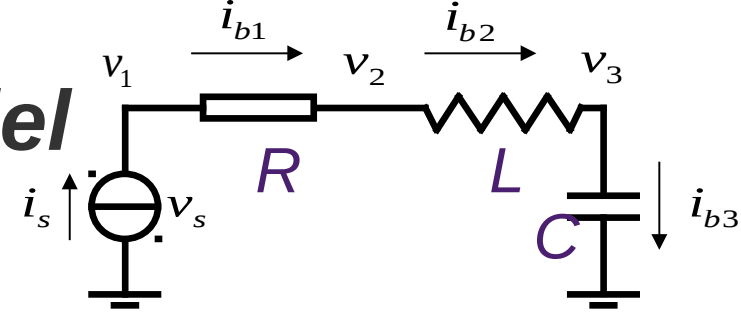
## State-space model (MNA)

$$\begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & C & 0 \\ 0 & 0 & 0 & L \end{bmatrix} \begin{pmatrix} \dot{V}_1 \\ \dot{V}_2 \\ \dot{V}_3 \\ \dot{i}_L \end{pmatrix} = \begin{bmatrix} 1/R & -1/R & 0 & 0 \\ -1/R & 1/R & 0 & 1 \\ 0 & 0 & 0 & -1 \\ 0 & -1 & 1 & 0 \end{bmatrix} \begin{pmatrix} V_1 \\ V_2 \\ V_3 \\ i_L \end{pmatrix} + \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \end{bmatrix} i_s$$

$$y = \begin{bmatrix} 1 & 0 & 0 & 0 \end{bmatrix} \begin{pmatrix} V_1 \\ V_2 \\ V_3 \\ i_L \end{pmatrix}$$



# RLC circuit model

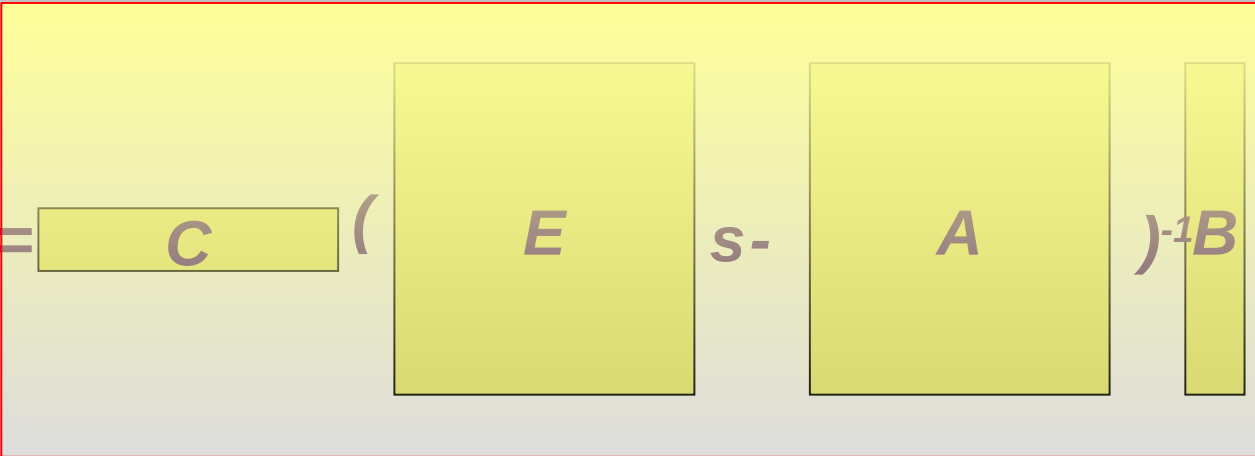


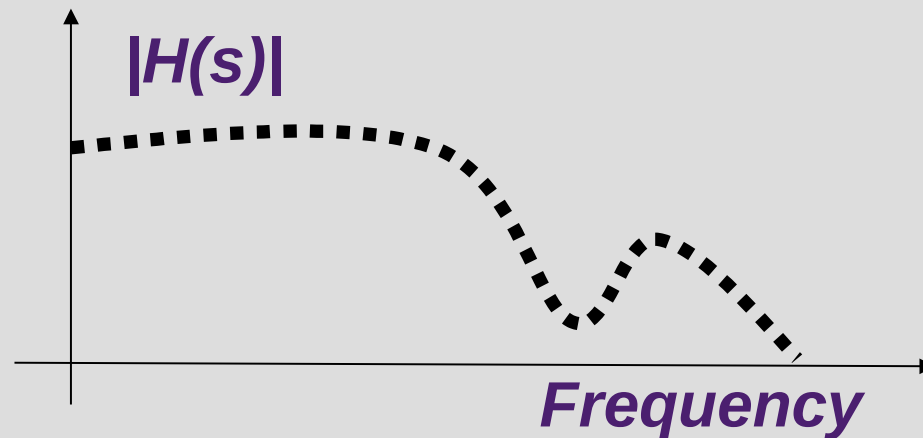
## State-space model (MNA)

$$\begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & EC & 0 \\ 0 & 0 & 0 & L \end{bmatrix} \begin{pmatrix} \dot{V}_1 \\ \dot{V}_2 \\ \dot{V}_3 \\ \dot{i}_L \end{pmatrix} = \begin{bmatrix} 1/R & -1/R & 0 & 0 \\ -1/R & 1/R & 0 & 0 \\ 0 & 0 & A & 0 \\ 0 & 0 & -1 & 1 \end{bmatrix} \begin{pmatrix} V_1 \\ V_2 \\ V_3 \\ i_L \end{pmatrix} + \begin{bmatrix} 0 \\ 1 \\ -1 \\ 0 \end{bmatrix} i_s$$

$$y = \begin{bmatrix} C \end{bmatrix} \begin{pmatrix} V_1 \\ V_2 \\ V_3 \\ i_L \end{pmatrix}$$

# TRANSFER FUNCTION

$$Y(s) = C (E s - A)^{-1} B U(s)$$




# MOMENT MATCHING

*Taylor expansion:*

$$H(s) = \boxed{C} \left( \boxed{M_0} + \boxed{M_1} s + \boxed{M_2} s^2 \dots \right)$$

# Moment-matching

*Taylor expansion:*

$$H(s) = \boxed{C} \left( \boxed{M_0} + \boxed{M_1} s + \boxed{M_2} s^2 \dots \right)$$

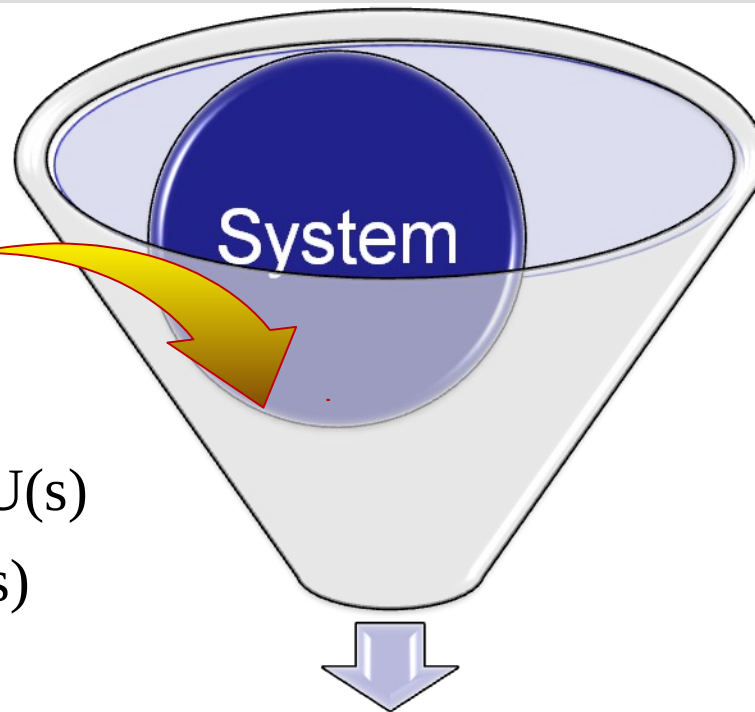
$$V = \begin{array}{|c|c|c|} \hline M_0 & M_1 & M_2 \\ \hline \end{array}$$



# OVERVIEW

- ★ Model Order Reduction
- ★ **Multipoint expansion**
- ★ Parameterized modeling

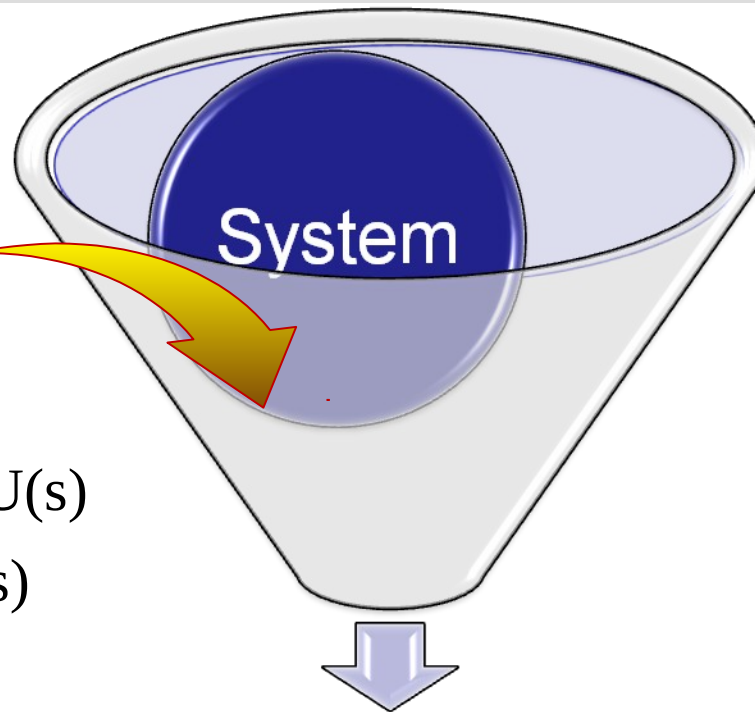
# *EXPANSION POINT*



$$sEX(s) = AX(s) + BU(s)$$

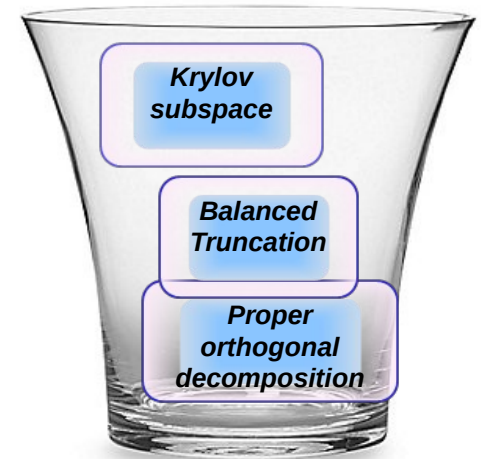
$$Y(s) = CX(s) + DU(s)$$

# EXPANSION POINT



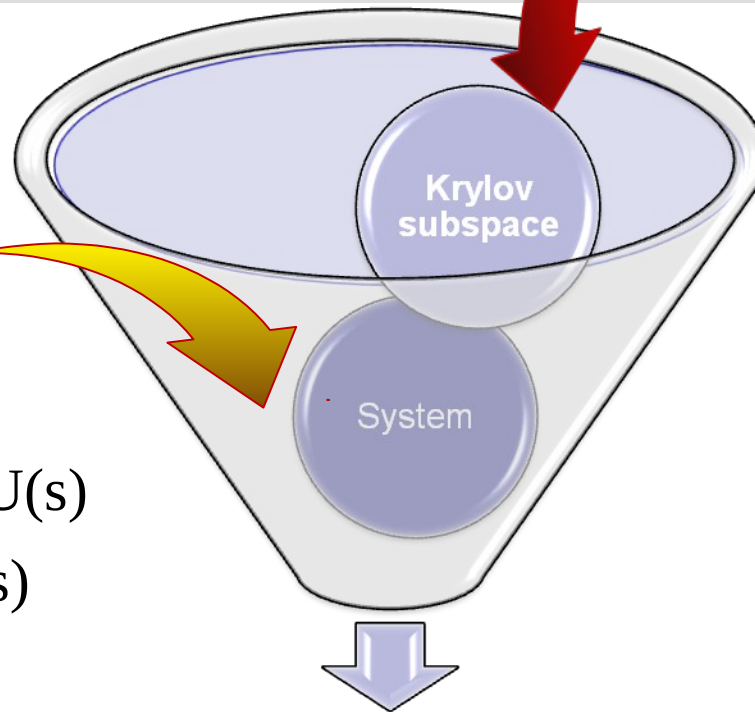
$$sEX(s) = AX(s) + BU(s)$$

$$Y(s) = CX(s) + DU(s)$$



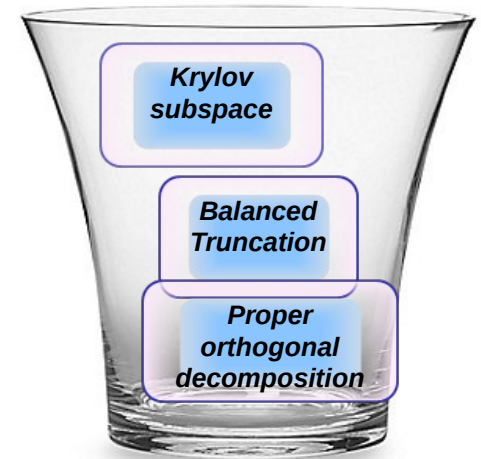
**MOR**  
**Techniques**

# EXPANSION POINT



$$sEX(s) = AX(s) + BU(s)$$

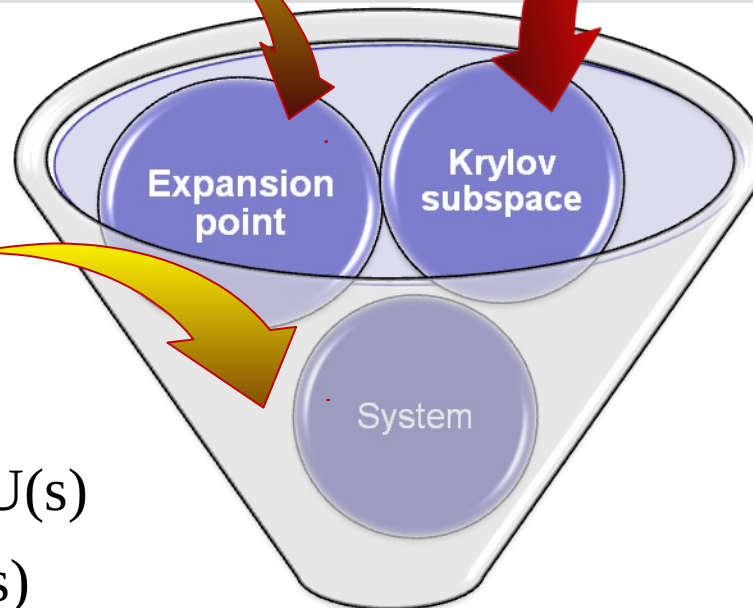
$$Y(s) = CX(s) + DU(s)$$



**MOR**  
**Techniques**

# EXPANSION POINT

$$H(s) = m_0 + m_1(s - s_0) + \dots + m_i(s - s_0)^i - \dots$$

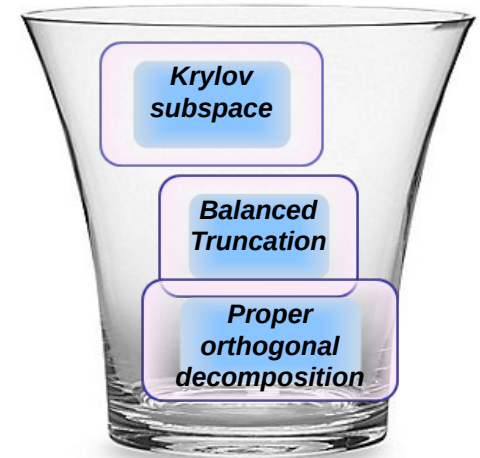


$$sEX(s) = AX(s) + BU(s)$$

$$Y(s) = CX(s) + DU(s)$$

$$sE_r X(s) = A_r X(s) + B_r U(s)$$

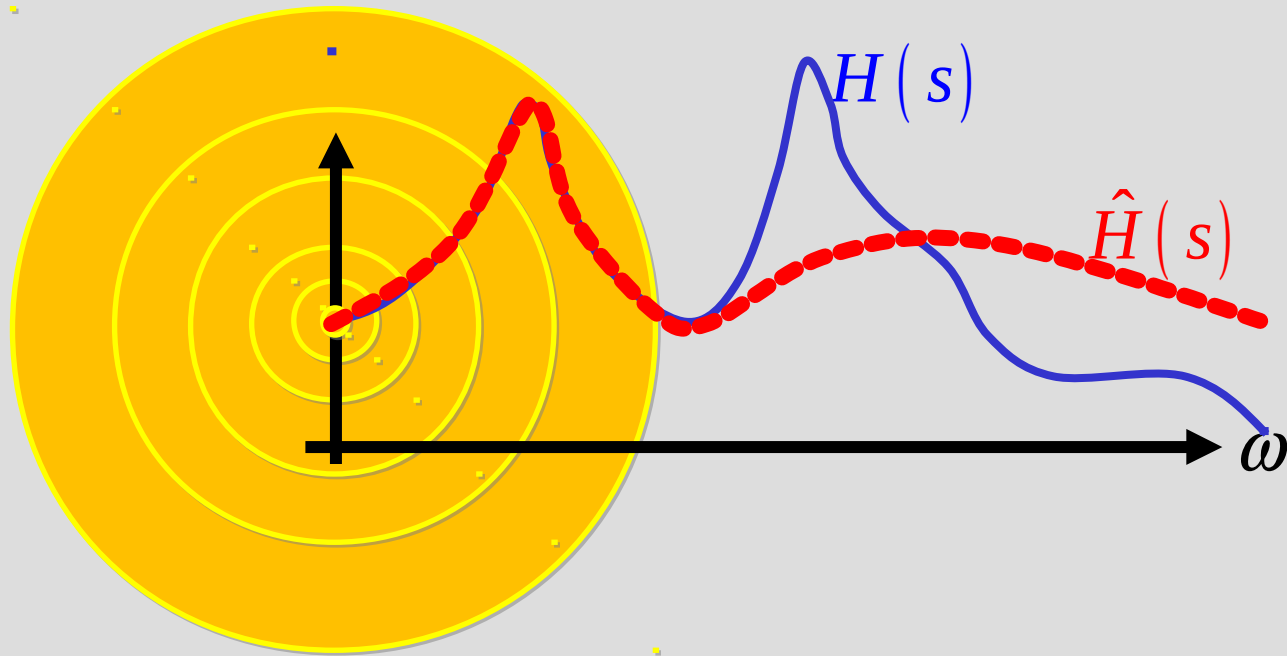
$$Y(s) = C_r X(s) + D_r U(s)$$



**MOR**  
**Techniques**

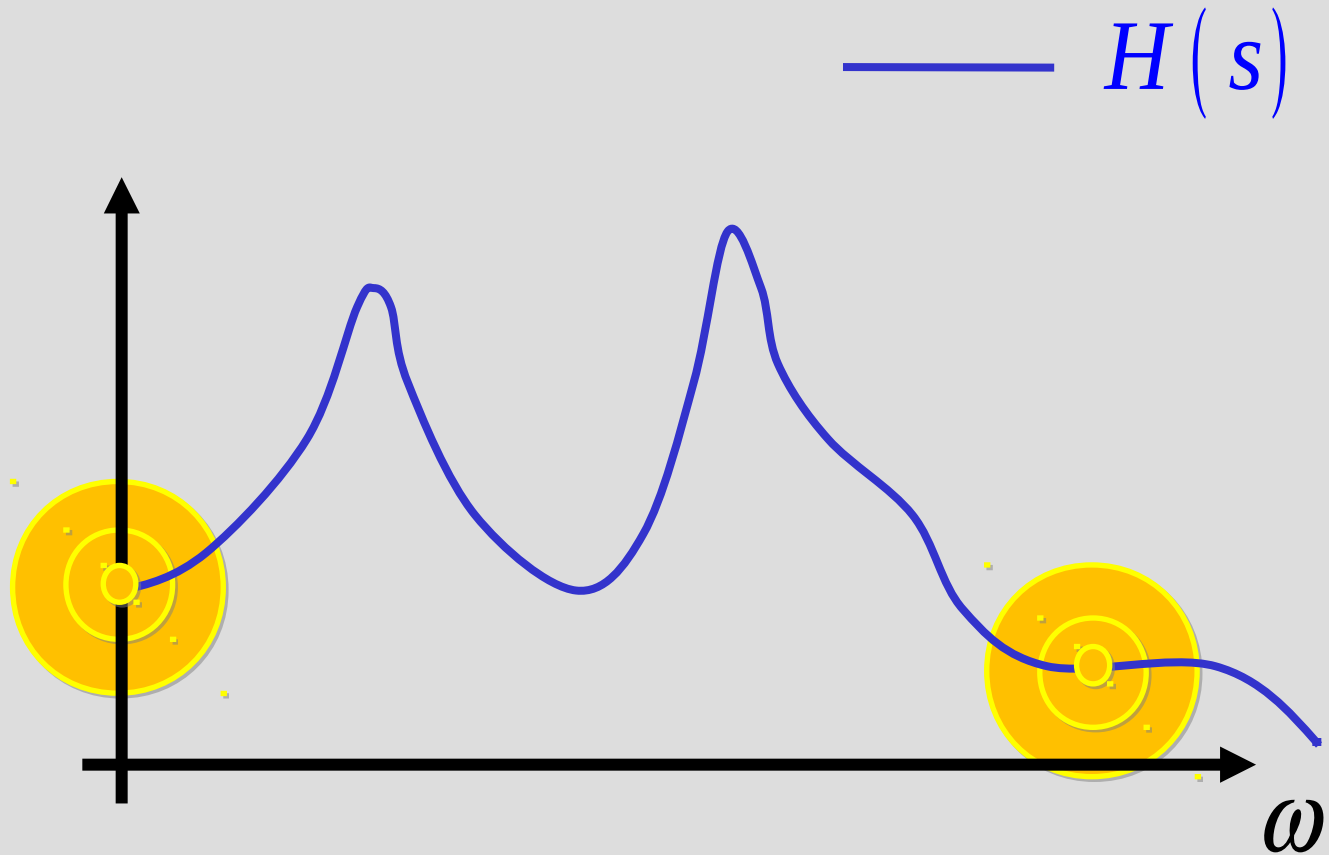


# EXPANSION POINT



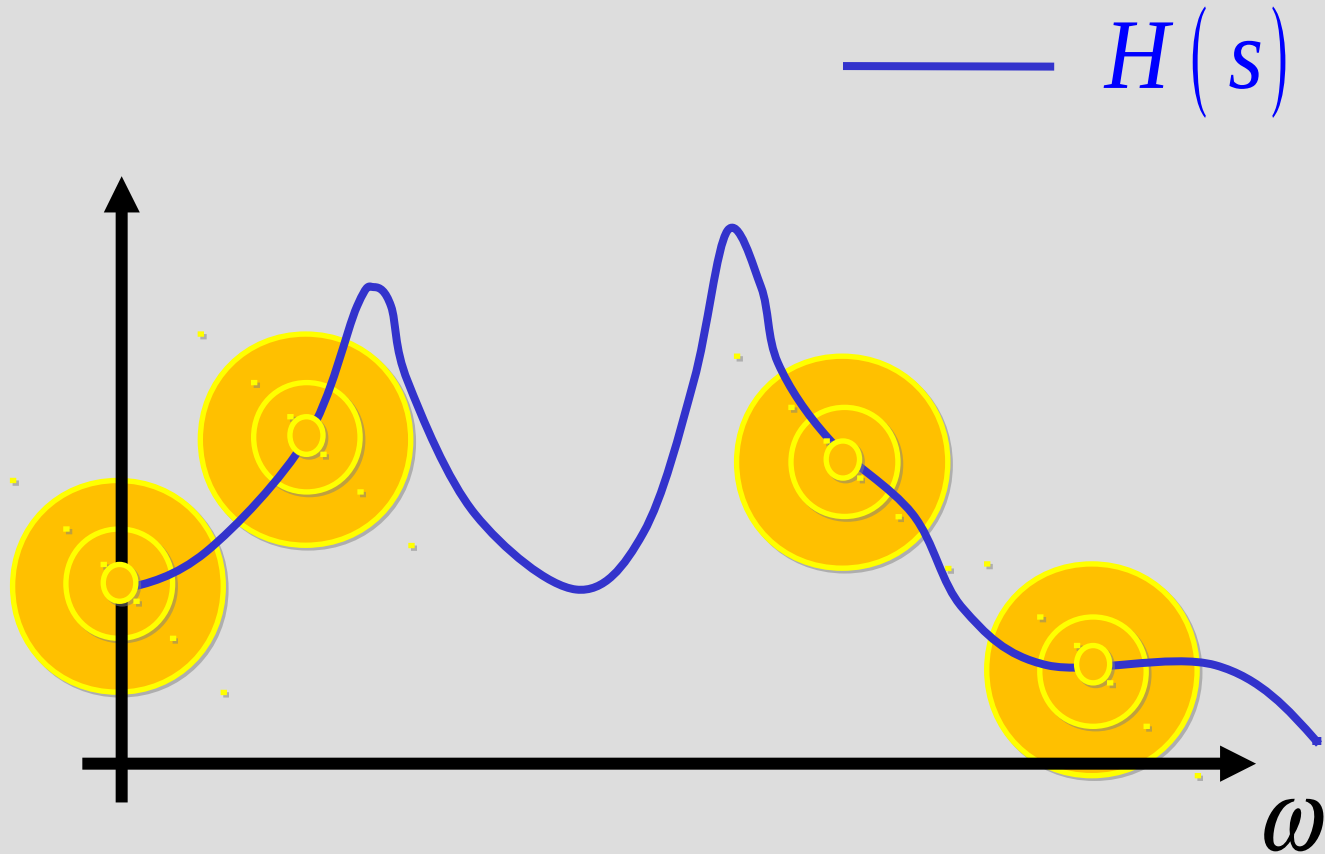
# EXPANSION POINT

*For multiple expansion point*



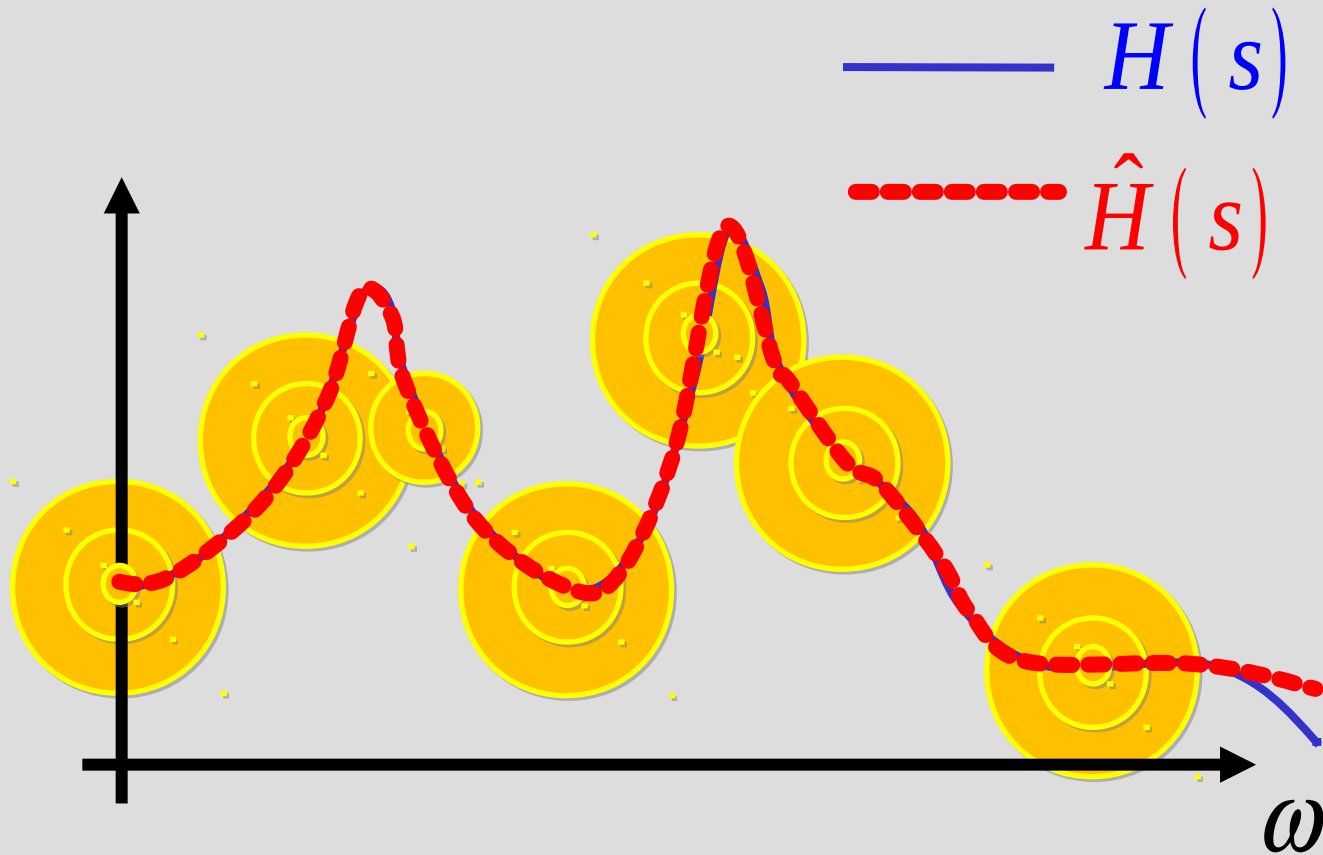
# EXPANSION POINT

*For multiple expansion point*



# EXPANSION POINT

*For multiple expansion point*



# OVERVIEW

- \* Model Order Reduction
- \* Multipoint expansion
- \* **Parameterized modeling**

# *PARAMETERIZED MODELING*

*Let us make a cake*



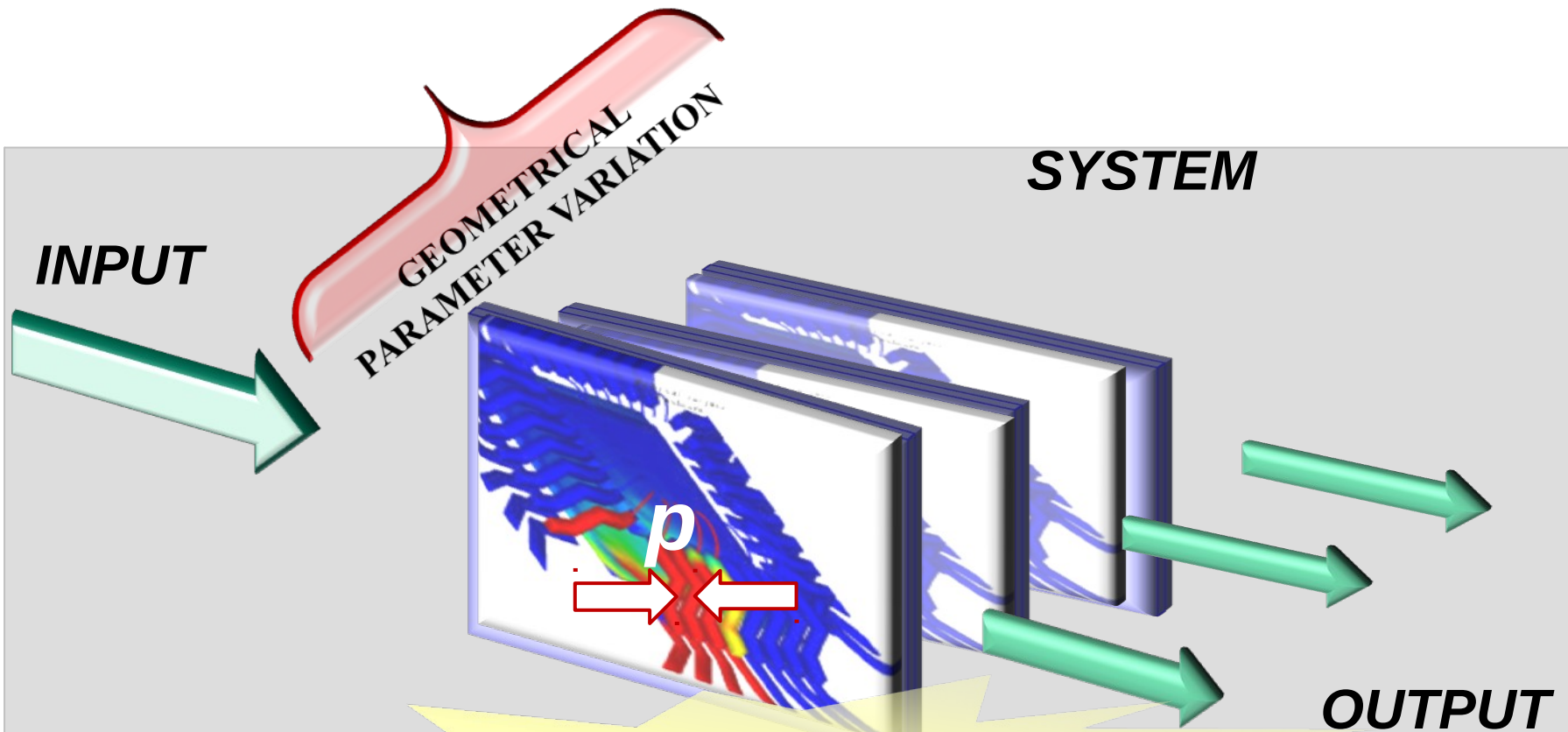


# *PARAMETERIZED MODELING*

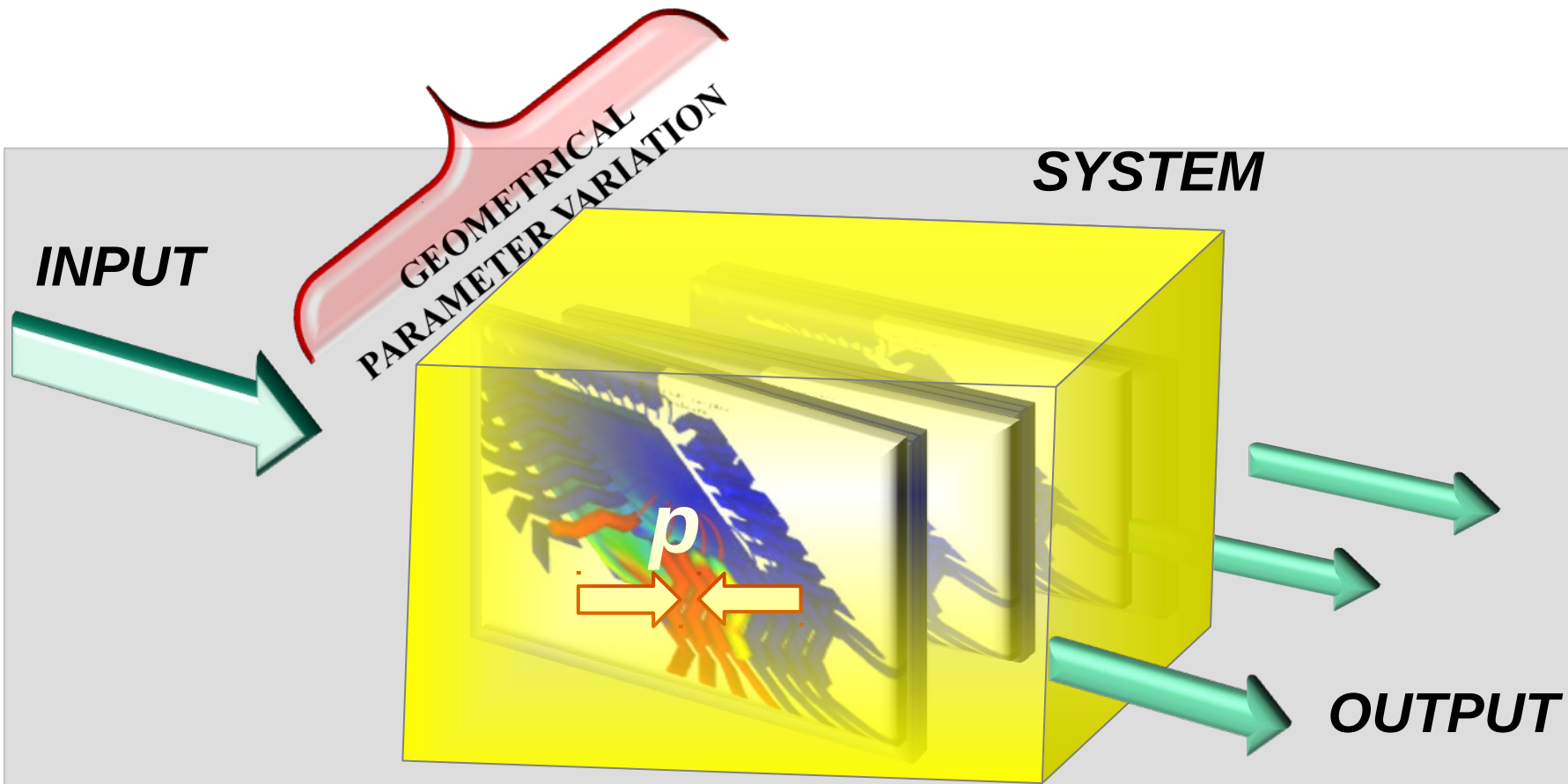


# *PARAMETERIZED MODELING*





**Parameterized modeling** and  
model order reduction for  
large electrical systems



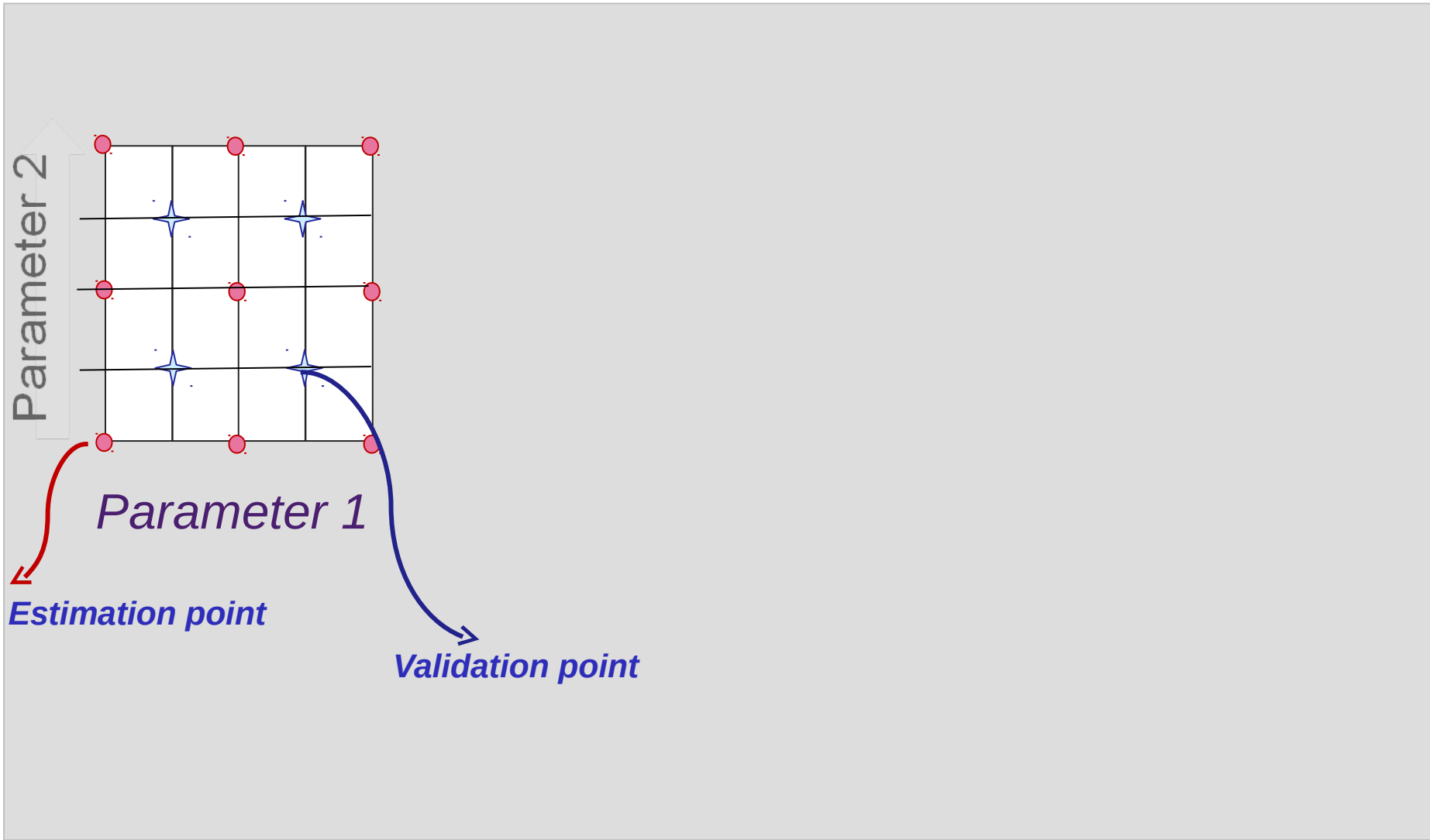
# *RESEARCH CONTRIBUTION*

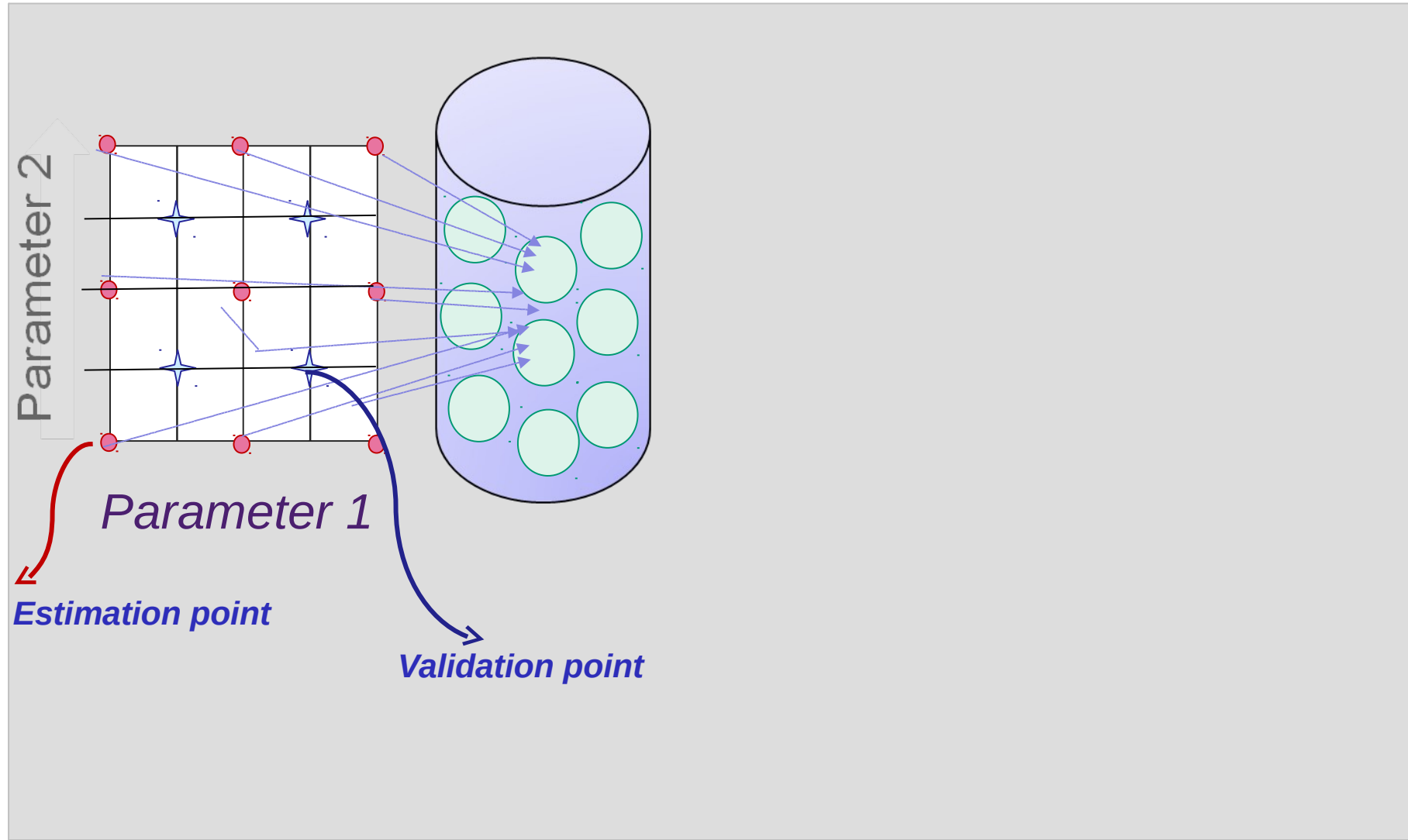
- Model order reduction – **Systems with delay**
- Multipoint expansion – **Adaptive frequency sampling algorithm**
- Parameterized modeling – **Sylvester realization**
- Parameterized model order reduction using a **common projection matrix with state space interpolation**

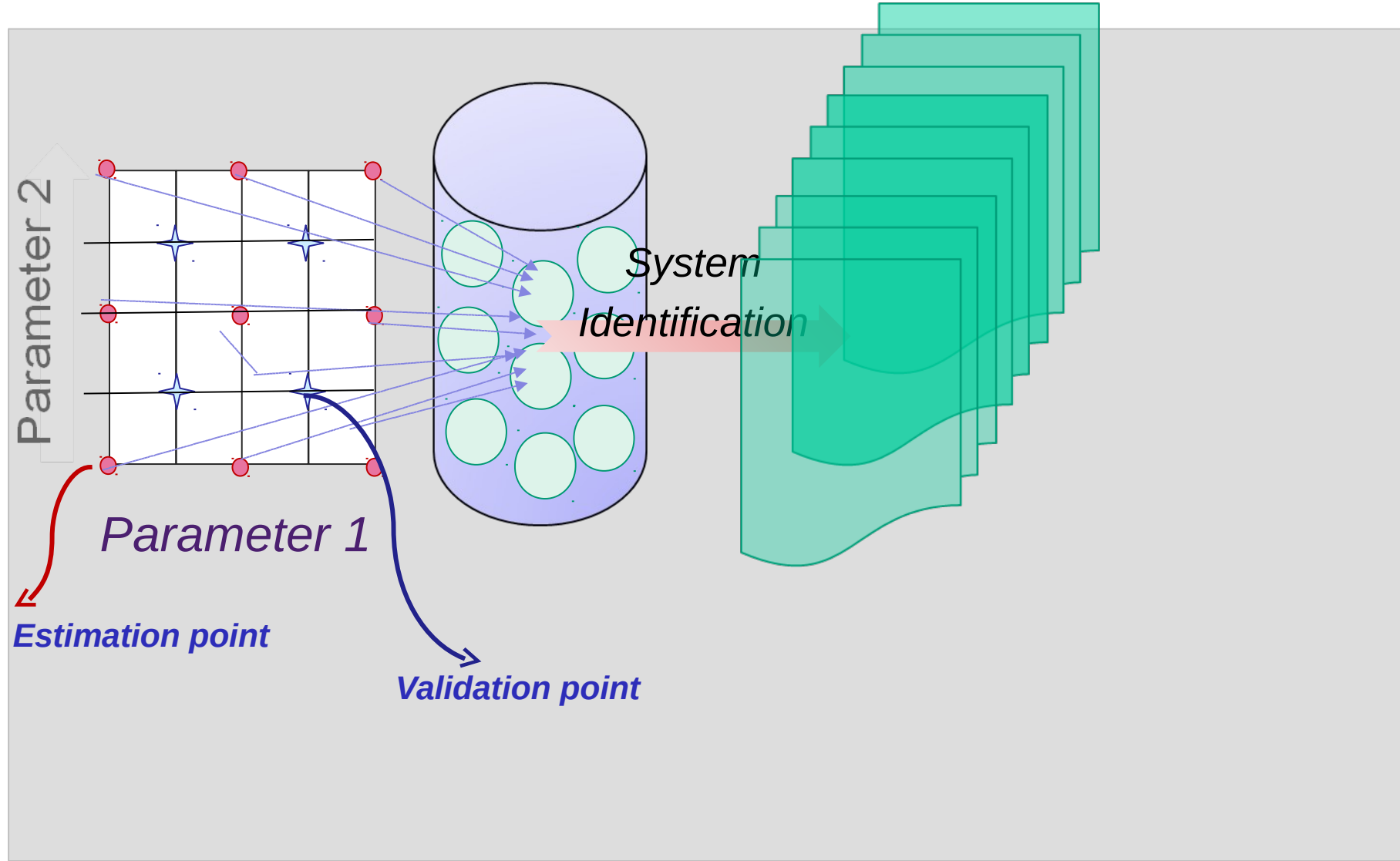
# *RESEARCH CONTRIBUTION*

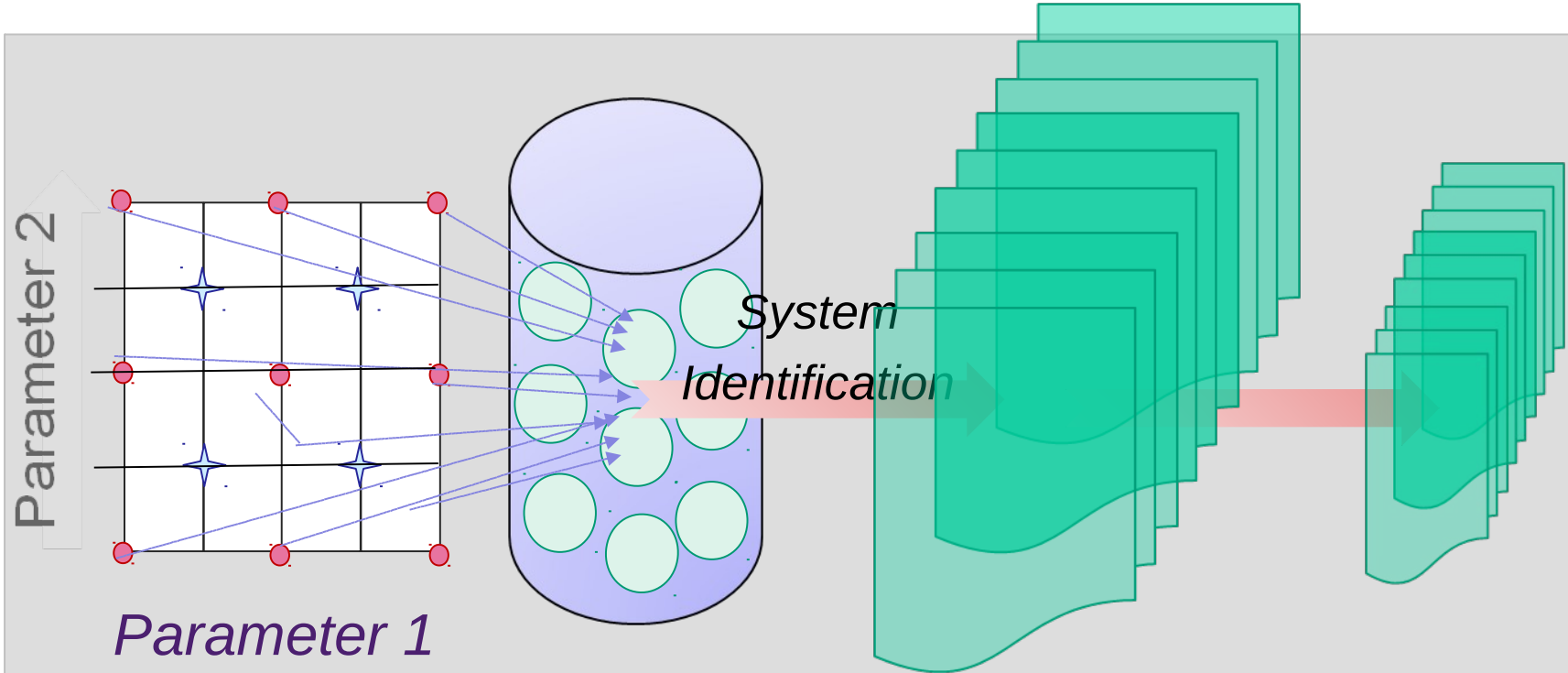
- Model order reduction – Systems with delay
- Multipoint expansion – Adaptive frequency sampling algorithm
- Parameterized modeling – Sylvester realization
- **Parameterized model order reduction using a common projection matrix with state space interpolation**

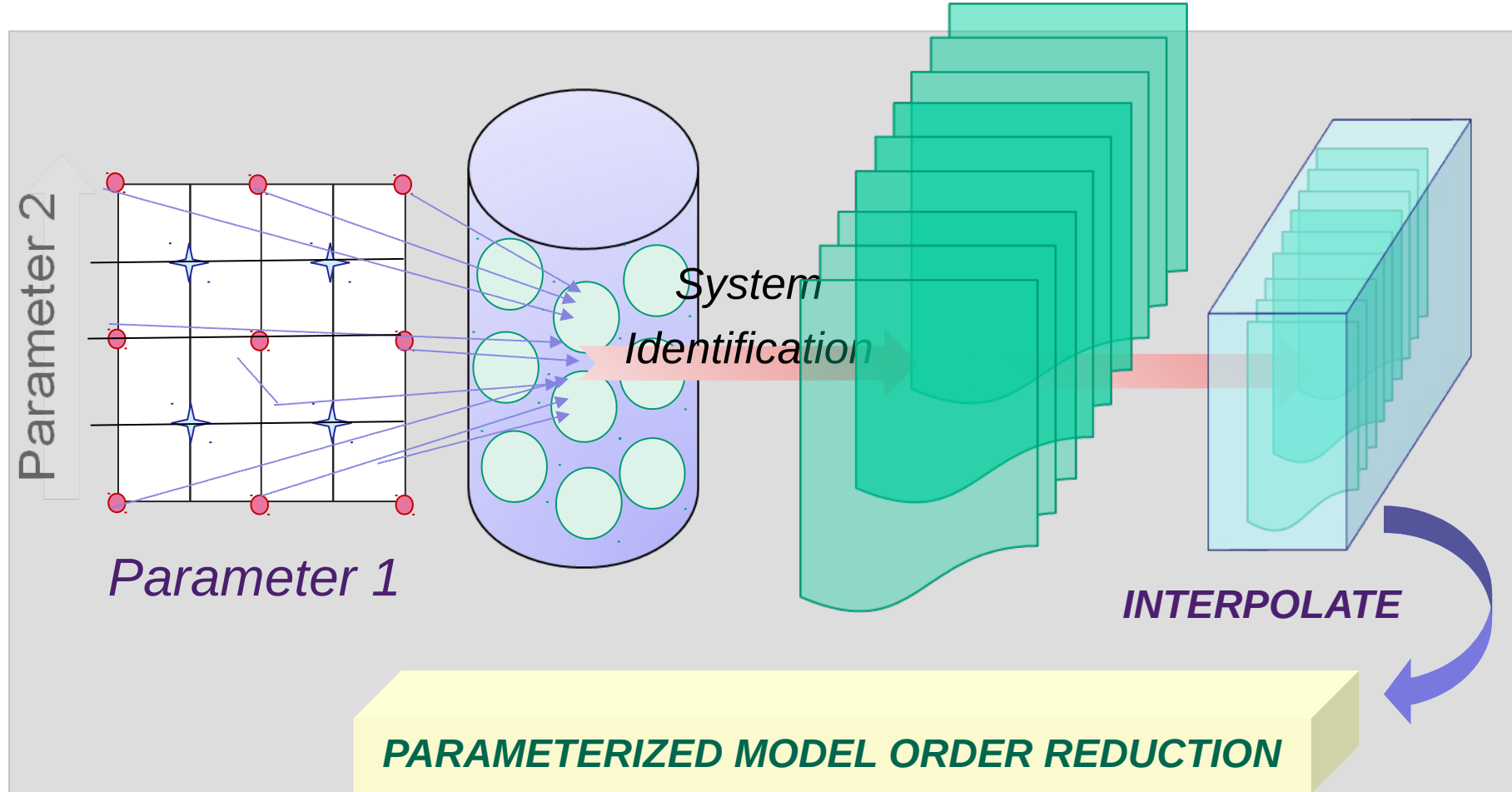


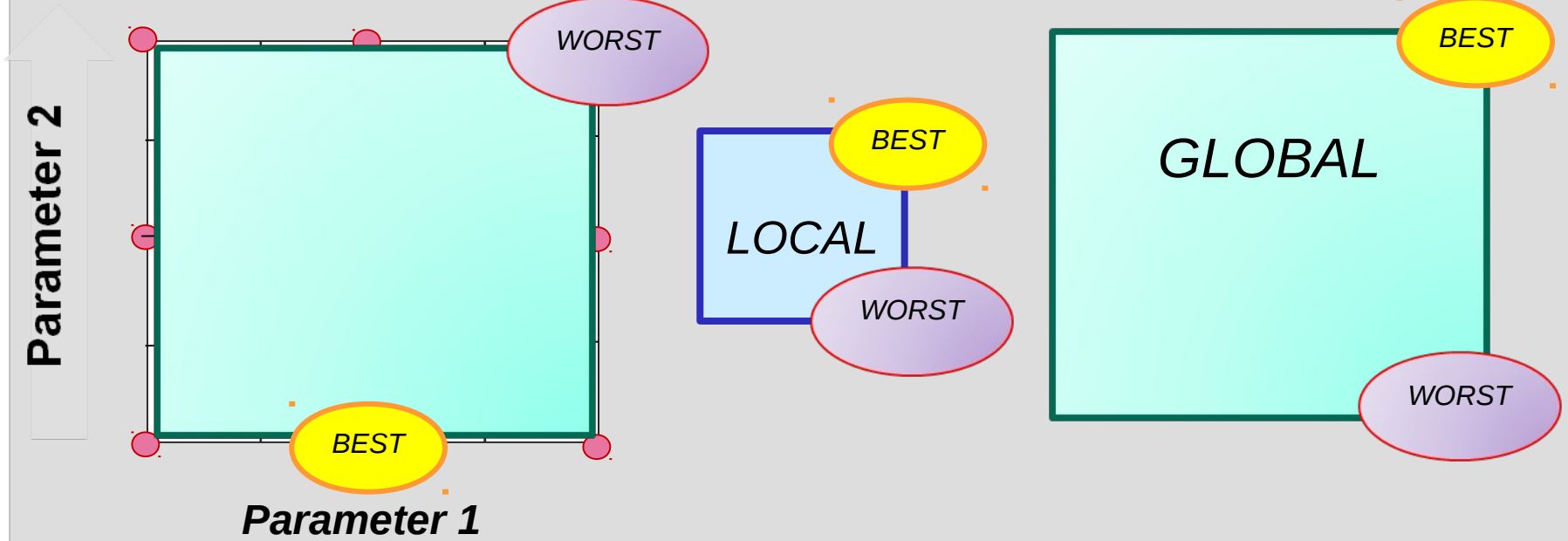






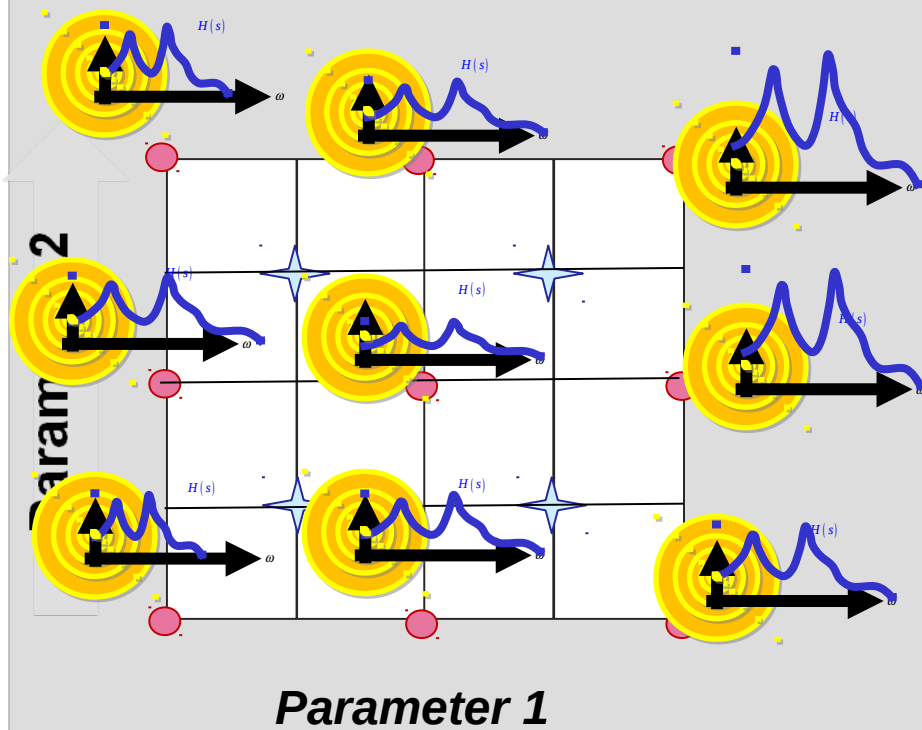




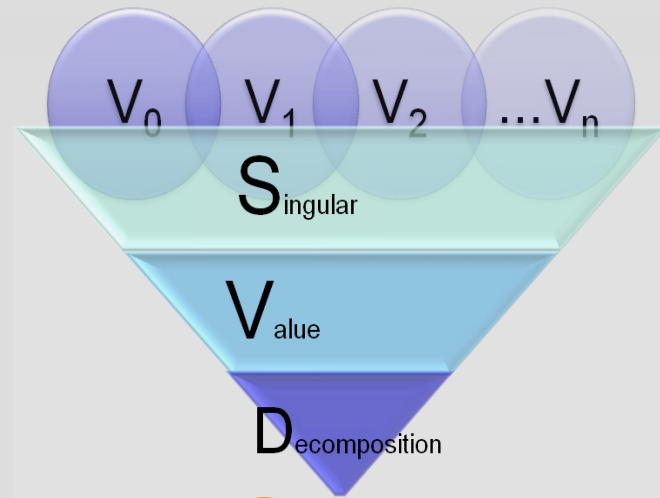
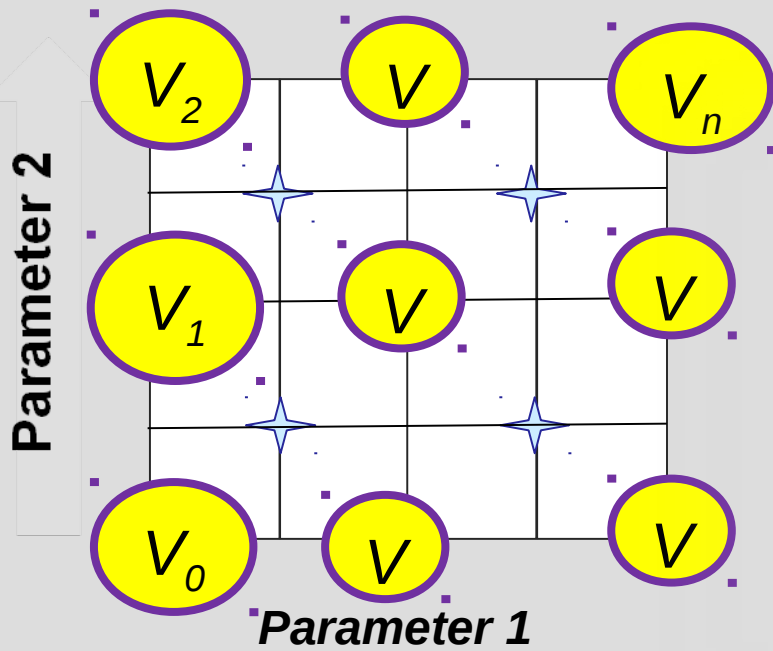
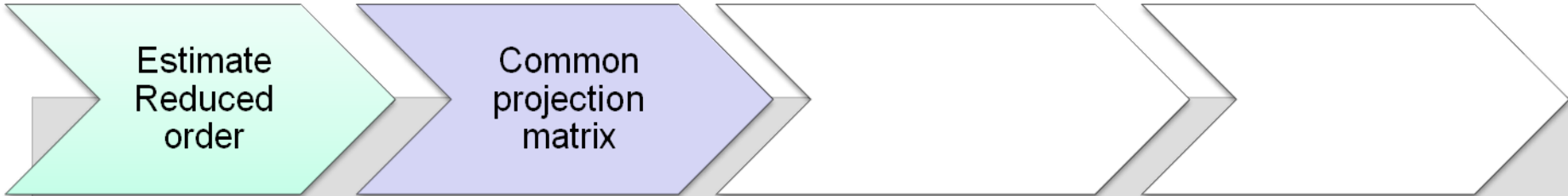


Estimate  
Reduced  
order

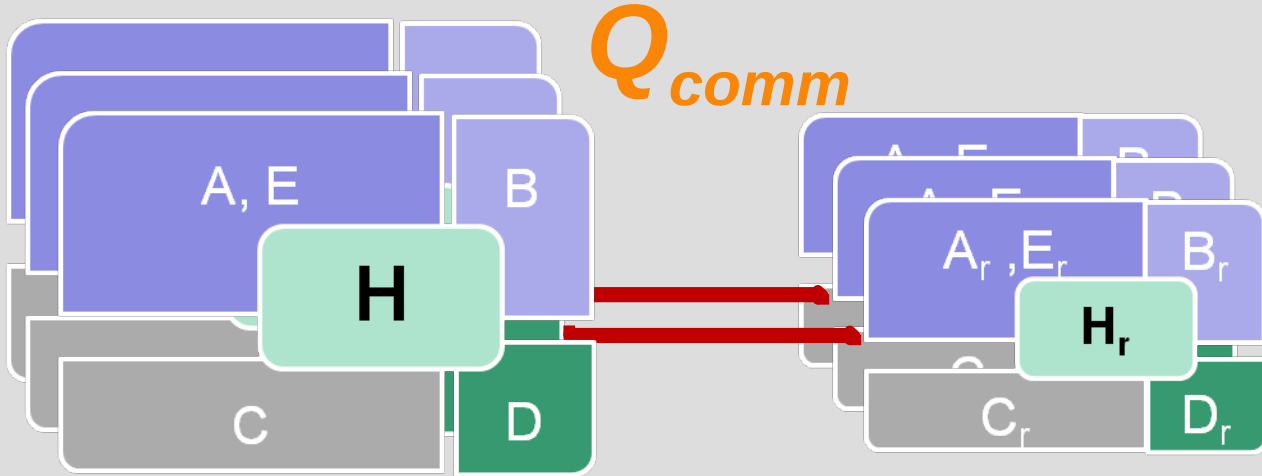
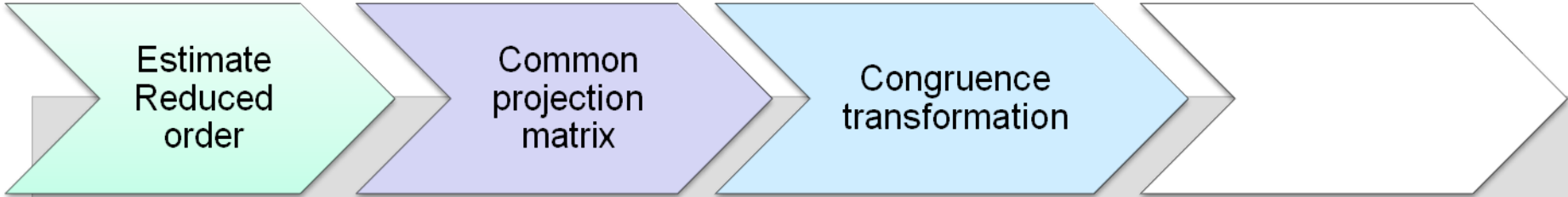
Common  
projection  
matrix

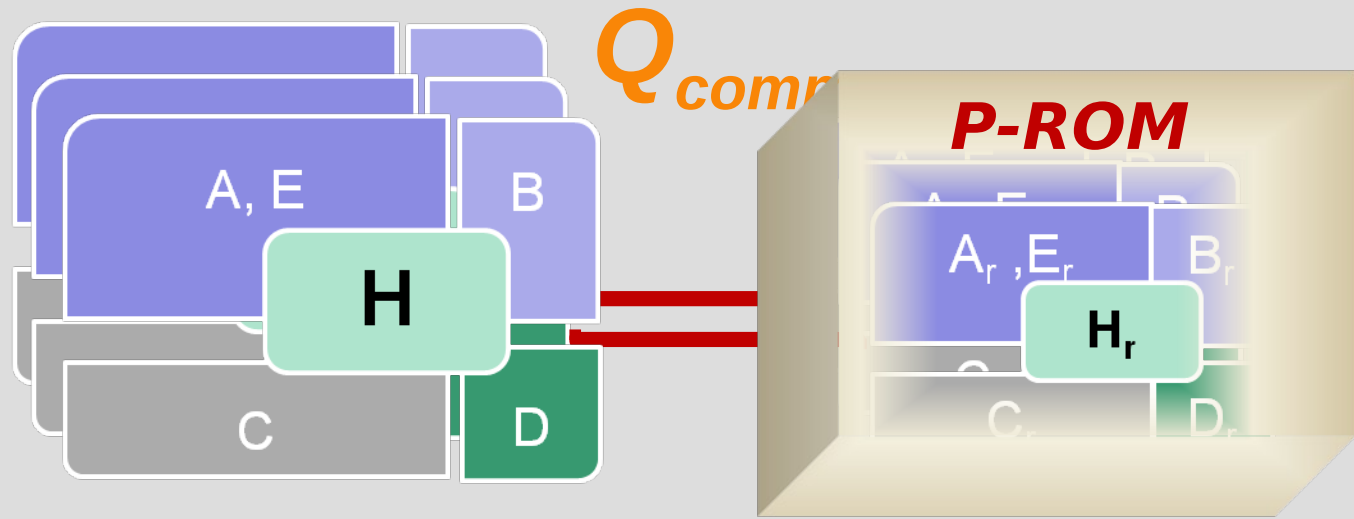
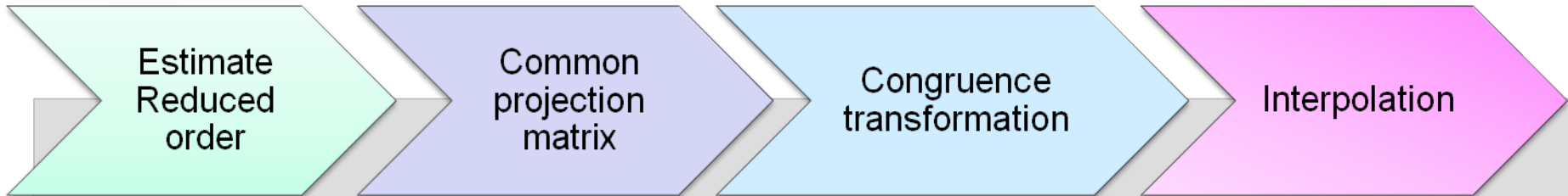


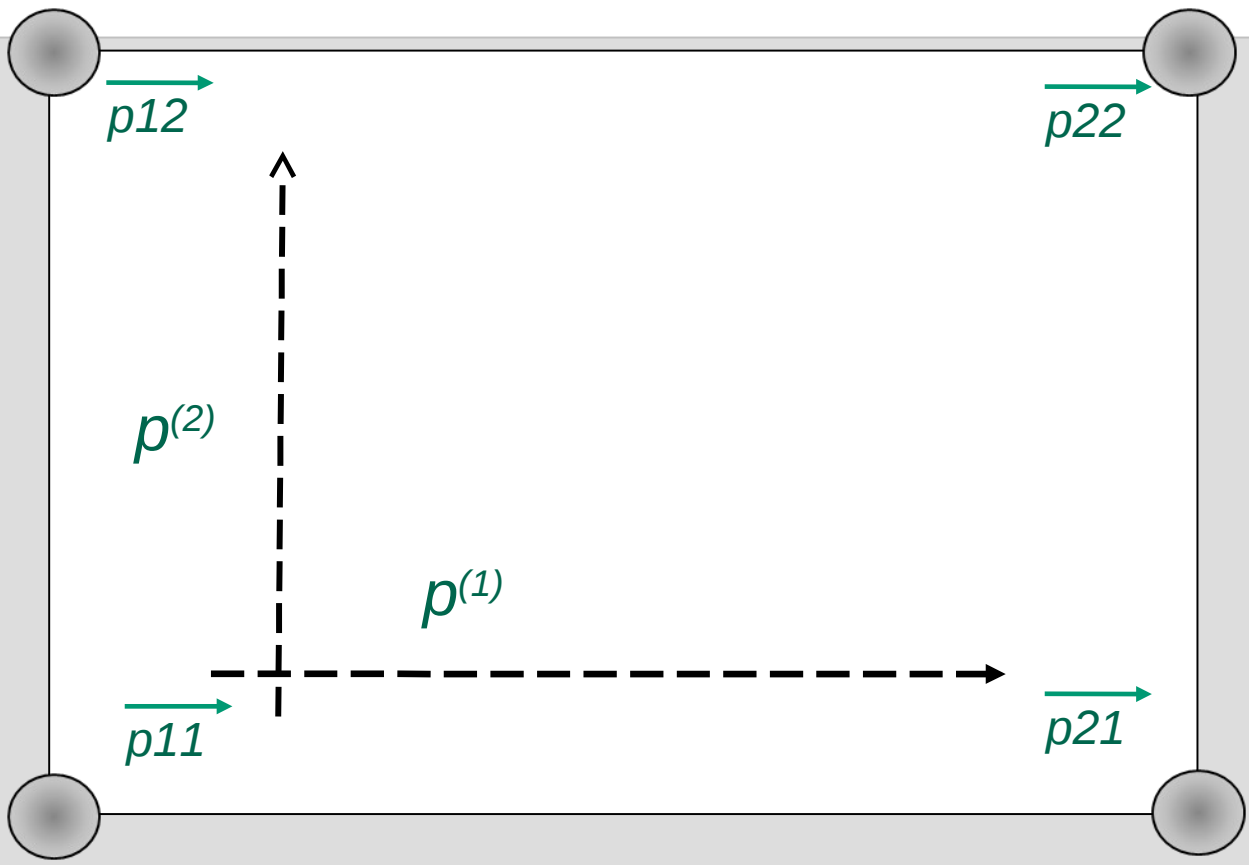


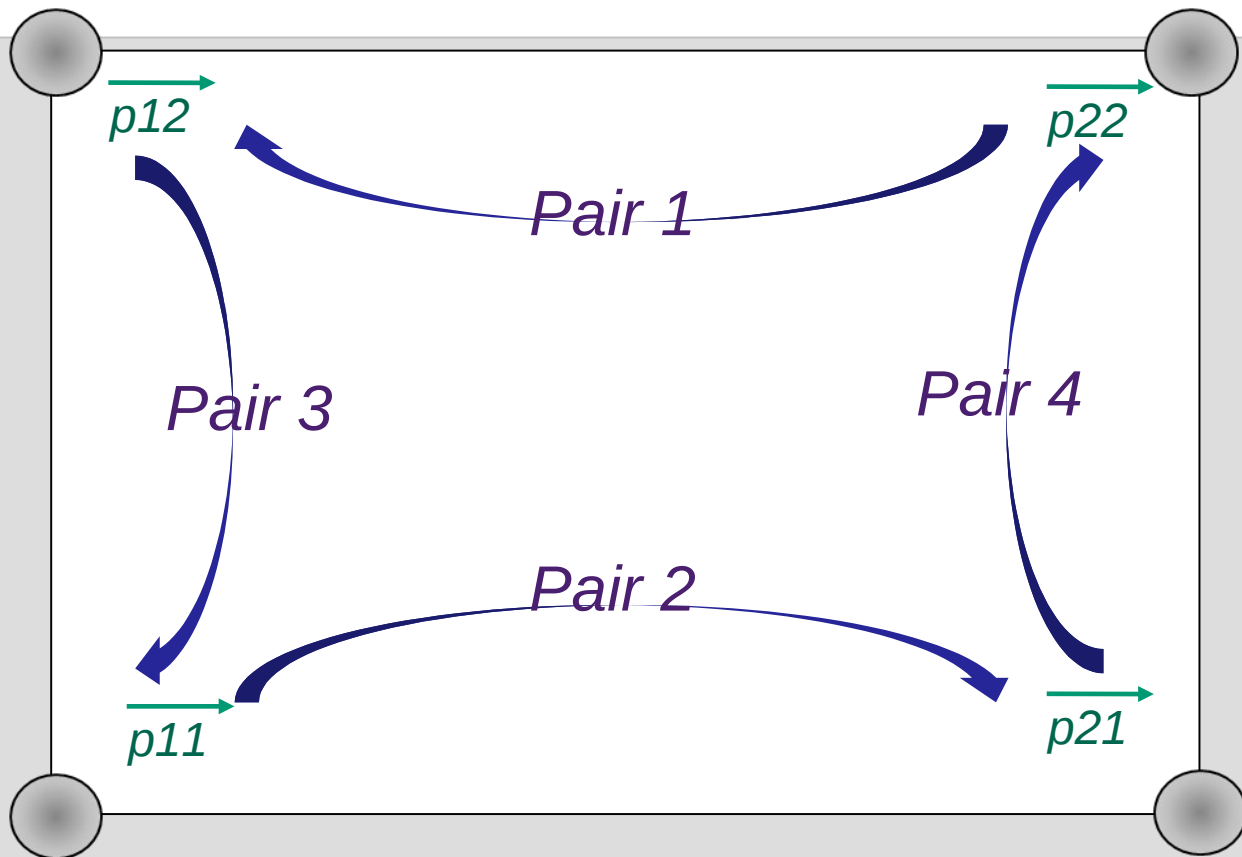


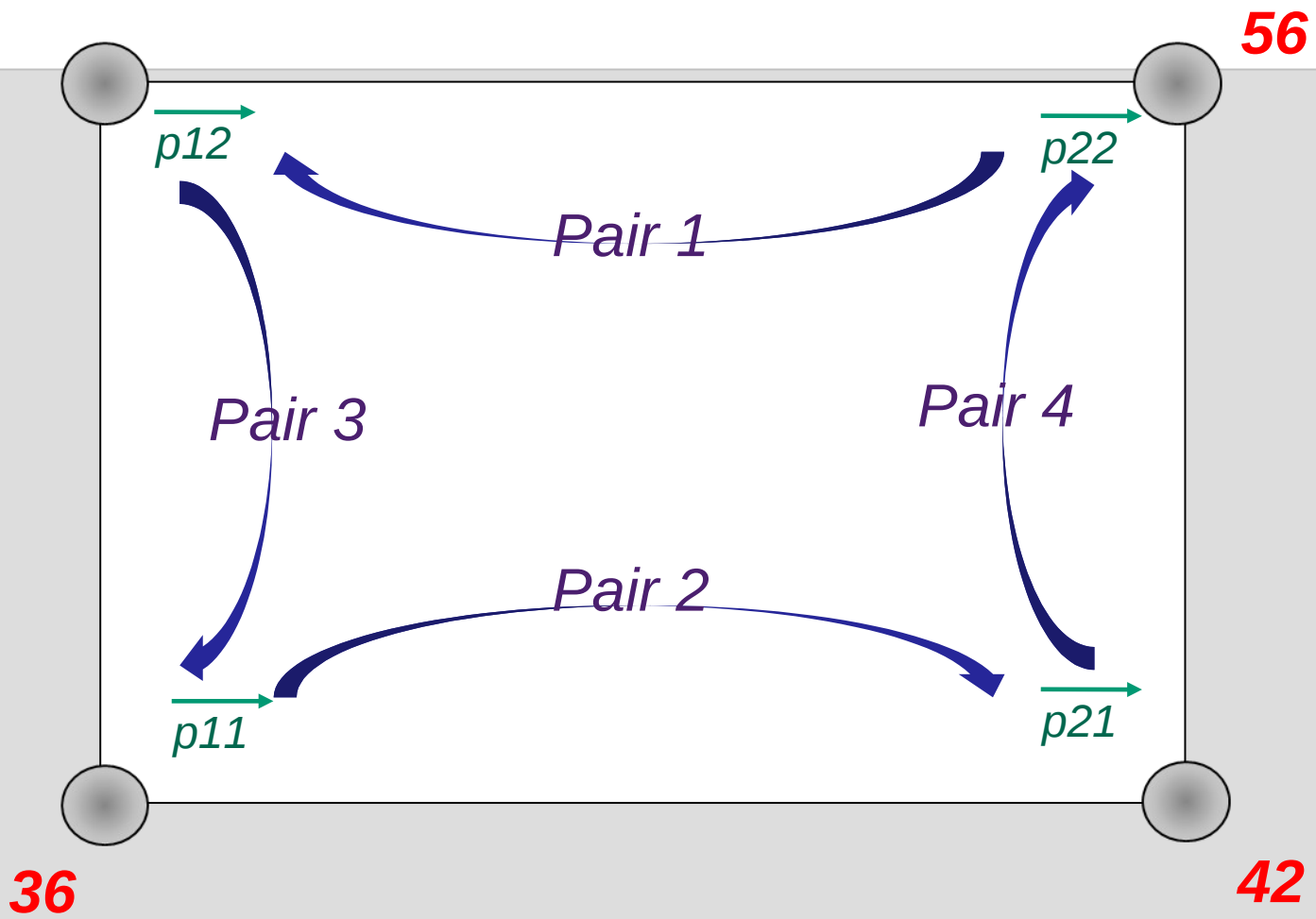
**Q<sub>comm</sub>**

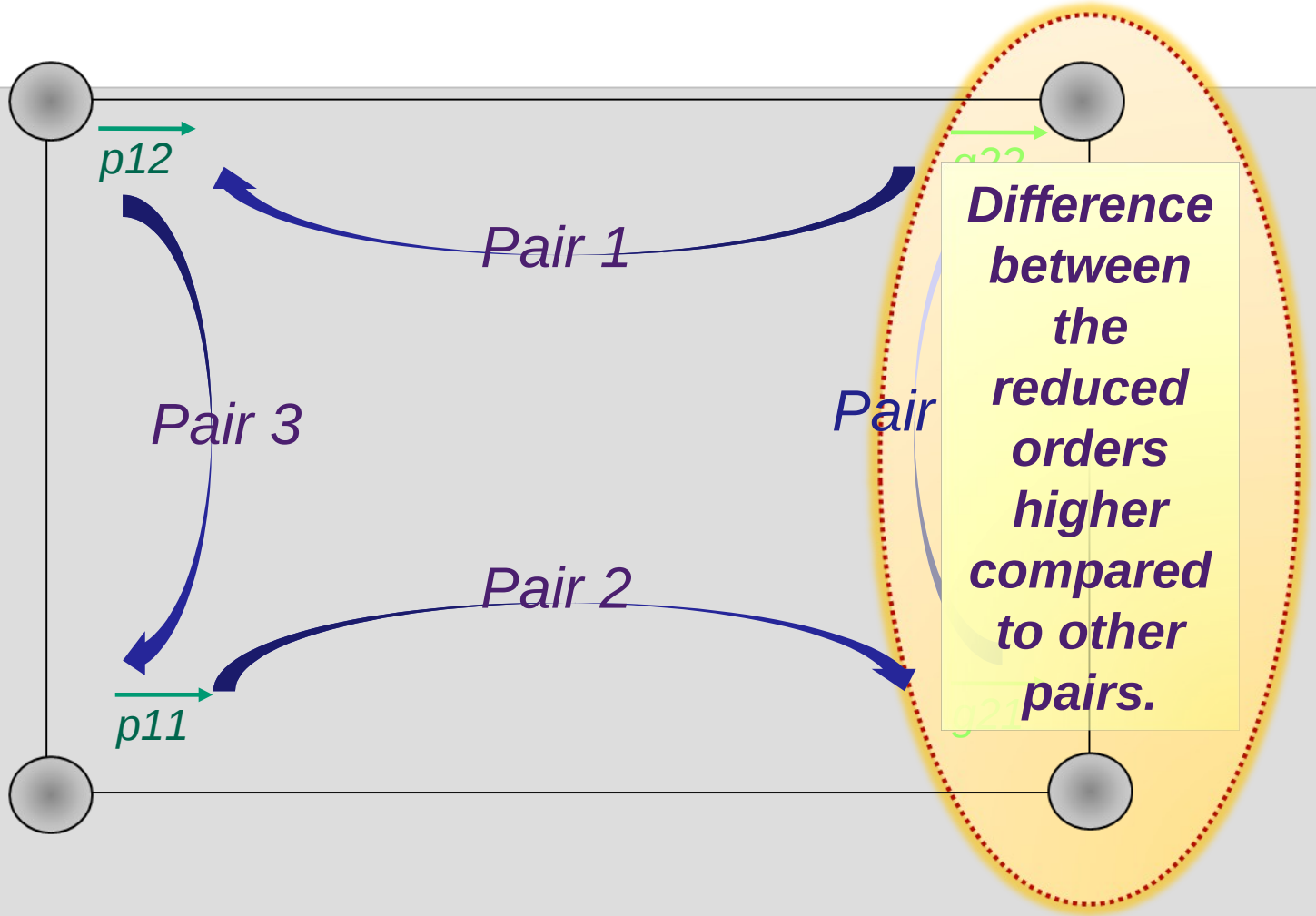


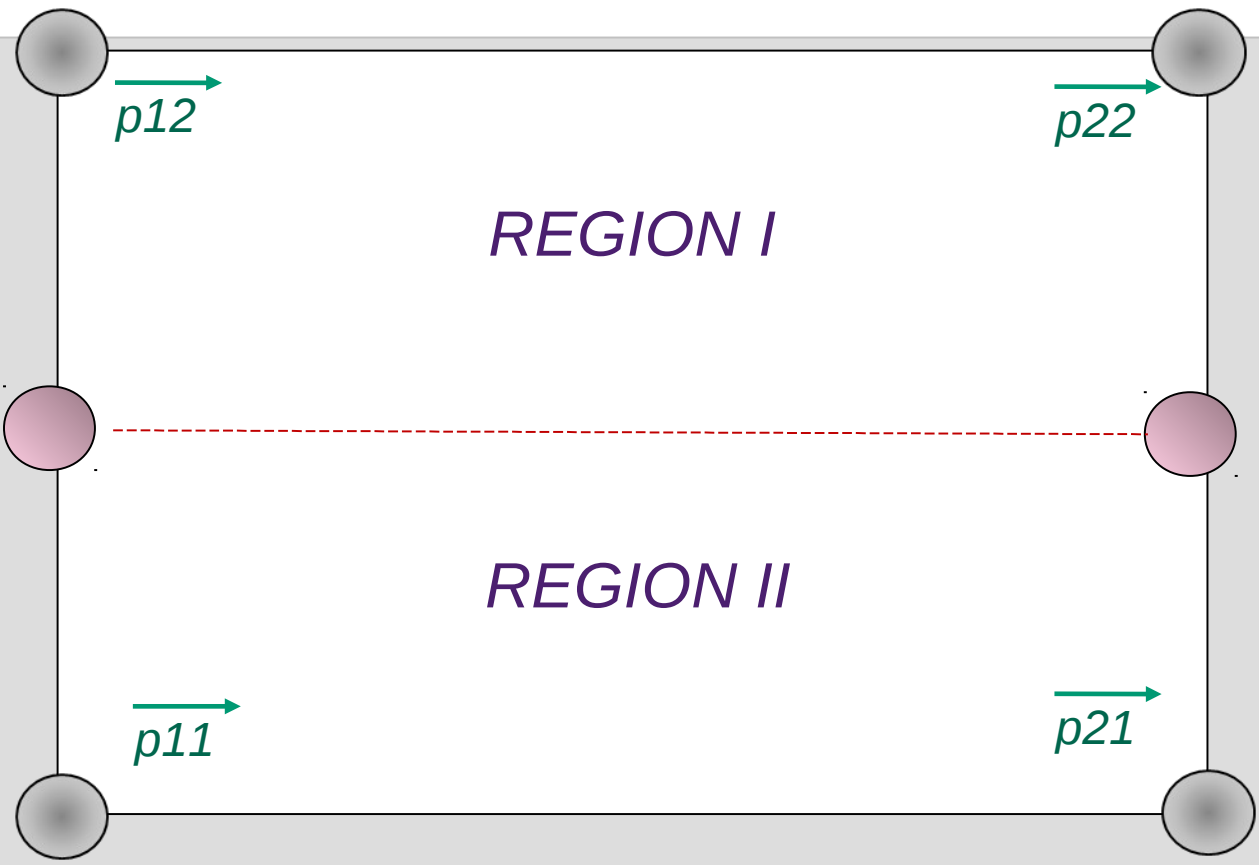




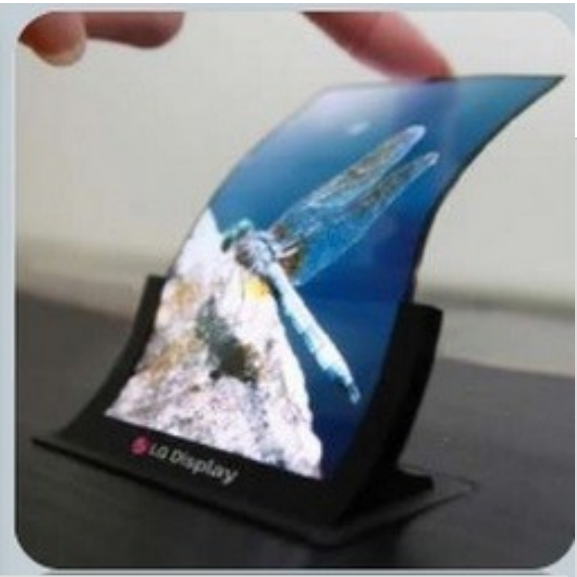


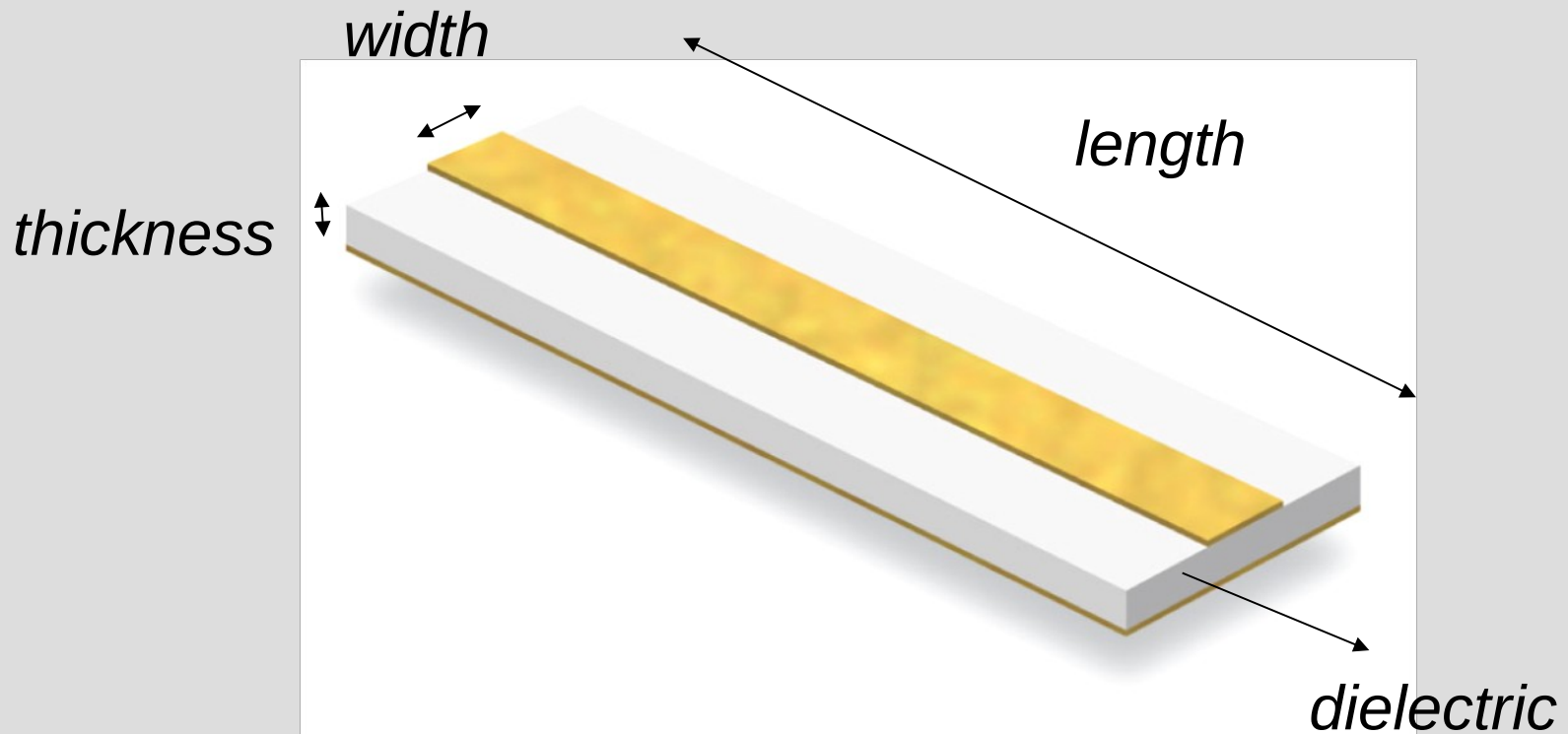




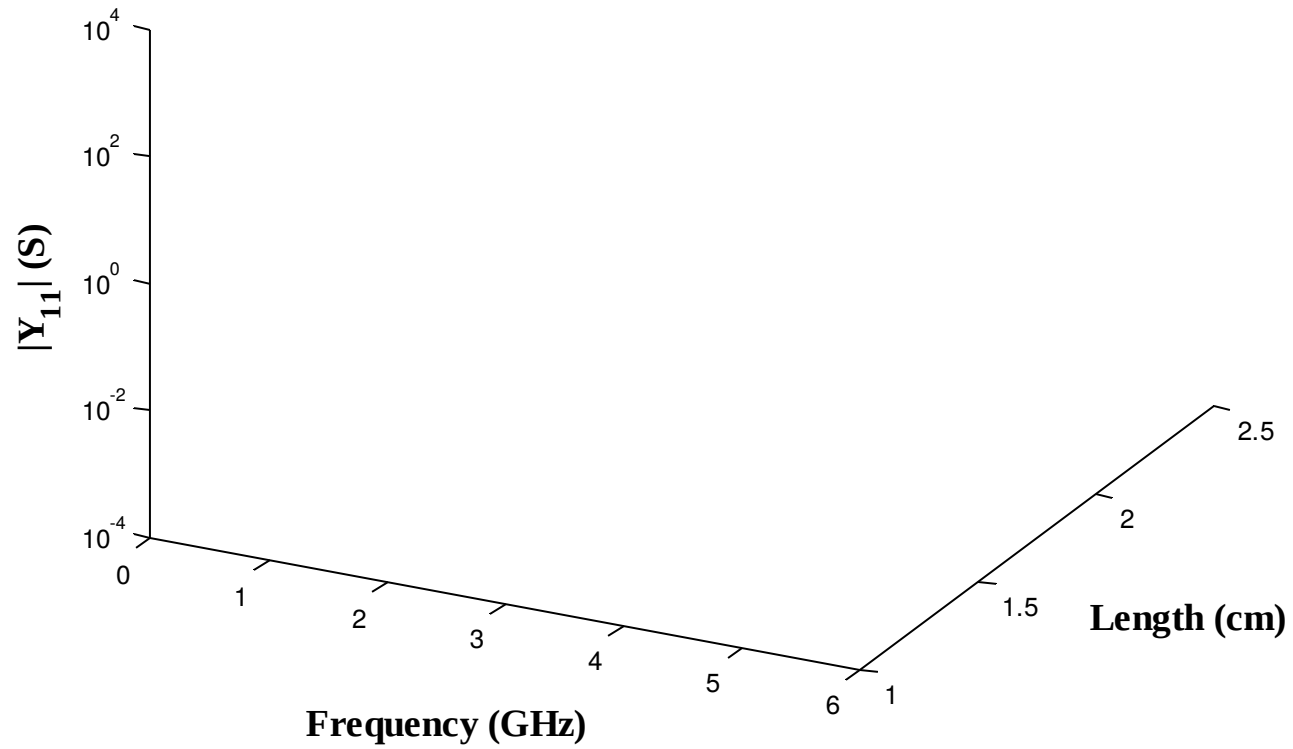




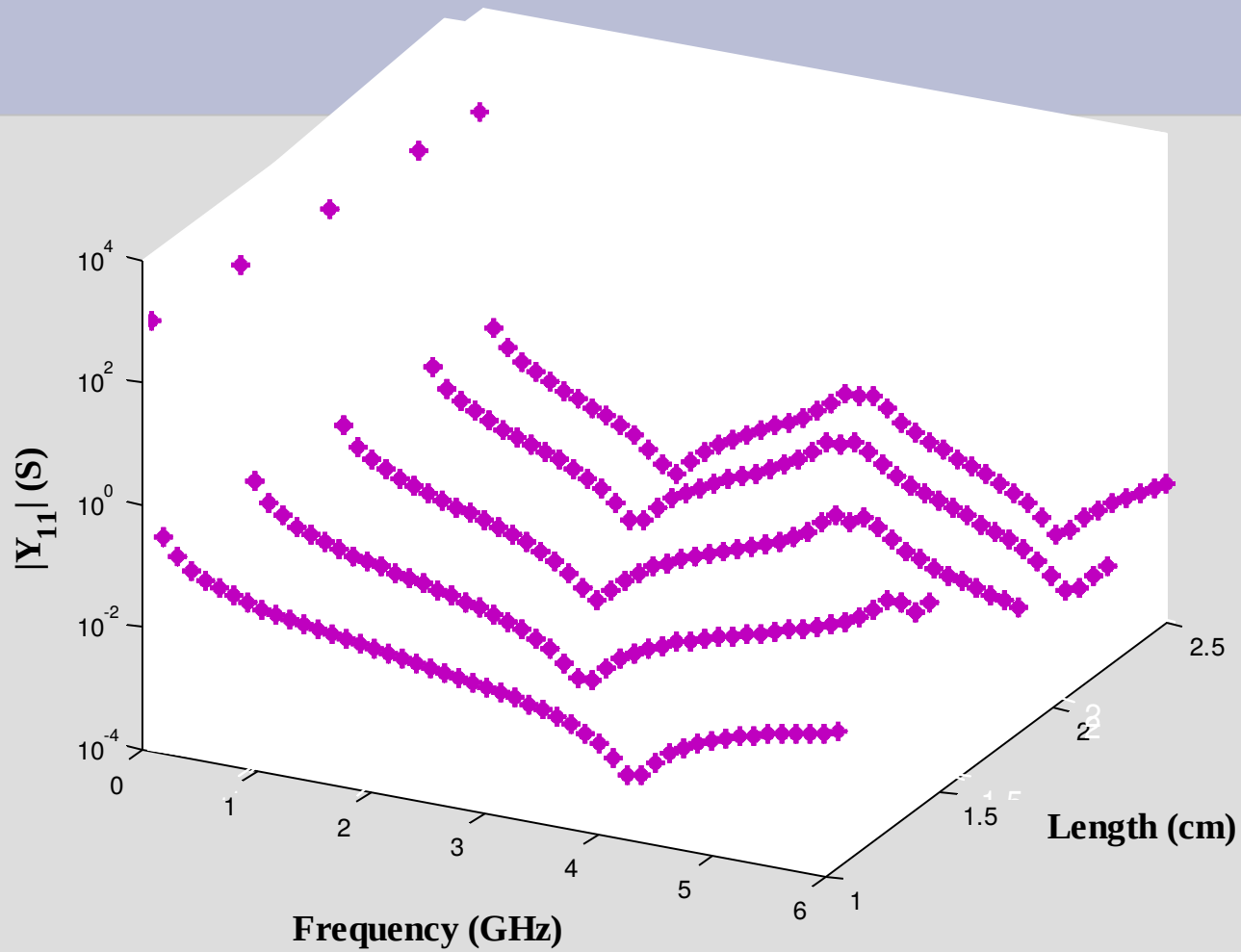


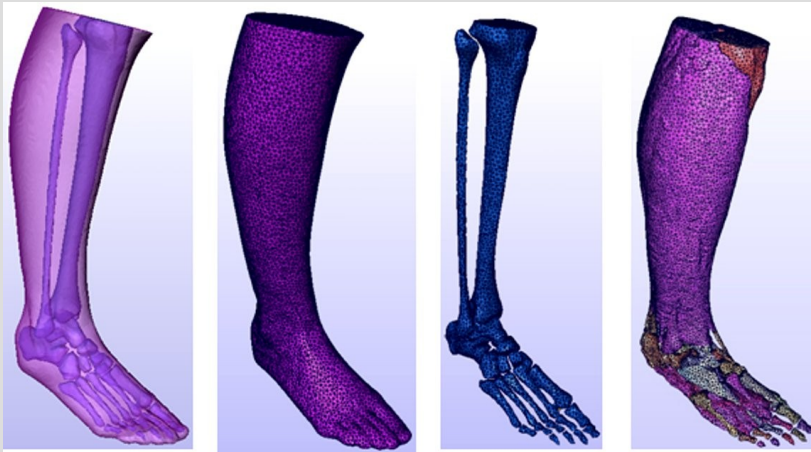
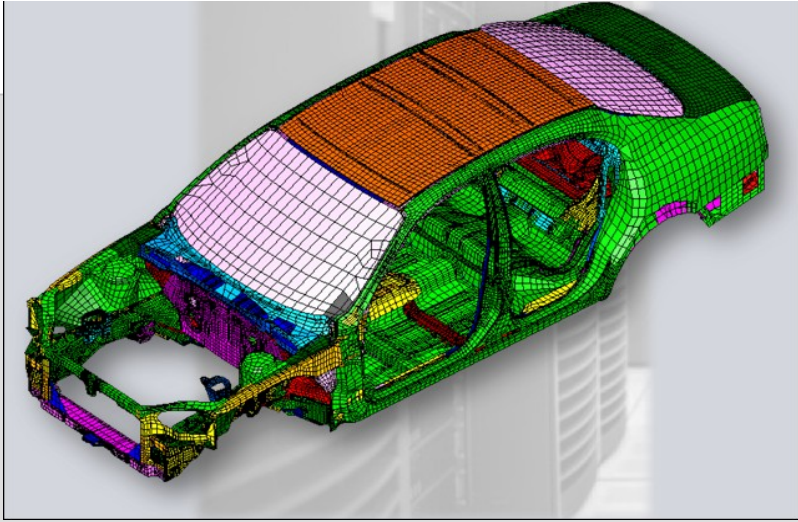


# MICROSTRIP



# MICROSTRIP







***Thank you***

*Elizabeth Rita Samuel*  
*lizita3@gmail.com*

